

# Clustering-Based Device-to-Device Cache Placement <sup>☆</sup>

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## Abstract

In this work we consider the problem of optimal cache placement in a D2D enabled cellular network. There are a number of helper devices in the area, which use their cached contents to help other users and offload traffic from the base station. The goal of cache placement is maximizing the offloaded traffic. We first formulate and optimally solve the cache placement problem as a mixed integer linear program. Then we propose a distributively implementable algorithm that clusters helpers. Helpers in each cluster collectively decide the contents to be cached, based on the content popularity. Numerical evaluations show that the proposed cache placement scheme always performs within 5% of the optimal result and it is robust to popularity profile and cache capacity.

*Keywords:* Caching, Wireless, D2D, Clustering, Integer Programming

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## 1. Introduction

Ongoing developments in the wireless communications technology have led to widespread use of smart devices. Apart from computers and cellular phones, tablets, wearable devices and even vehicles can be connected to the Internet. This variety results in an unprecedented increase in demand for enriched content such as real time applications and video streaming. Excessive increase in demand may cause a considerable decrease in quality of service at the user side.

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<sup>☆</sup>Fully documented templates are available in the elsarticle package on CTAN.

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8 In order to avoid such an outcome, deploying more base stations, increasing  
9 the amount of allocated bandwidth and physical layer improvements in wireless  
10 communication technology can be proposed as solutions. However, for dense  
11 network scenarios, these solutions may be inadequate to alleviate high cellular  
12 load and alternative approaches are required such as Device-to-Device (D2D)  
13 communications.

14 D2D communications is a technology that enables direct communication of  
15 nearby devices, without using the base station as a relay. This technology has  
16 a potential of significantly decreasing delay and increasing throughput. With  
17 these potentials, D2D communications is seen as one of the 10 enabling tech-  
18 nologies of 5G [1]. D2D technology will lead to several proximity based services  
19 (ProSe) such as Local Services, Emergency Communications, IoT enhancement,  
20 terminal relaying, indoor positioning [2]. Another promising application of D2D  
21 communications is content delivery. D2D technology allows content caching at  
22 the network edge such as user terminals and helpers. Caching popular contents  
23 at various nodes in the network is an attractive solution in order to alleviate the  
24 peak load [3]. With this solution nodes can directly supply the future demands  
25 of other users via D2D links without increasing the backhaul traffic. Of course,  
26 one of the challenging points in D2D caching is the limited cache capacity of  
27 mobile devices. An advantage is that D2D transmissions can be performed with  
28 low power within a short proximity. Moreover, as an advantage of short range,  
29 in D2D devices can reuse the cellular bandwidth which improves spectral ef-  
30 ficiency significantly. Taking these into account, fundamental problem is the  
31 cache placement (i.e. which device to cache which content).

32 The works in [4] [5] and [6] are fundamental studies in wireless D2D/femtocell  
33 caching. In [4] the authors prove that a simple randomized device caching pol-  
34 icy (where the devices independently choose the file to cache, according to the  
35 popularity distribution) achieves the optimal scaling of behavior of D2D trans-  
36 mission opportunities in terms of total number of nodes. Note that, this is only  
37 a guarantee in terms of the *scaling of expected* number of D2D content deliveries  
38 with increasing number of users. However, *actual* performance can be very dif-

39 ferent in a given topology. In fact, we see in our simulations that our proposed  
40 clustering-based caching scheme outperforms such a popularity-based scheme.  
41 The authors in [5] proposed a femtocell cache placement algorithm based on  
42 bipartite matching. They prove that the proposed algorithm guarantees a de-  
43 lay performance within a factor 2 of the optimum. Although this is a valuable  
44 theoretical result, a factor of 2 is quite large. Moreover, the proposed algo-  
45 rithm is not distributed. Hence [4] and [5] only consider the throughput scaling  
46 laws and approximation ratios instead of the actual performances. Dissimilarly  
47 to the [5], in [6] authors introduced a coded caching solution, where rateless  
48 coded fragments of the contents are stored at distributed caches. However the  
49 proposed method is centralized. Moreover, throughput-outage trade of in D2D  
50 communications has been investigated in [7]. Authors define a *cluster*, which  
51 denotes the set of neighbors that a device asks for a content. The choice of the  
52 cluster size strikes a tradeoff between throughput and cache hit. As a result, the  
53 works [5], [6] and [7] find some fundamental performance results, however they  
54 do not propose a distributively implementable algorithm. On the other hand,  
55 our proposed algorithm is both amenable to distributed implementation, and it  
56 is tested by varying all parameters for robustness.

