



Elliptical instability in terrestrial planets and moons

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Abstract

Any planet may be subject to three kinds of harmonic mechanical forcing, driven respectively by libration, precession and tides. These forcings can generate flows in internal fluid layers such as fluid cores and subsurface oceans, whose dynamics then significantly differ from solid body rotation. In particular, tides and librations are known to be capable of exciting the so-called elliptical instability, corresponding to the destabilization of two-dimensional flows with elliptical streamlines, leading to three-dimensional turbulence. The presence of such an elliptical instability driven by tides and librations is investigated in terrestrial bodies. Its consequences on energy dissipation, on magnetic field induction and on heat flux fluctuations at the planetary scale are considered.

1. Introduction

The flow in fluid layers of planets and moons is of primary interest for their dynamics and evolution. Indeed, internal flows create energy dissipation, which remain negligible for stable laminar flows, but become significant for turbulent ones. Moreover, internal flows are directly responsible for magnetic field generation, either by induction of an existing background magnetic field or by excitation of a self-sustained dynamo. Finally, heat fluxes are also directly linked to flows in fluid layers, which can act as thermal blankets for stably stratified configurations, or as efficient heat flux conveyers in the case of convective flows.

Planetary fluid layers are subject to body rotation, which implies that inertial waves can travel through them. Usually damped by viscosity, these waves can be excited by libration, precession and tides, seen by the rotating fluid as harmonic mechanical forcings of azimuthal periodicity $m = 0, 1$ and 2 respectively. The fluid response to such forcings in ellipsoids is a long standing issue (see e.g. [1] for tides). In particular, it has been shown that the dynamics of a fluid layer are completely modified when the forcing directly resonates with an inertial wave. In addition, in-

ertial waves can also form triadic resonances, leading to parametric inertial instabilities. For instance, the so-called shear instability can be excited by precession [2] and the elliptical instability can be excited by tides [3, 4] and librations [5].

2. Elliptical instability

The elliptical instability is a generic instability that affects any rotating fluid whose streamlines are elliptically deformed. A fully three-dimensional turbulent flow is excited in the bulk as soon as (i) the ratio between the ellipticity of the streamlines β and the square root of the Ekman number E (which represents the ratio between the viscous and Coriolis forces) is larger than a critical value of order one and (ii) a difference in angular velocity exists between the mean rotation of the fluid and the elliptical distortion. In a planetary context, the ellipticity of streamlines is related to the gravitational deformation of the rigid boundaries of the considered fluid layer, corresponding either to dynamic tides or static bulges. The differential rotation between the fluid and the elliptical distortion can be oscillatory when due to libration in synchronized systems, or stationary, as for instance in non-synchronized ones: the elliptical instability is then referred to as libration driven elliptical instability (LDEI) and tide driven elliptical instability (TDEI) respectively. TDEI and LDEI have already been suggested to take place respectively in Earth [6] and in Io [5]. Using a local WKB method, we have reexamined these previous works and determined generic formulas for quantifying the presence of the elliptical instability in terrestrial bodies, taking into account the relative motion of the elliptical distortion and the presence of imposed thermal and magnetic fields.

3. Applications

Our theoretical results are applied to the telluric planets and moons of the solar system as well as to two Super-Earths, CoRoT-7b and GJ-1214b. We consider an ellipticity ranging between the hydrostatic equilib-

rium tides calculated at the external boundary of the considered layer with the Clairaut-Radau theory, and the diurnal tides. Regarding TDEI, only the Early Earth core is shown to be clearly unstable. Regarding LDEI, the core of Io is shown to be stable, contrary to previously thought [5], whereas Europa (Fig. 1), CoRoT-7b and GJ-1214b cores are clearly unstable over a large range of libration amplitude. The subsurface ocean of Europa and the core of Titan are also unstable, but in the vicinity of threshold. This present state-of-the-art does not preclude more unstable situations in the past.

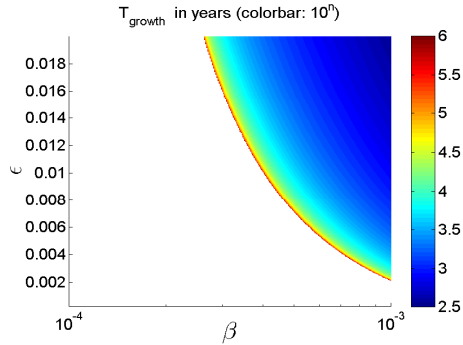


Figure 1: Evolution of the typical growth time of the LDEI in Europa's core, depending on the tidal bulge ellipticity β and the dimensionless libration amplitude ϵ .

4. Consequences

One can wonder what are the signatures and consequences of such an instability on the planetary dynamics. A first consequence would be on the orbital evolution and synchronization process: indeed, the elliptical instability generates three-dimensional turbulent flows with cycles of growth, saturation, fluctuations and relaminarization [4]. Timescales involved range typically between the spin period and the typical growth time of the instability. Dissipation rates at the planetary scale, hence its celestial dynamics, would then follow the same variations, with periods of rapid evolution when an elliptical instability is present, followed by more quiescent periods. The second consequence would be on heat flux variations at the planetary surface: indeed, as shown in [7], flows driven by elliptical instability are very efficient in transporting heat by advection. Hence, sub-adiabatic cores should not

be regarded as thermal blankets when tidally unstable. Besides, in the presence of natural thermal convection, the superimposition of chaotic elliptically driven flows would induce large scale variations of the same amplitude as the background heat flux. Internal flows driven by elliptical instability are also directly responsible for magnetic field generation. The question of whether or not LDEI and TDEI are dynamo capable is still open and remains out of reach of the currently available numerical capacity. But in any case, elliptically driven flows induce a magnetic field from an existing background one, with a significant amplitude. For instance, starting from the jovian magnetic field component along the rotation axis, the LDEI in Europa subsurface ocean is capable of explaining the perturbation of the background z-component of the magnetic field from 410 nT to 380 nT at a distance of Europa about 1.5 Europa radius, as measured by the Galileo's E4 flyby (see [8]). Finally, elliptical instability could also grow in hot-jupiters and stars in extra-solar systems, where they may cause the rotational axis of both bodies to change orientation with time at a relatively short timescale.

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