Multi-Carrier Link-Layer Energy Efficiency and Effective Capacity Tradeoff

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Abstract—A joint energy and spectral efficient power allocation strategy for a point-to-point multi-carrier link, subject to a delay-outage probability constraint, is proposed in this paper. Since the two objectives, namely, link-layer energy efficiency (EE) and effective capacity (EC), conflict with each other, the tradeoff problem falls into the scope of multi-objective optimization problems (MOP). With the \(\varepsilon\)-constraint approach, the MOP is converted into a single-objective optimization problem (SOP) by maximizing the multi-carrier EC, subject to \(\varepsilon\) EE constraint. Then, by introducing an adjustable performance indicator, \(\text{EE-loss-rate} (\alpha_{\text{EE}})\), into the \(\varepsilon\) EE constraint limit, the tradeoff level is flexibly controlled. Finally, we prove that the proposed tradeoff formulation is a concave maximization problem and the optimum power allocation strategy can be derived using Lagrangian method. Analytical results indicate that the proposed power allocation has a similar structure to the one for EE-maximization problem over a frequency-selective fading channel, but with a different cut-off threshold.

I. INTRODUCTION

Green communication networks have received more and more attention in recent years. The three major drivers are: a) increases in carbon dioxide emissions, b) increases in operational expenditures, and c) wider gap between the demand for energy and the offered battery capacity [1]. Firstly, the information and communication technology (ICT) sector is identified to be responsible for approximately 0.75 million tons of CO\(_2\) emissions for every 1 TeraWatt hour (TWh) energy consumption [2]. At the same time, it is known that ICT industry has the potential to reduce more than 23% of its current global green house gases (GHG) emissions [3]. Secondly, GHG effects cause lots of economical issues. In particular, if no action is taken, the overall costs and risks of climate change will be equivalent to losing at least 5% of global gross domestic product (GDP) every year [3]. In contrast, it is claimed that if one-third of the GHG emissions can be reduced, the generated economical benefit will be higher than the required investment [4]. Thirdly, the demand for wireless traffic is growing, while the improvement in battery technology is sluggish, about 10% increase every two years [5], as opposed to the power consumption of the processor, increasing by 150% every two years. This leads to a rapidly increasing gap between the demand for energy and the offered battery capacity. All these facts indicate that green communication networks are imperative.

Energy efficiency (EE) metric, in b/J/Hz, and spectral efficiency (SE), in b/s/Hz, have been considered as two key performance indicators for green wireless communication systems. However, considering the compromise between the network performance and energy savings, how to balance the two conflicting objectives is a real challenge. The EE-SE tradeoff problem in a downlink orthogonal frequency division multiple access (OFDMA) network was considered in [6], which proposed an EE-maximization problem under a minimum overall throughput requirement and a series of minimum rate requirements. A joint power and subcarrier allocation scheme to maximize EE under minimum rate requirements for the service requested by each user, in cooperative cognitive radio networks, was proposed in [7]. A new green performance metric, namely, resource efficiency for EE-SE tradeoff; in a single cell downlink OFDMA network was introduced in [8], which used a weighted sum method to achieve an adjustable tradeoff formulation. For orthogonal frequency division multiplexing (OFDM) networks with imperfect channel estimation, an adaptive power loading solution was provided in [9], which addressed the EE-SE tradeoff problem with changeable priority levels of EE and SE.

Overall, in the aforementioned studies, the system throughput was given by Shannon limit, which ignored the delay quality-of-service (QoS) requirements. However, for many new mobile multimedia applications, which are delay-sensitive and power-consuming, such as video conferencing and online gaming, delay QoS requirement is a critical factor [10] [11]. In this matter, link-layer effective capacity (EC) metric has been recently proposed to specify the maximum constant arrival rate under a delay-outage probability constraint [10]. And the link-layer EE can be defined as the ratio of EC to the total expenditure power. However, it is known that EE-maximization and EC-maximization approaches can be conflicting [10], [12]. Therefore, the compromise between the two metrics deserves elaborate study.

