Pre-compensation for a Hybrid Fuzzy PID Control of a Proportional Hydraulic System

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1. Introduction

Fluid power is a term which was created to include the generation, control, and application of smooth, effective power of pumped or compressed fluids when this power is used to provide force and motion to mechanisms. Fluid power includes hydraulic, which involves liquids, and pneumatic, which involves gases. Hydraulic and pneumatic power offer many advantages over electric motors, especially for systems that require high speed linear travel, moving or holding heavy loads, or very smooth position or pressure control. Compared to other types, hydraulic and pneumatic actuators are smaller and quieter. They also produce less heat and electromagnetic interference (EMI) at the machine than do electric actuators, and in many cases, in particular with high performance hydraulic or pneumatic system, they offer the ability to build machines at considerable savings compared to machines employing purely electrical or mechanical motion (Chuang & Shiu, 2004; Knohl & Unbehauen, 2000).

Hydraulic drives, thanks to their high power intensity, are low in weight and require a minimum of mounting space. They facilitate fast and accurate control of very high energies and forces. The hydraulic actuator (cylinder) represents a cost-effective and simply constructed linear drive. The combination of these advantages opens up a wide range of applications. The increase in automation makes it ever more necessary for pressure, flow rate, and flow direction in hydraulic systems to be controlled by means of an electrical control system. The obvious choice for this is hydraulic proportional valves (or servo valves) as an interface between controller and hydraulic system (Knohl & Unbehauen, 2000).

The hydraulic actuator, usually a cylinder, provides the motion of the load attached to the hydraulic system. A control valve meters the fluid into the actuator as a spool traverses within the valve body. The control valve is either a servo valve or a proportional valve. In hydraulic control applications, proportional valves offer various advantages over servo valves (Eryilmaz & Wilson, 2006). Proportional valves are much less expensive. They are more suitable for industrial environments because they are less prone to malfunction due to fluid contamination. In addition, since proportional valves do not contain sensitive, precision components, they are easier to handle and service. However, these advantages are offset by their nonlinear response characteristics. Since proportional valves have less precise manufacturing tolerances, they suffer from performance degradation. The larger tolerances
on spool geometry result in response nonlinearities, especially in the vicinity of neutral spool position. Proportional valves lack the smooth flow properties of “critical centre” valves, a condition closely approximated by servo valves at the expense of high machining cost. Small changes in spool geometry (in terms of lapping) may have large effects on the hydraulic system dynamics. Especially, a closed-centre spool (overlapped) of proportional valve, which usually provides the motion of the actuator in a proportional hydraulic system (PHS), may result in the steady state error because of its dead zone characteristics in flow gain [Eryilmaz & Wilson, 2006]. Figure 1 illustrates the characteristics of proportional valve.

![Fig. 1. Characteristics of a closed-centre spool (overlapped) of proportional valve.](image)

Valve lap, or valve overlap, refers to the amount of spool travel from the center position required to start opening between the powered input port and the work (output) port or the tank port. A zero lapped valve is one in which any tiny, differentially small amount of spool shift, either way, starts the opening. However, there is no contact between the OD of the spool and ID of the bore. And even zero lapped valves have some slight amount of overlap. Nonetheless, the zero lapped term persists.

The characteristics of the proportional valve with dead zone $D$ (from figure 1) is described by the function

$$Q = D[u] = \begin{cases} 
  m(u - d), & \text{if } u \geq d \\
  0, & \text{if } -d \leq u \leq d \\
  m(u + d), & \text{if } u < -d 
\end{cases} \quad (1)$$

where $d, m \geq 0$. The parameter $2d$ specifies the width of the deadzone, while $m$ represents the slope of the response outside the dead zone.

The proportional hydraulic system shown in figure 2 is comprised of a double acting cylinder, a 4/3 way proportional valve, and load. The supply pressure $P$ is assumed to be constant, and the control objective is the positioning of the pay load. The proportional valve used in this plant is a low cost, which can be characterized by a relative large and symmetric dead zone. A complete mathematic model of such an electro-hydraulic system, for example, has been given by (Knoll & Unbehauen, 2000). However, these equations are highly complex and difficult to utilize in control design. A more practical model may be obtained through the linearization of the non-linear function.
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A mathematical model of the plant can be derived from the flow equation of valve, the continuity equation and balance of forces at the piston. The valve flow rate equation is highly non-linear and dependent on the valve displacement from neutral, which is proportional to input voltage \( u \) and the pressure drop across the load \( P_L \). A Taylor series linearization leads to

\[
Q_L = K_q u - K_c P_L
\]  

where, \( K_q \) = flow gain coefficient and \( K_c \) = flow pressure coefficient.