57 In the presence of D2D caching, the number of devices is potentially very  
58 large. A centralized cache placement, scheduling and resource allocation by  
59 the base station would increase the control message overhead to prohibitive  
60 levels. Therefore distributed solutions are sought in the literature. In [8] au-  
61 thors evaluated a distributed caching mechanism in order to maximize data  
62 offloading in an interference aware network. Proposed algorithm is based on  
63 the receiver-transmitter matching subject to interference constraint and com-  
64 pared to optimal solution which is derived based on known network information.  
65 Users try to find out the most valuable partner in order to match and become a  
66 transmitter-receiver pair. This scheme is based on the one-to-one matching and  
67 does not allow multiple access. In other words, users cannot request contents  
68 from the other users in their neighborhood unless they are matched. Such a  
69 constraint hampers the content diversity which improves the offloading rate of

70 the network. Benefits of the content diversity are explained in the following sec-  
71 tions. Besides, in [8] a device does not proactively cache a content just to help  
72 others. It only caches a content that it previously requested and obtained for  
73 itself. The authors in [9] devise a random access policy to maximize the cache-  
74 hit. However, they assume that the cache placement as given. In [10] optimal  
75 cache placement problem with different user mobilities, cache sizes and content  
76 popularities are considered. The authors proved that optimization problem is  
77 NP-hard and proposed an infrastructure-aided and distributed data offloading  
78 algorithm. The main assumption here is that the devices are mobile and D2D  
79 transmission can happen when the two devices are in content. In our work we  
80 assume fixed devices, or devices with intermittent mobility. Algorithms and  
81 solutions for a mobile network case is a direction for future research.

82 Game theoretical approaches that give caching decisions in a decentralized  
83 manner also take place in literature. Works in [11],[12], [13] and [14] propose  
84 cache placement algorithms using Stackelberg game model. In [11] and [13] D2D  
85 caching is not considered. In [12] Stackelberg framework provides an incentive  
86 mechanism in order to overcome the unwilling and selfish nature of D2D users  
87 and lead them to cache content and help others. In a previous work [14] we  
88 have implemented the algorithm in [12]. Simulation results have shown that for  
89 a realistic number of devices and contents Stackelberg-based algorithms require  
90 hundreds of iterations for convergence or an acceptable performance. On the  
91 other hand in our algorithm, once the clusters are formed, cache placement is  
92 easily performed.

93 There is also a group of works on reducing latency. In [5] authors focused on  
94 the cache placement problem, aiming at minimization of average download time.  
95 Assuming known content popularities, coded and uncoded caching schemes are  
96 considered. Authors in [15] analyze the average network delay minimization.  
97 In this work, the nearby devices form a cluster and cache contents in a disjoint  
98 manner. That is, the same content is not cached twice in a cluster. Our ap-  
99 proach, as will be explained in the subsequent sections, has some similarities.  
100 However, we assume the existence of a set of designated helper nodes and per-

101 form clustering on the helpers. As opposed to [15], in our case caching popular  
102 contents more than once in a cluster significantly improves the performance. In  
103 [15] users in the same cluster can exchange cached contents via D2D links, inter  
104 cluster cooperation is also possible between users via cellular links. Similar to  
105 these works, optimal caching decision is found centrally in a way that minimizes  
106 latency in [16].

107 A group of works in the literature use stochastic geometry in finding some  
108 fundamental results on cache placement. The work in [17] uses stochastic ge-  
109 ometry and proposes a low-complexity random cache placement and scheduling  
110 algorithm. Authors in [18] prove that spatially correlated caching improves the  
111 hit probability. In these works the main assumption is a Poisson Point Process  
112 (i.e. uniform) user distribution. This technique can be used to mathematically  
113 derive the cache hit probability averaged over all possible topologies. They de-  
114 fine an *exclusion region*, wherein if a user caches a content, then other users in  
115 close proximity do not cache that content. This exclusion region avoids redun-  
116 dant caching and provides content diversity. They [18] optimize the performance  
117 with respect to only the exclusion region. However, this is a very simplistic ap-  
118 proach and there is room for significant improvement. As will be seen in the  
119 following sections, we also utilize spatially correlated caching. However, in real-  
120 ity, only a fraction of cellular users would be eager to participate in caching and  
121 content delivery. We call these users as *helpers* and helpers from clusters. Clus-  
122 tering helpers is crucial since it provides content diversity and avoids duplicate  
123 caching of less popular contents at helpers that serve common users. However,  
124 contrary to [18] close helpers can still cache the same content if that content is  
125 very popular. The reason is that these helpers do not serve exactly the same  
126 set of users. Clustering approach reveals the advantages when proposed algo-  
127 rithm is compared to conventional caching schemes and the optimal solution.  
128 Meanwhile, clustering was also chosen as a method in [19], [20], [21]. However,  
129 in these works there are no helpers and only the users are clustered. Therefore,  
130 these works significantly differ from our work. The contributions of this paper  
131 are summarized as follows,

- 132 • We propose a distributed cache placement algorithm for D2D enabled  
133 cellular networks in order to maximize the network’s average offloading.  
134 Optimization problem is modeled as Mixed Integer Linear Programming  
135 (MILP) and optimal solution is provided.
- 136 • The derived optimal solution is centralized and expected to be handled by  
137 BS, requiring knowledge about network topology. Such kind of solutions  
138 cause computational complexities and signaling overhead. In order to  
139 obviate these drawbacks we concentrated on distributed cache placement  
140 approaches since they provide scalable and practical solutions. For this  
141 purpose, we proposed a clustering-based cache placement algorithm.
- 142 • We have analyzed the performance of the proposed algorithm in the pres-  
143 ence of varying cache size, number of network elements, skewness pa-  
144 rameter of Zipf distribution and number of contents. Results of these  
145 extensive simulations reveal that the proposed algorithm is robust with  
146 reasonable performance compared to conventional caching schemes and  
147 optimal caching.