In this trend, using a curve fitting method, signal-to-noise ratio (SNR) was expressed in terms of EC in frequency flat-fading channels in [13]. Then, EE, as a function of SNR, and in turn, as a function of EC, was analyzed. Finally, EE-EC curve was provided in [13] and the impact of circuit power and QoS requirements on EE-EC curve have been demonstrated by simulation results. Considering frequency flat-fading channels, an optimal power allocation strategy to maximize EC subject to an EE constraint, for delay-limited mobile multimedia applications was obtained in [14]. We note that the total average rate of a multi-carrier system, such as in [6]–[9], is a linear summation of the achievable average rate of each carrier. This, however, does not apply to systems with delay-limited applications. In delay-constrained systems, it is known that the concavity and monotonicity of EC do not remain homogeneous for single-carrier and multi-carrier...
systems [15]. In addition, it has been proven that the optimal power allocation strategy for single-carrier systems cannot be simply extended to multi-carrier systems [15]. Therefore, the joint energy and spectral efficient power allocation strategy in a multi-carrier system deserves separate study.

This paper addresses the EE-EC tradeoff problem for a multi-carrier link over a frequency-selective fading channel, under a delay-outage probability constraint. Firstly, in order to jointly maximize EE and EC, an MOP is formulated. Then, using the ε-constraint approach, the MOP is converted into an EC-maximization problem subject to a link-layer EE constraint. In order to flexibly control the constraint limit, and consequently control the tradeoff level, an adjustable indicator, referred to as EE-loss-rate (α_{EE}), is introduced. The EE constraint is then defined as a product of α_{EE} and the maximum achievable EE of the channel. We note that the independent power allocation for each subcarrier will not provide an optimal solution for multi-carrier systems [15]. Therefore, a joint optimization over both frequency and time is necessary. Since EC function in a multi-carrier system is concave in transmission power and the link-layer EE is quasi-concave, the proposed EE-EC tradeoff formulation could be treated as a concave optimization problem. Finally, using Lagrangian method, the optimal power allocation strategy is provided.

II. SYSTEM MODEL

We focus on a multiplexing-based system, which at the transmitter side, transmits different data streams through different subchannels and at the receiver side, recovers the parallel data streams separately [15]. To be specific, a wireless frequency-selective fading channel with a total bandwidth of B is considered. In order to combat frequency selectivity, N independent identically distributed (i.i.d.) flat-fading subchannels, each with a bandwidth of B/N, are employed.

Similar with the multi-carrier system model which is considered in [16], firstly, the upper-layer packets are divided into frames at the data-link layer. The frames are stored at the transmit buffer and split into bit streams at the physical layer. Then, based on the channel-state information (CSI) and QoS constraint, adaptive modulation and coding (AMC) and power policy are applied at the transmitter [15]. Then, the bit streams are read out of the buffer and transmitted through N subcarriers.

Since each subcarrier is assumed to be experiencing block fading, the channel gains of N subcarriers are invariant within a fading-block’s time duration T_{t}, but independently varies from one fading block to another. In addition, the length of each fading-block, T_{t}, is considered to be an integer multiple of the symbol duration T_{s}, and is assumed to be less than the fading coherence time [15].

For the n^th subcarrier at fading-block index t, the subcarrier power gain is denoted as \{\gamma_{n}[t]\}, n \in \mathcal{N}_0, \mathcal{N}_0 = \{1, 2, \ldots, N\} represents the set of all subcarriers. The joint probability density function (PDF) of the subchannel power gains, \gamma[t] = \gamma_1[t] \gamma_2[t] \ldots \gamma_N[t], is given by \rho(\gamma). Each subcarrier is also assumed to experience i.i.d. additive white Gaussian noise (AWGN) with power spectral density \vartheta_0/2.