The movement of the piston, the change of the oil volume due to compressibility and the leakage oil flow determine the total oil flow \( Q_L \) as

\[
Q_L = A_p \dot{y} + \frac{V_t}{4\beta_e} \dot{P}_L + f(P_L)
\]  

where, \( V_t \) is the total compressed oil volume, \( A_p \) the surface area of the piston, \( \dot{y} \) the velocity of the piston, \( \beta_e \) the effective bulk modulus (compressibility) and \( f(P_L) \) the non-linear influence of the internal and external oil leakage. Here, it is assumed that the rod and the head side areas of the piston are equal. If the leakage function is approximated by a linear relation, equation (3) can be rewritten as

\[
\dot{P}_L = \frac{4\beta_e}{V_t} (Q_L - C_{tp} P_L - A_p \dot{y})
\]

where \( C_{tp} \) is the total leakage coefficient of the piston. The balance of forces at the sliding carriage leads to

\[
F_G = A_p P_L = M_t \ddot{y} + B_p \dot{y} + y
\]

where \( F_G \) is the force generated by the piston, \( M_t \) the total mass of the piston and the load, and \( B_p \) the damping coefficient of the piston and the load. Neglect the non-linear effects of dry and adhesive friction, combining equations (2), (4), and (5) and applying the Laplace transformation to the resulting third order differential equation results in the transfer function.
where the abbreviations

\[ b_0 = \frac{4\beta \varepsilon}{V_t} K_q \]  

\[ a_0 = \frac{4\beta \varepsilon}{V_t} \left( \frac{B_p}{A_p} (K_C + C_{ip}) + A_p \right) \]  

\[ a_1 = \frac{B_p}{A_p} + 4\beta \varepsilon \frac{M_t}{V_t A_p} (K_C + C_{ip}) \]  

\[ a_2 = \frac{M_t}{A_p} \]  

The parameters of the linear model of the hydraulic system given by equation (7), which depend on the constants derived by linearization, are all of varying nature. Variation of the load mass and the damping coefficient can also be interpreted as parameter changes of the linear model. To take the dead zone of the actuating valve into account, a static non linear dead zone that is portrayed in figure 1.

2. Preliminary of Controller Designs

A closed loop system, whether the reference signal is set manually or automatically, can perform control of cylinder position, speed and force. Figure 3 represents typical of an “Automatic Closed Loop” control system. As shown in the figure, the position of a hydraulic cylinder is controlled by a proportional valve. The proportional valve solenoid is receiving driving electrical current from an amplifier card, which is generating the driving current based on a control signal supplied by a controller. The controller responsibility is to continuously compare the reference signal and the actual cylinder position fed back by the position sensor, after consequently generate the adequate control signal.

![Diagram of a closed loop control system](image)

Fig. 3. Conceptual controls of the PHS.
2.1 PID controller
Classical PID controllers are very popular in industries because they can improve both the transient response and steady state error of the system at the same time (Kim et al., 1994). Although great efforts have been devoted to develop PID controller, PID controllers are not robust to the parameter variation to the plants being controlled. Figure 4 shows the use of PID controller controls the PHS.

\[
\begin{align*}
K_p, K_i, K_D \\
\end{align*}
\]

Fig. 4. Block diagram of a PID controller.

The PID control method has been widely used in industry during last several decades because of its simplicity. The implementation of PID control logic, as shown in equation (8), requires finding suitable values for the gain parameters \(K_p\), \(K_i\), and \(K_D\). To tune these parameters, the model is linearized around different equilibrium points,

\[
u(k) = K_p e(k) + K_i \sum_{i=0}^{k} e(i) + K_D [e(k) - e(k-1)]
\]

where \(e(k)\) is the error signal. However, the PID method is not suitable for controlling a system with a large amount of lag, parameter variations, and uncertainty in the model. Thus, PID control logic cannot accurately control position in a hydraulic system.

2.2 Fuzzy logic controller
Fuzzy logic control (FLC) has found many applications in a variety of fields since Prof. Zadeh introduced fuzzy set theory in 1965 (Zadah, 1965). Among the most successful applications of this theory has been the area of FLC initiated by the work of (Mamdani & Assilian, 1975). FLC has the advantage that it does not require an accurate mathematical model of the process. It uses a set of artificial rules in a decision-making table and calculates an output based on the table. Figure 5 shows specific components characteristic of a FLC. Input variables go through the fuzzification interface and are converted to linguistic variables. Then, a database and rule base holding the decision-making logic are used to infer the fuzzy output. Finally, a defuzzification method converts the fuzzy output into a signal to be sent out.