148 The rest of the paper is organized as follows. Section 2 presents the system  
149 model. Section 3 formulates the optimal caching problem. Section 4 provides  
150 details of the proposed Clustering and Cache Placement Algorithms. Section  
151 5 includes simulations with the varying parameters. Section 6 concludes the  
152 paper and Section 7 mentions the issues that can be considered as future work.

## 153 2. System Model

154 We assume an LTE cell containing a base station that serves  $U + H$  users,  
155 which are composed of  $U$  ordinary users and  $H$  helper users. Helpers are able  
156 to cache contents and serve neighboring users, using device-to-device (D2D)  
157 communications. In D2D communications, two users that are closer than a  
158 range  $R_D$  are able to communicate directly. We assume there are  $C$  cacheable  
159 contents. Each helper can store  $C_c$  contents. We assume a uniform content

160 popularity profile throughout the network. Content popularities are Zipf dis-  
 161 tributed. Without loss of generality the contents are ordered in decreasing order  
 162 of popularity. Let  $p_{uc}$  be the probability that user  $u$  requests content  $c$ . Zipf rule  
 163 suggests that  $p_{uc}$  is proportional to  $\frac{1}{c^\alpha}$  for all users  $u$ . Here,  $\alpha$  is the skewness  
 164 exponent for the Zipf distribution. A higher  $\alpha$  means a more imbalanced pop-  
 165 ularity. We assume that when a content is requested by an ordinary user, this  
 166 request can be heard by a helper. If the content is available at the helper, then  
 167 a D2D transmission starts for content retrieval. If the requested content is not  
 168 available at any helper, then it is obtained from the base station. In this system  
 169 model, we aim to maximize the ratio of contents obtained from the helpers (i.e.  
 170 offloading). A helper can help an ordinary user, only if they are neighbors. Let  
 171 binary parameter  $a_{hu}$  be the neighborhood parameter, which takes value one if  
 172 helper  $h$  and user  $u$  are neighbors, zero otherwise. In the proposed solutions,  
 173 we implicitly assume that the base station is able to measure the popularity of  
 174 contents and regularly inform the helpers about the content popularity profiles.

175 We assume that D2D transmissions do not create interference to the actual  
 176 cellular transmissions. This can be possible by D2D overlay, where D2D trans-  
 177 missions use a separate frequency band. We assume that sufficient bandwidth  
 178 is allocated to D2D transmissions.

179 Another possibility of implementing D2D transmissions is using a different  
 180 technology. For example, WiFi-Direct is an extension of the classical WiFi tech-  
 181 nology for D2D transmissions. This technology enables short range, low power,  
 182 high bandwidth communications, even in the absence of Internet connection.  
 183 WiFi-direct can be implemented on top of the LTE cellular infrastructure, with-  
 184 out any major change in LTE protocols [22]. With this technology, neighboring  
 185 users can form groups and perform direct communication.

### 186 **3. Problem Formulation**

187 We define two sets of binary variables. Let  $x_{hc}$  be the binary variable that  
 188 takes value 1 if content  $c$  is cached by helper  $h$ . Let  $y_{huc}$  be the binary variable

189 that takes value 1 if helper  $h$  is authorized to help ordinary user  $u$  if it requests  
 190 content  $c$ . We define the following optimization problem,

$$\max_{\mathbf{x}, \mathbf{y}} \left\{ \sum_{u=1}^U \sum_{c=1}^C p_{uc} \sum_{h=1}^H y_{huc} \right\} \quad (1)$$

191 s.t.

$$\sum_{c=1}^C x_{hc} \leq C_c, \forall h = 1, \dots, H \quad (2)$$

$$\sum_{h=1}^H y_{huc} \leq 1, \forall u = 1, \dots, U, c = 1, \dots, C \quad (3)$$

$$y_{huc} \leq a_{hu} x_{hc}, \forall u = 1, \dots, U, c = 1, \dots, C, h = 1, \dots, H \quad (4)$$

192 Objective in (1) is the average received help (i.e. offloading) throughout  
 193 the cellular area. Constraint (2) is the cache capacity of each helper node.  
 194 Constraint (3) enforces that each node can only get help from at most one  
 195 node, for each content. Therefore the quantity  $\sum_{h=1}^H y_{huc}$  is a binary quantity.  
 196 It becomes one, if node  $u$  receives the content from any helper and becomes  
 197 zero, otherwise. Finally, constraint (4) enforces that an ordinary node  $u$  can  
 198 receive help from helper  $h$ , in terms of content  $c$ , only if helper  $h$  caches that  
 199 content and is a neighbor of node  $u$ .

200 The proposed problem and its constraints are all linear in terms of the deci-  
 201 sion variables. Moreover, the variables are all binary. Therefore this is a mixed-  
 202 integer linear program (MILP). It can be solved using off-the shelf solvers such  
 203 as CPLEX.

#### 204 4. Proposed Algorithm

205 Maximizing the traffic offloading is directly related to maximizing the hit  
 206 probability. This is the probability of a user finding a requested content from  
 207 a neighboring helper. A very simple cache placement solution would be each  
 208 helper caching the most popular contents. Although this solution will be a  
 209 benchmark in our simulations, it is certainly not the best solution. Consider



210 two helpers located very close to each other. In this case it would be better to  
211 cache different contents at these nodes. Caching this way improves the chance  
212 of an ordinary node to find a requested content at a helper neighbor. There-  
213 fore, we propose a clustering-based cache placement solution. In our solution,  
214 helpers form cliques. Helpers in a clique are in direct communication range with  
215 each other. After clusters are formed, each cluster will independently perform  
216 cache placement in a way that provides content diversity and maximizes hit  
217 probability.