Using Shannon limit, the total instantaneous service rate of the multi-carrier system at the t^th fading-block is given by

\[ R[t] = \frac{1}{N} \sum_{n=1}^{N} \log_2 \left( 1 + \frac{P_n(\theta, \gamma[t]) \gamma_n[t]}{P_{C} \vartheta_0 \left( \frac{2}{N} \right)} \right) \quad \text{[b/s/Hz]}, \]

where \( P_{C} \) denotes the distance-based path-loss power and \( P_n(\theta, \gamma[t]), n \in \mathcal{N}_0 \), as a function of \theta and \gamma[t], is the transmission power for the n^th subcarrier. Since the service rate process \{R[t], t = 1, 2, \ldots \} is considered to be stationary and ergodic [15], hereafter, the block index t could be omitted for simplicity.

A. Effective Capacity

Considering a queue of infinite buffer size, the probability of the queue length exceeding a threshold x can be derived using the large deviation theory [17], which satisfies

\[ -\lim_{\varepsilon \to 0} \frac{\ln \left( \Pr\{Q(\infty) > x\} \right)}{\varepsilon} = \theta, \]

where \( \Pr\{a \geq b\} \) shows the probability of \( a \geq b \), \( Q(\infty) \) shows the steady-state queue length. Note that in (2), the parameter (\theta > 0) indicates the exponential decay rate of the QoS violation probability. A smaller value of \theta denotes a looser QoS requirement, while larger \theta represents a more stringent delay constraint. Particularly, when \theta \to 0, there is no delay constraint, which means the system can tolerate unlimited delay.

Now, assuming that the Gartner-Ellis Theorem [18, Pages 34-36] is satisfied, EC of a multi-carrier system with N i.i.d. subchannels can be expressed as [10]

\[ E_{C}(\theta) = -\frac{1}{\theta T_{r} B} \ln \left( \mathbb{E} \left[ e^{-\theta B T_{r} R(\theta)} \right] \right) \quad \text{[b/s/Hz]}, \]

where \( \mathbb{E}[\cdot] \) indicates the expectation operator. Substituting (1) into (3), EC can be further expressed as

\[ E_{C}(\theta) = -\frac{1}{\alpha} \log_2 \left( \mathbb{E}_{\gamma} \left[ \gamma_1 \gamma_2 \gamma_3 \ldots \gamma_N \right] \right), \]

where \( \alpha = \frac{\theta T_{r} B}{\ln(2)} \), \( \mathbb{E}_{\gamma}[\cdot] \) indicates the expectation over the PDF of \( \gamma, \mathbb{P}(\theta, \gamma) = \mathbb{P}_{1}(\theta, \gamma) \mathbb{P}_{2}(\theta, \gamma) \ldots \mathbb{P}_{N}(\theta, \gamma) \) denotes a \( N \times 1 \) vector of subcarrier power allocations. Now, the delay-outage probability, which is defined as the probability that the delay exceeds a maximum delay-bound \( D_{\max} \), can be estimated as [10]

\[ P_{\text{out}}(\text{delay}) = \Pr\{\text{Delay} \geq D_{\max}\} \approx \Pr\{Q(t) \geq \emptyset \} e^{-\theta D_{\max}}, \]

where \( D_{\max} \) is in units of a symbol period (\( T_{s} = 1/B \)). For a given \( \mu, \Pr\{Q(t) \geq \emptyset \} \) denotes the probability that the buffer is nonempty at time t and can be approximated as the ratio of the constant arrival rate to the average service rate [17], i.e.,

\[ \Pr\{Q(t) \geq \emptyset \} \approx \frac{\mu}{\mathbb{E}[\gamma(t)]}. \]

Hence, in order to meet a target delay-outage probability limit \( P_{\text{out}}(\text{delay}) \), a source needs to limit its data rate to the maximum of \( \mu, \) where \( \mu = E_{C}(\theta) \).