Fuzzy control is robust to the system with variation of system dynamics and the system of model free or the system which precise information is not required. It has been successfully used in the complex ill-defined process with better performance than that of a PID controller. Another important advance of fuzzy controller is a short rise time and small overshoot (Li et al., 2006; Rahbari & Silva, 2000).
FLC has the advantage that it does not require an accurate mathematical model of the process. It uses a set of artificial rules in a decision-making table and calculates an output based on the table (Li et al., 2006; Rahbari & Silva, 2000).

Figure 6 shows a fuzzy control of the PHS. Input variables go through the fuzzification interface and are converted to linguistic variables. Then, a database and rule base holding the decision-making logic are used to infer the fuzzy output. Finally, a defuzzification method converts the fuzzy output into a signal to be sent out.

When used in a control system, FLC is robust since it provides a fast rise time and a small amount of overshoot. The control parameters and set of terms that describe each linguistic variable must be determined when designing a FLC. Obviously, the position in the electro-hydraulic is the parameter to be controlled in the system. A two-dimension structure will be used to produce fast calculations. The two input linguistic variables are the error of the position (e) and the error change of the position (Δe). The output is the voltage signal to control the amplifier and proportional valve. Thus, the FLC has two antecedences and one consequence.

The controller structure of a FLC, which the fuzzy states of the inputs and the output, all are chosen to be equal in number and use the same linguistic descriptors: NB = negative big, N = negative, Z = zero, P = positive, and PB = positive big. The fuzzy sets and its memberships function is shown in figure 7. A set of fuzzy rules is shown in Table 1.

Since the dynamics of each cylinder is not symmetric, due to the difference in the effective area of the rod side and the head side of the piston. The designed fuzzy set of the fuzzy controller accounts for this asymmetry as well (Rahbari & Silva, 2000; Pratumsuwan & Thongchai, 2009).
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Fig. 5. Structure of FLC.

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![Fuzzy sets of a FLC.](image)

![Input-output mapping of a FLC.](image)

Table 1. Fuzzy Rules of a FLC.

<table>
<thead>
<tr>
<th>Δe</th>
<th>NB</th>
<th>N</th>
<th>Z</th>
<th>P</th>
<th>PB</th>
</tr>
</thead>
<tbody>
<tr>
<td>e NB</td>
<td>NB</td>
<td>NB</td>
<td>N</td>
<td>N</td>
<td>Z</td>
</tr>
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<tr>
<td>PB Z</td>
<td>P</td>
<td>P</td>
<td>PB</td>
<td>PB</td>
<td>PB</td>
</tr>
</tbody>
</table>

2.3 Hybrid of fuzzy and PID controller

While conventional PID controllers are sensitive to variations in the system parameters, fuzzy controllers do not need precise information about the system variables in order to be effective. However, PID controllers are better able to control and minimize the steady state error of the system. Hence, a hybrid system, as shown in figure 9, was developed to utilize the advantages of both PID controller and fuzzy controller (Parnichkul & Ngagecharoenkul, 2000; Erenoglu et al., 2006; Pratumsuwan et al., 2009).
Figure 9 shows a switch between the fuzzy controller and the PID controller, where the position of the switch depends on the error between the actual value and set point value. If the error in position reaches a value higher than that of the threshold $e_0$, the hybrid system applies the fuzzy controller, which has a fast rise time and a small amount of overshoot, to the system in order to correct the position with respect to the set point. When the position is below the threshold $e_0$ or close to the set point, the hybrid system shifts control to the PID, which has better accuracy near the set position (Parnichkul & Ngaecharoenkul, 2000; Erenoglu et al., 2006; Pratumsuwan et al., 2009).

2.4 Fuzzy pre-compensated PID controller
Since classical PID controllers are widely used in industrial applications, they exhibit poor performance when applied to the PHS containing unknown nonlinearities, such as dead zones, saturation, and hysteresis. In this section, we will describe a fuzzy logic-based pre-compensation design for PID controllers (Kim et al., 1994).

Figure 10 illustrates the basic control structure. The scheme consists of a classical PID control structure together with fuzzy pre-compensator. The fuzzy pre-compensator uses the command input $y_m$ and the PHS output $y_p$ to generate a pre-compensated command signal $y'_m$, described by the following equations (Kim et al., 1994).
In the above, \( e(k) \) is the position error between the command input \( y_m(k) \) and the PHS output \( y_p(k) \) and \( \Delta e(k) \) is the change in position error. The term \( F[e(k), \Delta e(k)] \) is a nonlinear mapping of \( e(k) \) and \( \Delta e(k) \) based on fuzzy logic. The term \( \mu(k) = [e(k), \Delta e(k)] \) represents a compensation or correction term, so that the compensated command signal \( y'_m(k) \) is simply the sum of the external command signal \( y_m(k) \) and \( \mu(k) \). The correction term is based on the error \( e(k) \) and the change of error \( \Delta e(k) \). The compensated command signal \( y'_m(k) \) is applied to a classical PID scheme, as shown in figure 10.