218 The reason of using cliques (clusters) is to facilitate collaboration of helpers  
219 and provide content diversity in a cluster. There are vast number of clustering  
220 methods developed for wireless ad hoc and sensor networks [23]. Our definition  
221 of clique is a set of helpers all having *one hop* distance between each other.  
222 This choice of *single hop* is for the following reasons: 1) Helpers in a clique  
223 can communicate directly with each other and hierarchically allocate contents  
224 to their cache. For example helpers in a clique can send the popularity and  
225 cache capacity information to a designated clusterhead, and the clusterhead  
226 can perform cluster cache allocation. 2) Helpers are very close to each other, so  
227 that they serve mostly common users. A user can easily find a proximate helper  
228 that caches a desired popular content.

229 Algorithm 1 shows the pseudocode of the clustering algorithm. Algorithm  
230 accepts the neighborhood and distance information as inputs. Channel gains  
231 can also be used instead of distances. Algorithm consists of two nested loops. In  
232 each outer loop, a separate clique is formed. Set  $\mathcal{H}$  is initialized as all helpers.  
233 Each time a helper joins a cluster, it is excluded from  $\mathcal{H}$ . Line 4 finds the helper  
234 pair with minimum distance, among the remaining helpers. If these helpers are  
235 neighbors, then a new cluster is initialized (Lines 6,7). Inner loop (Lines 9-18)  
236 tries to add as many helpers to this cluster as possible. Line 10 finds the set of  
237 helpers that can directly communicate (i.e. neighbors) to each existing helpers  
238 in the cluster. If there are no such helpers, then the cluster is finalized (Line  
239 16). If there are such helpers, then the algorithm finds the one with least total  
240 distance to the existing helpers and adds it to the cluster (Lines 12,13). In other

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**Algorithm 1** Clustering Algorithm

---

```
1: Initialize  $\mathcal{H} = \{1, 2, \dots, H\}$ ,  $\text{loop1} = 0$ ,  $\text{loop2} = 0$ ,  $g = 0$ ;  
2: Input: Neighborhood information and distances  $a_{hh'}$ ,  $d_{hh'} \forall h, h' \in \mathcal{H}$ .  
3: while  $\text{loop1} = 0$  do  
4:   Find  $\min_{h, h' \in \mathcal{H}} \{d_{h, h'}\}$   
5:   if  $a_{hh'} = 1$  then  
6:      $g = g + 1$   
7:     New clique:  $\mathcal{G}_g = \{h, h'\}$   
8:     Update:  $\mathcal{H} = \mathcal{H} \setminus \{h, h'\}$   
9:     while  $\text{loop2}=0$  do  
10:      Find set:  $\mathcal{N} = \{i | i \in \mathcal{H}, a_{ih} = 1, \forall h \in \mathcal{G}_g\}$   
11:      if  $\mathcal{N} \neq \emptyset$  then  
12:        Find  $i^* = \min_{i \in \mathcal{N}} \{\sum_{h \in \mathcal{G}_g} d_{ih}\}$   
13:        Add  $\mathcal{G}_g = \mathcal{G}_g \cup \{i^*\}$   
14:        Update:  $\mathcal{H} = \mathcal{H} \setminus \{i^*\}$   
15:      else  
16:         $\text{loop2}=1$ ;  
17:      end if  
18:    end while  
19:  else  
20:     $\text{loop1}=0$   
21:  end if  
22: end while  
23: Return: All cliques  $\mathcal{G}_1, \mathcal{G}_2, \dots, \mathcal{G}_g$ .
```

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241 words, this algorithm attempts to find maximal cliques. Algorithm returns the  
242 set of helpers in each cluster. The remaining helpers cannot form any cliques,  
243 since they are isolated.

244 Our clustering algorithm addresses the “maximal clique” problem in the lit-  
245 erature, where we form cliques that can not be enlarged. Forming maximal  
246 cliques facilitates allocating as many different contents as possible to a helper  
247 cluster, which facilitates content diversity. This provides great benefits espe-  
248 cially in the case of low Zipf skewness  $\alpha$ . This way, less popular contents can  
249 also be cached in a cluster. Our simulations verify the success of this approach,  
250 wherein the proposed algorithm performs almost as good as the MILP-based  
251 optimal solution. The maximal clique problem is NP-complete [24], [25]. How-  
252 ever we need a easy-to-implement clustering algorithm that forms clusters as  
253 large as possible, in order to provide content diversity in cache placement.

254 We did not include a fully-described distributed clustering protocol in this  
255 paper. However such a clustering algorithm can be approximately implemented  
256 in a distributed manner. For example, the authors in [26] also used the idea  
257 of maximal cliques and proposed a distributed clustering algorithm. The nodes  
258 first collect the connectivity information with their neighbors. Each node waits  
259 a random amount of time before starting a cluster advertisement. This time  
260 duration is inversely proportional to the number of neighbors. Hence the node  
261 with highes number of neighbors advertises first as a cluster head. A node  
262 receiving an advertisement joins in a cluster if it satisfies the single-hop condition  
263 with every existing node in the cluster. The helper that has the most number  
264 of ordinary user neighbors becomes the clusterhead.