B. Energy Efficiency

We formulate the link-layer EE of a multi-carrier system as the ratio of EC to the sum of the circuit power, \( P_{C} \), and the
transmission power scaled by the power amplifier efficiency $\epsilon$. Therefore, EE can be mathematically expressed as

$$\EE(\theta) = \frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \frac{\prod_{n=1}^{N} \left( 1 + \frac{NP_n(\theta, \gamma) \gamma_n}{K_\ell} \right)^{-\frac{\gamma}{\epsilon}}}{P_c + \frac{1}{\epsilon} \cdot \mathbb{E}_\gamma \left( \sum_{n=1}^{N} P_n(\theta, \gamma) \right)} \right),$$

where $K_\ell = P_0 K B$ denotes the path loss factor, including both AWGN power and path loss power.

### III. Optimal Power Allocation

In this section, for a multi-carrier link with $N$ i.i.d. subcarriers, we propose an MOP approach to integrate the link-layer EE-EC tradeoff problem, and solve it using $\varepsilon$-constraint formulation and Lagrangian method.

Firstly, in order to jointly maximize the two conflicting objectives, EE and EC, an MOP could be formulated as

$$\max \EE(\theta) \quad \text{and} \quad \max E_c(\theta).$$

In order to solve the MOP, we convert it into an SOP using the $\varepsilon$-constraint approach, which arranges the objective functions in order of their importance [19]. In this paper, EC is maximized subject to a constraint on the required link-layer EE level. Therefore, in a multi-carrier system, the proposed EE-EC tradeoff formulation can be mathematically expressed as

$$E_{\text{EE}}(\theta) = \max_{P_n(\theta, \gamma) \geq 0} \left( \frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left( \prod_{n=1}^{N} \left( 1 + \frac{NP_n(\theta, \gamma) \gamma_n}{K_\ell} \right)^{-\frac{\gamma}{\epsilon}} \right) \right) \right),$$

s.t.

$$\frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left( \prod_{n=1}^{N} \left( 1 + \frac{NP_n(\theta, \gamma) \gamma_n}{K_\ell} \right)^{-\frac{\gamma}{\epsilon}} \right) \right) \geq \eta_{\text{min}}(\theta),$$

where $P_n(\theta, \gamma) = \frac{P_n}{K_\ell}$, $P_c = \frac{P_0}{K_\ell}$. Further, $\eta_{\text{min}}(\theta)$ represents the required EE level and is defined by a certain ratio of the maximum achievable EE at the target delay-outage probability.

Specifically, similar to [14], an adjustable indicator, EE-loss-rate ($\alpha_{\text{EE}}$), is introduced to control the value of $\eta_{\text{min}}(\theta)$ and in turn, control the EE-EC tradeoff level, which yields

$$\eta_{\text{min}}(\theta) = \alpha_{\text{EE}} \cdot \max(\theta),$$

where $\eta_{\text{max}}(\theta)$ represents the maximum achievable EE of the multi-carrier system and $0 \leq \alpha_{\text{EE}} \leq 1$. In particular, when $\alpha_{\text{EE}} = 0$, the EE constraint limit $\eta_{\text{min}}(\theta) = 0$, which indicates that the tradeoff problem is simplified into an EC-maximization problem. In contrast, when $\alpha_{\text{EE}} = 1$, the EE constraint limit $\eta_{\text{min}}(\theta) = \eta_{\text{max}}(\theta)$, which results in an EE-maximization problem.

Setting $\eta'_{\text{min}}(\theta) = \eta_{\text{min}}(\theta) K_\ell$, then, $K_\ell$ in (7b) could be canceled to scale the system performance with respect to the path loss factor. Further, the multi-carrier transmit power is referred to as $P^*_n(\theta, \gamma) = \left[ P_1(\theta, \gamma) \ P_2(\theta, \gamma) \ ... \ P_N(\theta, \gamma) \right]$ and the EE-EC tradeoff formulation can be re-formulated as

$$E_{\text{EE}}^*(\theta) = \max_{P_n(\theta, \gamma) \geq 0} \left( \frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left( \prod_{n=1}^{N} \left( 1 + \frac{NP_n(\theta, \gamma) \gamma_n}{K_\ell} \right)^{-\frac{\gamma}{\epsilon}} \right) \right) \right),$$

s.t.