The equations governing the PID controller are as follows

\[
e'(k) = y'_m(k) - y_p(k)
\]

\[
\Delta e'(k) = e'(k) - e'(k-1)
\]

\[
u(k) = u(k-1) + K_P \Delta e'(k) + K_I e'(k) + K_D (\Delta e'(k) - \Delta e'(k-1))
\]

The quantity \( e'(k) \) is the pre-compensated position error between the pre-compensated command input \( y'_m(k) \) and PHS output \( y_p(k) \), and \( \Delta e'(k) \) is the change in the pre-compensated position error. The control \( u(k) \) is applied to the input of the PHS. The purpose of the fuzzy pre-compensator is to modify the command signal to compensate for the overshoots and undershoots present in the output response when the PHS has unknown nonlinearities.

For PID tuning in this paper, we set PID gains with Ziegler-Nichols and trial-error method. The purpose of the fuzzy pre-compensator is to modify the command signal to compensate for the overshoots and undershoots present in the output response when the PHS has unknown nonlinearities. An expert's experience and knowledge method is used to build a rule base and membership functions (Rahbari & Silva, 2000).

In our description, we think of \( e(k) \) and \( \Delta e(k) \) as inputs, and \( \mu(k) \) as the output. The fuzzy states of the inputs and the output, all are chosen to be equal in number and use the same linguistic descriptors: NB = negative big, NM = negative medium, NS = negative small, ZO = zero, PS = positive small, PM = positive medium, and PB = positive big. (The fuzzy sets is shown in figure 11.) The decision-making output can be obtained using a max-min fuzzy inference where the crisp output is calculated by the center of gravity (COG) method. Using these fuzzy sets, the fuzzy rules can be designed. The designed rules are presented in table 2. To explain how these rules were obtained, consider for example the rules in table 2. Suppose that the command signal is a constant \( y_m \), the error \( e(k) \) is zero, and the change of error \( \Delta e(k) \) is a negative number. This mean that the output \( y_p(k) = y_m - e(k) \) is increasing, i.e., heading in the direction of an overshoot. To compensate for this, we decrease the command signal. This corresponds to applying a correction term \( \mu(k) \) that is negative. Hence, we get the rule “if error is zero and change of error is negative medium, then output a negative big correction term”.
2.5 Two-layered fuzzy logic controller

In this section we describe a fuzzy pre-compensated fuzzy controller or a two-layered fuzzy logic controller (Kim et al., 1994; Pratumsuwan & Thongchai, 2009). The aim is to eliminate the steady state error and improve the performance of the output response for control systems with dead zones.
We now proceed to describe the proposed controller. First, define the variables $y'_m(k)$ and $e'(k)$ as follows:

$$y'_m(k) = y_m(k) + \mu(k)$$  
$$e'(k) = e(k) + \mu(k)$$

where $\mu(k)$ is a compensating term which is generated using a fuzzy logic scheme, which we will describe below. The proposed control scheme is shown in figure 13. The controller consists of two “layers” : a fuzzy pre-compensator, and a usual fuzzy PD controller. Hence we refer to the scheme as a two-layered fuzzy logic controller. The error $e(k)$, and change of error $\Delta e(k)$, are inputs to the pre-compensator. The output of the pre-compensator is $\mu(k)$.

The dynamics of overall system is then described by the following equations:

$$e(k) = y_m(k) - y_p(k)$$
$$\Delta e(k) = e(k) - e(k-1)$$
$$\mu(k) = G[e(k), \Delta e(k)]$$
$$y'_m(k) = y_m(k) + \mu(k)$$
$$e'(k) = y'_m(k) - y_p(k)$$
$$\Delta e'(k) = e'(k) - e'(k-1)$$
$$u(k) = K_1 y'_m(k) + F[e'(k), \Delta e'(k)]$$

where $K_1$ is the feed forward gain.

3. Pre-compensation of a Hybrid Fuzzy PID Controller

Pre-compensation of a hybrid fuzzy PID controller, as shown in figure 14, was developed to combine the advantages of both fuzzy pre-compensated PID controller and fuzzy pre-compensated fuzzy controller, which described in section 2.3, 2.4, and 2.5.