265 Algorithm 2 presents the pseudocode of the cache placement algorithm. Al-  
266 gorithm consists of a for loop (Lines 3-21), where cache placement of cluster  
267 occurs in each turn. Let  $N_h$  be the number of helpers in cluster  $g$  (Line 4).  
268 The total cache capacity in this cluster is denoted by `total`. The for loop in  
269 Lines 6-11 determines of how many copies of each content will be cached in the  
270 cluster. Line 7 finds an integer number for each content. The sum of these  
271 numbers barely exceeds the total cache capacity. Line 12 sorts helpers in the

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**Algorithm 2** Cache Placement Algorithm

---

```
1: Initialize  $x_{hc} = 0, \forall h = 1, \dots, H, c = 1, \dots, C$ 
2: Input: All cliques  $\mathcal{G}_1, \mathcal{G}_2, \dots, \mathcal{G}_g$ , Content popularity:  $p_{uc}$ , Number of contents  $C$ , Cache capacity  $C_c$ 
3: for all clusters  $g$  do
4:   Number of helpers in the cluster  $N_h = |\mathcal{G}_g|$ 
5:   total =  $N_h \times C_c$ 
6:   for  $i=1:C$  do
7:      $t_c = \min\left(N_h, \text{round}\left(\frac{p_{uc}}{p_{ui}}\right)\right), \forall c$ 
8:     if then  $\sum_{c=1}^C t_c \geq \text{total}$ 
9:       Exit loop
10:    end if
11:  end for
12:  Sort helpers in cluster  $g$  as  $(1), (2), \dots, (N_h)$ , according to number of neighboring ordinary users
13:  for  $(h) = (1) : (N_h)$  do
14:    for  $c$  do  $=1:C$ 
15:      if  $t_c > 0$  then
16:        Set  $x_{(h),c} = 1$ 
17:         $t_c = t_c - 1$ 
18:      end if
19:    end for
20:  end for
21: end for
22: for all helpers  $h \notin \bigcup_{i=1}^g \mathcal{G}_i$  do
23:   Set  $x_{hc} = 1$  for  $c = 1, 2, \dots, C_c$ 
24: end for
25: Return:  $x_{hc}, \forall h = 1, \dots, H, c = 1, \dots, C$ 
```

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272 cluster, where the helpers with more ordinary neighbors gain priority. The loop  
 273 in Lines 13-20 scans the helpers according to their priority. This loop fills the  
 274 caches of the helpers starting from the most popular content. Finally the loop  
 275 in line 22-24 fills the helpers that are not included in any cluster (i.e. isolated  
 276 helpers). Each of these isolated helpers cache the most popular contents. The  
 277 content popularity information can be obtained from a centralized server, or it  
 278 can be estimated by the base station and informed to the helpers.

279 The following examples shows the main loop of the algorithm (Lines 3-21)  
 280 in action:

281 Suppose that there are  $C = 10$  contents with popularities (skewness  $\alpha = 1$ )  
 282  $\mathbf{p}_{\mathbf{uc}} = [0.341, 0.171, 0.114, 0.085, 0.068, 0.057, 0.049, 0.043, 0.038, 0.034]$ . Let us  
 283 consider a cluster of 3 users,  $\{1, 2, 3\}$  where each user can cache  $C_c = 2$  contents.  
 284 So total cache capacity of this cluster is  $3 \times 2 = 6$  contents and  $t_c$  stands for the  
 285 temporary cached contents by the corresponding cluster.

- 286 • We first divide  $\mathbf{p}_{\mathbf{uc}}$  by 0.341 and round. The results becomes  $t_c =$   
 287  $[1100000000]$ . The sum is smaller than 6.
- 288 • We then divide  $\mathbf{p}_{\mathbf{uc}}$  by 0.171 and round. The results becomes  $t_c =$   
 289  $[2111000000]$ . The sum is smaller than 6.
- 290 • We then divide  $\mathbf{p}_{\mathbf{uc}}$  by 0.114 and round. The results becomes  $t_c =$   
 291  $[3211110000]$ . The sum is greater than 6. We exit the loop in Lines  
 292 6-11.
- 293 • Assume that, after performing the operation in Line 12, the order does  
 294 not change.
- 295 • Node 1 caches contents 1,2. Update  $t_c$  as  $t_c = [2111110000]$ .
- 296 • Node 2 caches contents 1,2. Update  $t_c$  as  $t_c = [1011110000]$ .
- 297 • Node 3 caches contents 1,3. Update  $t_c$  as  $t_c = [0001110000]$ .
- 298 • All the capacity in the cluster is filled. The algorithm passes to the next  
 299 cluster.

Table 1: Simulation Parameters

Simulation Parameters	Value
Number of contents ( $C$ )	[30, 40]
Number of ordinary users ( $U$ )	[300,1000]
Number of helper users ( $H$ )	[40, 45, 50, 55, 60]
Zipf Skewness Parameter ( $\alpha$ )	[0.6, 1, 1.5]
D2D Maximum Range ( $R_D$ )	50 meters
Cache capacity ( $C_c$ )	[2, 4, 6, 8] contents
Radius of cellular area ( $R_{max}$ )	250 meters
Content Size ( $S_c$ )	1 unit

300 As seen in this example, content 1, which is very popular, is cached at each  
 301 helper in the cluster. Content 2 is cached in two helpers and content 3 is cached  
 302 in only one helper. Other contents are not cached. This method both maximizes  
 303 hit probability and provides content diversity.