$$\frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left( \prod_{n=1}^{N} \left( 1 + \frac{NP_n(\theta, \gamma) \gamma_n}{K_\ell} \right)^{-\frac{\gamma}{\epsilon}} \right) \right) \geq \eta'_{\text{min}}(\theta).$$

The objective function (9a) has been proved to be concave in $P^*_n(\theta, \gamma)$ in [16]. Then, EE, as the ratio of a concave function over a non-negative affine function in $P^*_n(\theta, \gamma)$, is quasi-concave in subcarrier power allocations [16]. Therefore, its upper contour set defined by (9b) is convex [20]. Hence (9a)-(9b) is a concave optimization problem and the Karush-Kuhn-Tucker (KKT) conditions are both sufficient and necessary for the global optimum value.

The constraint (9b) can be further transformed to

$$-\frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left( \prod_{n=1}^{N} \left( 1 + \frac{NP_n(\theta, \gamma) \gamma_n}{K_\ell} \right)^{-\frac{\gamma}{\epsilon}} \right) \right) \leq \eta'_{\text{min}}(\theta),$$

Moreover, considering $\lambda \in R$ is the Lagrange multiplier associated to (10), the Lagrangian is

$$\mathcal{L}(P^*_n(\theta, \gamma), \lambda) = -\frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left( \prod_{n=1}^{N} \left( 1 + \frac{NP_n(\theta, \gamma) \gamma_n}{K_\ell} \right)^{-\frac{\gamma}{\epsilon}} \right) \right) + \lambda \left( -\frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left( \prod_{n=1}^{N} \left( 1 + \frac{NP_n(\theta, \gamma) \gamma_n}{K_\ell} \right)^{-\frac{\gamma}{\epsilon}} \right) \right) \right) \geq 0.$$
the KKT condition (12) can be simplified as

\[(1 + N P_n^r \gamma_n)^{-\frac{1}{\gamma_n}} \prod_{i \neq n} \left(1 + N P_i^r \gamma_i \right)^{-\frac{1}{\gamma_i}} = \frac{\beta}{\gamma_n} \quad \forall n \in N_0,\]

(13)

where \(\beta = \frac{\lambda_0^r(\theta)}{e^{(\lambda + 1)/\log_2 e} \mathbb{E}[\gamma]} \left[\prod_{n=1}^{N} \left(1 + N P_n^r \gamma_n \right)^{-\frac{1}{\gamma_n}}\right] \).

By multiplying the right and left-hand sides of the \(N\) equations in (13), the optimal power allocation strategy can be obtained as

\[P_n^r = \frac{1}{N} \left[\frac{1}{\beta^{N+1} \prod_{i \in N_0 \setminus \{n\}} (\frac{\gamma_i}{\gamma_n})^N} - \frac{1}{\gamma_n}\right] \quad n \in N_0. \quad (14)\]

The derived power allocation strategy (14) is optimal only when all subcarriers are assigned with positive powers. If there are one or more subcarriers which are allocated non-positive powers, then the second case needs to be taken into consideration.

2) Case 2: \(P_n^r = 0, \ \exists \ n \in N_0\): If there exists \(P_n^r \leq 0\), then the set of subcarriers, which only positive powers should be assigned, needs to be found.

Firstly, we define \(N_1\) as

\[N_1 = \left\{ n \in N_0 \bigg| \frac{1}{N} \left[\frac{1}{\beta^{N+1} \prod_{i \in N_0 \setminus \{n\}} (\frac{\gamma_i}{\gamma_n})^N} - \frac{1}{\gamma_n}\right] \geq 0 \right\}. \]