Figure 14 shows a switch between the fuzzy controller and the PID controller, where the position of the switch depends on the error between the actual value and set point value. If the error in PHS reaches a value higher than that of the threshold $e_0$, the control system applies the fuzzy controller, which has a fast rise time and a small amount of overshoot, to the system in order to correct the position with respect to the set point. When the position is
lower the threshold \( e_0 \) or close to the set point, the control system shift switch to the PID controller, which has better accuracy near the set point.

Fig. 14. Block diagram of pre-compensation of a hybrid Fuzzy PID controller.

4. Experimental Description

The specifications of a PHS are depicted in figures 15, 16 and table 3 respectively. Figure 15 shows a diagram of the tested system. The position control of a PHS procedure is described as follows: upon the intended initial and ending position of the piston (stroke) are given, the computer receives the feedback signal through DAQ card (A/D) from linear potentiometer, realizes various control algorithm and transmits a control signal through DAQ card (D/A) and amplifier card to proportional valve. The spool displacement of proportional valve is proportional to the input signal.

Fig. 15. PC-Based position control of a PHS.
Fig. 14. Block diagram of pre-compensation of a hybrid Fuzzy PID controller.

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Fig. 15. PC-Based position control of a PHS.

Fig. 16. The experimental setup.

<table>
<thead>
<tr>
<th>Elements</th>
<th>Descriptions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cylinder</td>
<td>piston diameter 16 mm, piston rod diameter 10 mm, stroke 200 mm</td>
</tr>
<tr>
<td>Proportional valve (4/3 closed-center spool, overlapped)</td>
<td>directly actuated spool valve, grade of filtration 10 μm, nominal flow rate 1.5l/min (at ΔpN = 5 bar/control edge), leakage oil flow &lt; 0.01 l/min (at 60 bar), nominal current 680 mA, resolution &lt; 1 mA, setting time of signal jump 0…100% = 60 ms, repetition accuracy &lt; 1%</td>
</tr>
<tr>
<td>Pump (supply pressure)</td>
<td>60 bar</td>
</tr>
<tr>
<td>Linear potentiometer</td>
<td>output voltage 0…10V, measuring stroke 200 mm, linearity tolerance 0.5%</td>
</tr>
<tr>
<td>Amplifier card</td>
<td>set point values ± 10 VDC, solenoid outputs (PWM signal) 24 V, dither frequency 200 Hz, max current 800 mA,</td>
</tr>
<tr>
<td>DAQ Card (NI 6221 PCI)</td>
<td>analog input resolutions 16 bits (input range ±10V), output resolutions 16 bits (output range ±10V), 833 kS/s (6 μs full-scale settling)</td>
</tr>
<tr>
<td>Operating systems &amp; Program</td>
<td>Windows XP, and LabVIEW 8.6</td>
</tr>
</tbody>
</table>

Table 3. Specifications of a PHS.

5. The Experimental Results
The control algorithms described in section 2.3, 2.4, and 2.5 were hybridized and applied to the PHS using by LabVIEW, Nation Instruments as the development platform and shown in figure 17.
In our experiments we compare the performance of conventional hybrid fuzzy PID controller to the proposed pre-compensation of a hybrid fuzzy PID controller. A testing of response of the system was performed using a square wave input. The parameter values of the pre-compensation of a hybrid fuzzy PID controller were experimentally determined to be: $K_1 = 0.93$, $K_p = 5.6$, $e_0 = 0.92$. Figures 18 and 19 shows the output response of a conventional hybrid fuzzy PID system compared to the pre-compensation of a hybrid fuzzy PID system. It is found that the pre-compensation of a hybrid fuzzy PID controller gives the most satisfying results of rise time, overshoot, and steady state error.

Fig. 18. Output response of conventional (hybrid fuzzy PID) controller.
Fig. 19. Output response of a proposed controller.

6. Conclusions

The objective of this study, we proposed the pre-compensation of a hybrid fuzzy PID controller for a PHS with deadzones. The controller consists of a fuzzy pre-compensator followed by fuzzy controller and PID controller. The proposed scheme was tested experimentally and the results have superior transient and steady state performance, compared to a conventional hybrid fuzzy PID controller. An advantage of the present approach is that an existing hybrid fuzzy PID controller can be easily modified into the control structure by adding a fuzzy pre-compensator, without having to retune the internal variables of the existing hybrid fuzzy PID controller.

In this study, an experimental research, so we do not address the problem of analyzing the stability of the control scheme in this paper. This difficult but important problem is a topic of ongoing research.

7. References