## 304 5. Simulation Results

305 In this section we will compare the performances of the proposed algorithm  
 306 with that of the optimal solution, along with some benchmarks. Table 1 shows  
 307 the simulation parameters. We will compare the following methods,

- 308 • MILP-based optimal solution.
- 309 • Proposed clustering-based algorithm.
- 310 • Popularity based caching: This is a simple scheme, where each helper  
 311 independently caches the most popular contents.
- 312 • One Copy: This is a hybrid scheme, where helpers are clustered using the  
 313 proposed clustering method. However any content is cached by at most  
 314 one helper in a cluster.

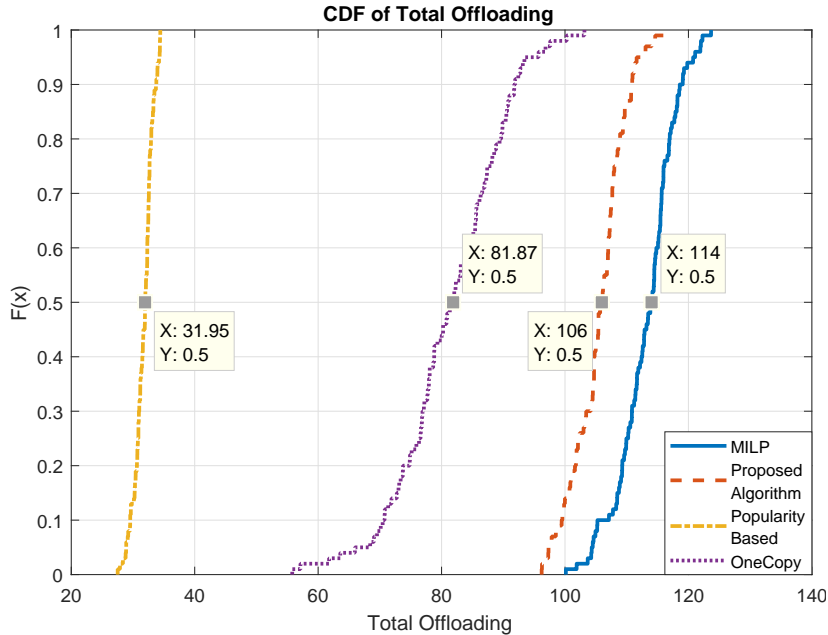


Figure 1: Cumulative Distribution Function for Total Offloading ( $U=300$ ,  $C=30$ ,  $C_c=4$ ,  $\alpha=0.6$ )

315 Figure 1 shows the empirical cumulative distribution function (CDF) of the  
 316 total offloading for 300 ordinary users, 50 helpers, 30 contents where  $\alpha = 0.6$ .  
 317 Median offloading results show that our proposed method provides an offload  
 318 within 7% of the optimal. This is a very promising result. Moreover, the offload-  
 319 ing provided by the popularity based caching method is only one third of the  
 320 optimal. This shows the importance of clustering. One Copy algorithm is some-  
 321 where in between, but it can still provide only 70% of the optimal offloading.  
 322 This shows the success of our proposed cache placement algorithm in providing  
 323 high hit probability.

324 Figure 2 shows the performance for higher skewness of content popularities  
 325 where  $\alpha = 1.5$ . This points to a more imbalanced popularity profile. In this  
 326 case a small fraction of contents occupy a large fraction of total popularity. Our  
 327 algorithm performs even better in this case, within 5% of the optimal perfor-  
 328 mance. Popularity based caching can only provide half of the optimal offloading.

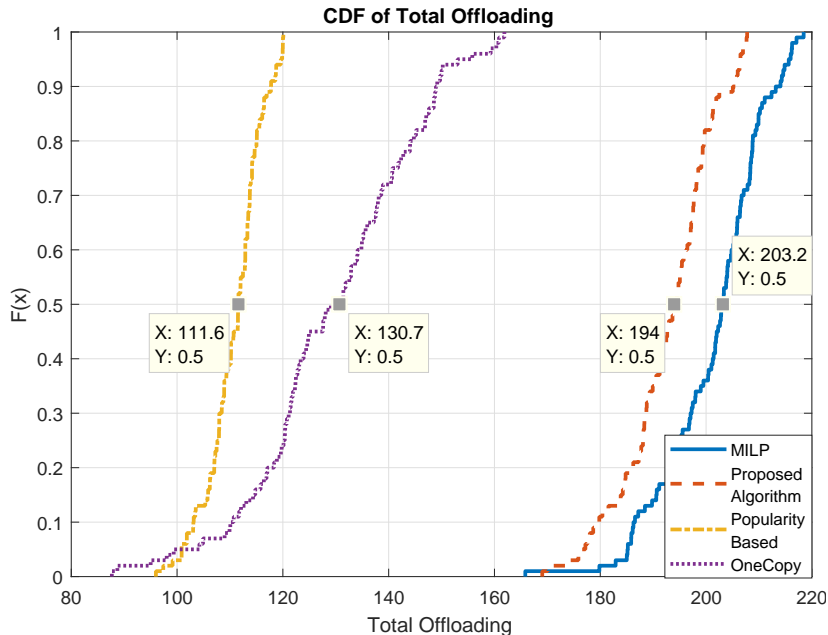


Figure 2: Cumulative Distribution Function for Total Offloading ( $U=300$ ,  $C=30$ ,  $C_c=4$ ,  $\alpha=1.5$ )

329 Relative performance of One Copy method is worse (64% of the optimal median  
 330 offloading). This is because One Copy method caches unnecessary contents,  
 331 that have low popularity.