According to Lemma 1 in [15], the total power must be assigned to the subcarriers which belong to \(N_1\), while the subcarriers \(n \notin N_1\) should not be allocated any power. Therefore, a new optimization problem could be expressed as

\[E_c^{opt} (\theta) = \max_{\{P_n^r (\theta, \gamma) \geq 0 \}} \left\{ \frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left[ \prod_{n=1}^{N_1} \left(1 + N P_n^r (\theta, \gamma) \gamma_n \right)^{-\frac{1}{\gamma_n}} \right] \right) \right\} \quad \text{s.t.} \]

\[-\frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left[ \prod_{n=1}^{N_1} \left(1 + N P_n^r (\theta, \gamma) \gamma_n \right)^{-\frac{1}{\gamma_n}} \right] \right) \geq \eta_{min}(\theta), \]

\[P_{cr} + \frac{1}{\epsilon} \cdot \mathbb{E}_\gamma \left[ \sum_{n=1}^{N_1} P_n^r (\theta, \gamma) \right] \geq \eta_{min}(\theta). \quad (15a,15b)\]

where \(N_1 = |N_1|\) represents the cardinality of \(N_1\).

Therefore, if \(P_n^r > 0, \ \forall \ n \in N_1\), then the optimization problem can be solved exactly like Case 1. Otherwise, if there are subcarriers \(n \in N_1\) having \(P_n^r = 0\), then \(N_1\) must be further partitioned by recursively repeating the above process until a set \(N^*\) can be found, in which all subcarriers are allocated positive powers [16] (i.e., if \(N_k = N_{k-1} = \{ n \in N_0 | P_n^r > 0 \}\), then \(N^* = N_k\)).

After obtaining \(N^*\), the optimal power allocations are computed as

\[P_n^r = \left\{ \begin{array}{ll}
\frac{1}{N} \left[\frac{1}{\beta^{N+1} \prod_{i \in N^*} (\frac{\gamma_i}{\gamma_n})^N} - \frac{1}{\gamma_n}\right] , & n \in N^*, \\
0 , & \text{otherwise}
\end{array} \right. \quad (16)\]

where \(N^* = |N^*|\).

The optimal value for \(\beta\), referred to as \(\beta^*\), is found when EE constraint is satisfied with equality, yielding

\[-\frac{1}{\alpha} \log_2 \left( \mathbb{E}_\gamma \left[ \prod_{n=1}^{N} \left(1 + N P_n^r (\theta, \gamma) \gamma_n \right)^{-\frac{1}{\gamma_n}} \right] \right) - \frac{1}{\epsilon} \cdot \mathbb{E}_\gamma \left[ \sum_{n=1}^{N} P_n^r (\theta, \gamma) \right] = 0. \quad (17)\]

Note that since EE versus EC is a bell shape curve, the minimum EE limit, if possible, can be achieved at two different EC values, which means that there will be two solutions for \(\beta\) in (17). Considering our intention to maximize EC, \(\beta^*\) is chosen such that it corresponds to the larger EC.

After obtaining \(\beta^*\), the average input power level \(\bar{P}_\text{if}^r\) could be found from

\[\bar{P}_\text{if}^r = K_\ell \cdot \mathbb{E}_\gamma \left[ \sum_{n=1}^{N} P_n^r \right] |_{\beta = \beta^*}. \quad (18)\]

IV. NUMERICAL RESULTS

We numerically evaluate the performance of the multi-carrier EE-EC tradeoff formulation over a Rayleigh frequency-selective fading channel, subject to delay-outage probability and EE constraints. We firstly assume that the \(N\) i.i.d. subcarriers’ power gains, i.e., \(\gamma_1, \gamma_2, \ldots, \gamma_n\), are exponentially distributed with unit mean. In the following simulations, we assume that \(B \cdot T_2 = 200\), the circuit-to-noise power ratio \(P_{cr} \approx -10dB\) and the power amplifier efficiency \(\epsilon = 1\).