332 Figures 3 and 4 show the empirical CDF of the offloading for the case of  
 333 higher ( $U = 1000$ ) ordinary users. As expected, this results in increased total  
 334 offloading for all compared methods. Our proposed algorithm approaches even  
 335 closer to the optimum, with a median offloading performance within 4% and  
 336 2.5% of the optimal for  $\alpha = 0.6$  and 1.5.

337 In order to form Table 2, we ran the simulations for our proposed algo-  
 338 rithm and optimal MILP solution for 100 uniformly distributed random topol-  
 339 ogy which includes helpers and ordinary users. Then divided the total offloading  
 340 of the proposed algorithm to that of the optimal. Table shows the value of this  
 341 obtained quantity for different cache capacities and number of helpers. Here  
 342  $max$ , denotes the 95th percentile of the considered topologies, while  $min$  de-



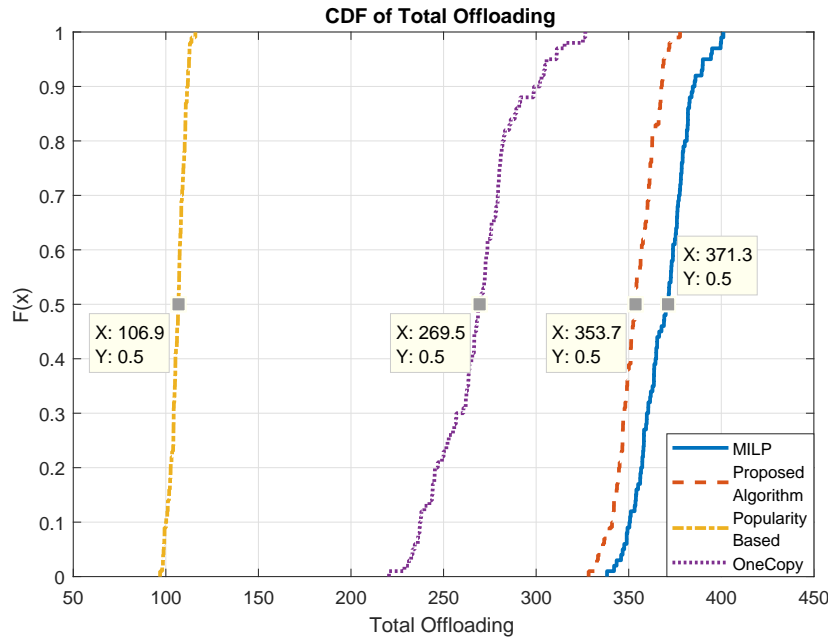


Figure 3: Cumulative Distribution Function for Total Offloading ( $U=1000$ ,  $C=30$ ,  $C_c=4$ ,  $\alpha=0.6$ )

343 notes the 5th percentile. The results in the Table indicate that for all cache  
 344 sizes and number of helpers, the proposed algorithm almost always perform  
 345 within 10% of the optimal. Our algorithm especially approaches the optimal for  
 346 lower number of helpers and a larger cache capacity.

## 347 6. Conclusions

348 In this work we consider the problem of optimal cache placement using D2D  
 349 communications in a cellular system. We propose a cache placement scheme,  
 350 where the helper nodes are first clustered and then the caches in a cluster are  
 351 collectively utilized in order to provide higher hit probability and content diver-  
 352 sity. The results clearly show that our algorithm is very successful and provides  
 353 close-to-optimal offloading uniformly for all values of simulation parameters.  
 354 The proposed algorithm has two main advantages. First of all it is robust,  
 355 meaning that it performs close to optimal for various values of number of users,

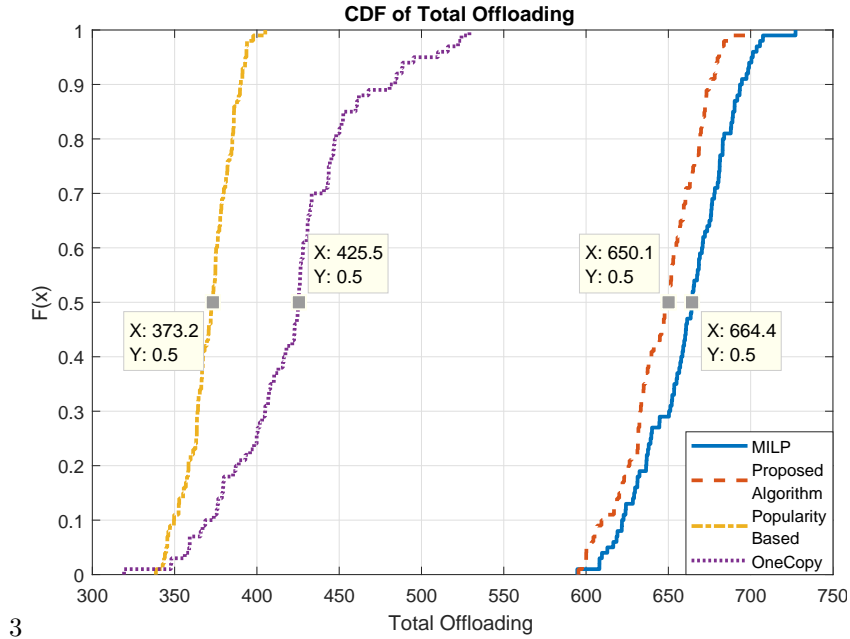


Figure 4: Cumulative Distribution Function for Total Offloading ( $U=1000$ ,  $C=30$ ,  $C_c=4$ ,  $\alpha=1.5$ )