We start by plotting EC (on the left-hand-side (LHS) y-Axis, in solid lines) and EE (on the right hand side (RHS) y-Axis, in dash lines) of the considered multi-carrier system versus EE-loss-rate (\(\alpha_{EE}\)), for various numbers of subcarriers, \(N\), in Fig. 1. The figure indicates that with fixed \(N\), when \(\alpha_{EE}\) increases, EE increases and EC decreases. This is due to the fact that larger \(\alpha_{EE}\) indicates more stringent EE constraint, which leads to a larger EE. Since the tradeoff system operates in the conflicting region of EE and EC, the EE-increase results from EC-reductions. Moreover, with fixed \(\alpha_{EE}\), as the number of subcarriers increases, both EC and EE increase. It means that the multi-carrier transmission scheme has significant advantage over single-carrier transmission scheme, where the larger the number of subcarriers, the higher the achievable EC and EE.

We then plot the results for EE and EC of the multi-carrier system versus EE-loss-rate (\(\alpha_{EE}\)), for two different values of delay QoS exponent \(\theta\) and various values of \(N\), in Fig. 2. With fixed \(N\), when the delay QoS exponent \(\theta\) increases, both EE and EC decrease. Especially, when \(N = 1\), the decreases of EE and EC, as a result of the increase in \(\theta\), are significant. However, when \(N\) is larger, e.g., \(N = 8\), the decreases of EE and EC are minor. This indicates that the multi-carrier communication system is more robust against delay requirements, in comparison with single-carrier communication system. To be specific, when the system QoS requirement becomes more stringent, the multi-carrier system would sacrifice less EE and EC to guarantee the required \(\theta\).

Link-layer EE versus the number of subcarriers, \(N\), for various values of \(\theta\) is plotted in Fig. 3, which shows that, for a determined tradeoff level with fixed \(\alpha_{EE}\), when the number of subcarriers is low, EE will be easily influenced by the delay QoS exponent. In other words, this figure also confirms our
above analysis that the system with more subcarriers is more robust with changes of $\theta$. In addition, in Fig. 3, when $N$ is fixed and for $a_{EE} = 0.8$, EE in $\theta = 0.001$ is always larger than $\theta = 0.1$. This indicates that, in comparison with stringent QoS requirement system, EE in loose delay-constrained system could sacrifice more to achieve a larger increase in EC.

Finally, the delay-outage probability, $P_{out}^{delay}$, versus delay QoS exponent $\theta$, for various values of $a_{EE}$ with a maximum tolerable delay threshold $D_{max} = 200$, is plotted in Fig. 4. The figure reveals that for loose delay-constrained systems, e.g., $\theta = 10^{-4}$, the achievable $P_{out}^{delay}$ will stay the same with different $a_{EE}$. When the delay requirement is more stringent, e.g., $\theta = 10^{-2}$, smaller $a_{EE}$ will provide less delay-outage probability. This happens because smaller $a_{EE}$ results in more sacrifices of EE from its maximum values, i.e., $\eta_{max}(\theta)$, and in turn, results in more increases in EC. Therefore, the probability that the buffer length exceeds $D_{max}$ decreases, henceforth, the delay-outage probability decreases.

V. CONCLUSIONS

For a multi-carrier channel with $N$ i.i.d. flat-fading subcarriers, we considered the link-layer EE-EC tradeoff problem as an MOP, and then solved it using $\varepsilon$-constraint approach followed by Lagrangian method. To be specific, the problem was formulated as an EC-maximization problem subject to an EE constraint. By introducing the adjustable performance indicator, EE-loss-rate ($a_{EE}$), into the EE constraint, the constraint limit and in turn, the tradeoff level were flexibly controlled. We then proved that the proposed tradeoff formulation is a concave maximization problem which can be solved using Lagrangian method. Finally, the optimal power allocation strategy was provided, carrying a similar structure with the power allocation technique for EE-maximization problem in a frequency-selective fading channel, but with a different cut-off threshold. In addition, the numerical results showed that for a more stringent delay-limited system, the multi-carrier system would sacrifice less EE and EC to guarantee the required $\theta$, in comparison with single-carrier communication system.
IEEE ICC 2015 - Workshop on Next Generation Green ICT