356 helper, Zipf skewness parameter and cache sizes. Secondly it is amenable to dis-  
 357 tributed implementation. There are various distributed clustering algorithms in  
 358 the literature, which can be applied in order to form helper cliques.

### 359 7. Extensions and Future Work

360 There are number of issues that can be considered as future work,

#### 361 7.1. Jointly Optimal Cache Placement and Resource Allocation for Helpers

362 In this work we assumed that D2D transmissions do not cause interference  
 363 to cellular transmissions. This can be possible either by using an orthogonal  
 364 frequency resources (overlay) or using a different technology (e.g. WiFi). In  
 365 future we plan to consider a D2D underlay, where D2D transmissions interfere  
 366 with the cellular transmissions [14].

Table 2: Proposed Algorithm vs. MILP for  $U=1000, C=40, \alpha=1$

		Number of Helpers $H$				
		40	45	50	55	60
Cache Size $C_c$	2	max: 99.39%	max: 98.13%	max: 96.39%	max: 97.62%	max: 95.82%
		min: 90.55%	min: 89.32%	min: 89.26%	min: 88.78%	min: 87.43%
	4	max: 99.77%	max: 99.66%	max: 99.19%	max: 98.77%	max: 98.42%
		min: 93.68%	min: 93.17%	min: 92.98%	min: 92.36%	min: 91.63%
	6	max: 99.66%	max: 99.58%	max: 99.60%	max: 99.41%	max: 98.92%
		min: 94.77%	min: 94.01%	min: 94.32%	min: 93.32%	min: 92.65%
	8	max: 99.60%	max: 99.57%	max: 99.39%	max: 96.65%	max: 99.09%
		min: 95.24%	min: 94.81%	min: 94.73%	min: 93.99%	min: 93.16%

367 *7.2. Estimating the Content Popularities*

368 In this work we assume that the base station perfectly knows the content  
369 popularities and feeds it back to the helpers. However, our proposed algorithm  
370 is also able to work in case of estimated probabilities. Moreover, content pop-  
371 ularity can also be measured by the helpers. Helpers in a cluster can collect  
372 content requests and share their statistics with their cluster head. Cluster head  
373 then perform content placement and tell the other cluster members about which  
374 content to cache.

375 Online stochastic learning can also be used in order to implement and online  
376 and adaptive caching mechanism. This method has been recently used as a  
377 channel and power allocation mechanism in D2D transmissions [27]. Online  
378 stochastic learning can be implemented as follows: The helper first randomly  
379 caches a content, then measures the request rate and resulting offloading. The  
380 probability of caching of a content increases in the next stage depending on its  
381 request rate. After some iterations, caching probability of a content approaches  
382 1, which ends the iterations. Although such algorithms require a high number  
383 of iterations to converge, they can be preferred for a distributed mechanism,  
384 which requires no intervention from the base station.

385 In real applications content popularity can also be geographically varying.  
386 In such a case, estimating the popularity centrally by the base station will be

387 suboptimal. In this case estimation of popularity separately at each cluster is  
388 a good choice. Since the helpers in a cluster are geographically close, content  
389 popularity in their region should be similar. Our proposed algorithm is also  
390 applicable in case of geographically varying content popularity.

### 391 *7.3. Distributed Clustering*

392 With its current form our proposed clustering algorithm for helpers is a  
393 centralized algorithm. However it can be modified as a distributed algorithm.  
394 In [22] an architecture is proposed that uses WiFi-Direct jointly with LTE for  
395 D2D communications. In their architecture, cellular users build a WiFi-Direct  
396 cluster and the clusterhead serves as a bridge between LTE and WiFi Direct  
397 networks [28]. In [28] an architecture is proposed, where a device can be in  
398 more than one group as a client or group owner. This way a helper clique can  
399 create a separate group for content placement. Each helper can also create their  
400 own group with neighboring ordinary users. Besides, an ordinary user can be in  
401 all groups of neighboring helpers. When a user requests a content, the closest  
402 helper that has the content serves the user. Since WiFi-direct uses a separate  
403 and unlicensed frequency band, this would result in significant reduction in LTE  
404 bandwidth demand.

### 405 *7.4. Time Varying User Location and Content Popularity Profiles*

406 In this work we consider a single-shot scenario, where clustering and cache  
407 placement is performed for a given set of user locations and content popularity  
408 profile. In reality, location of mobile users and helpers would change frequently,  
409 which requires cluster maintenance and cache content replacement. Developing  
410 cache placement methods for mobile users and time varying content profiles is  
411 a subject of future work.

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