Spatial and Temporal Variability of Soil Moisture

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Abstract

The characterization of temporal and spatial variability of soil moisture is highly relevant for understanding the many hydrological processes, to model the processes better and to apply them to conservation planning. Considerable variability in space and time coupled with inadequate and uneven distribution of irrigation water results in uneven yield in an area. Spatial and temporal variability highly affect the heterogeneity of soil water, solute transport and leaching of chemicals to groundwater. Spatial variability of soil moisture helps in mapping soil properties across the field and variability in irrigation requirement. While the temporal variability of water content and infiltration helps in irrigation management, the temporal correlation structure helps in forecasting next irrigation. Kriging is a geostatistical technique for interpolation that takes into account the spatial auto-correlation of a variable to produce the best linear unbiased estimate. The same has been used for data interpolation for the C. T. A. E. Udaipur India. These interpolated data were plotted against distance to show variability between the krigged value and observed value. The range of krigged soil moisture values was smaller than the observed one. The goal of this study was to map layer-wise soil moisture up to 60 cm depth which is useful for irrigation planning.

Keywords: Soil Moisture, Spatial & Temporal Variability, Kriging

1. Introduction

Spatially and temporally varying soil moisture is being increasingly used as input to hydrological and meteorological models. Knowledge of spatial and temporal variability of field soil helps in characterization of the soil. The use of mathematical model to simulate the water and solute movement into the field soil has accelerated the need to understand the variability of soil properties that affect the interpretation of model output variability.

Soil moisture spatial distribution varies both vertically and laterally due to evapotranspiration and precipitation, influenced by topography, soil texture, and vegetation. While small scale spatial variations are influenced by soil texture, larger scales are influenced by precipitation and evaporation [1]. Field soil encompasses considerable inherent variability in their texture, structure and physical and chemical properties due to variability in parent material and other soil forming factors. Variability in water holding capacity of the soil can adversely affect yield and would complicate irrigation scheduling. Thus, variability has been found to have significant affect on moisture movement, process and the parameters associated with this process. The characteristics of soil moisture variability is essential for understanding and predicting land surface processes, that varies based on topography, soil texture, and vegetation at different spatial and temporal scales [2]. Thus, the spatial characteristics is a key parameter used in the background statistical error models as well dynamic propagation of the modeled state uncertainty in data assimilation modeling systems [3-7].

Temporal variability of soil water properties are induced by tillage, cropping and other management practices. Surface seal and compaction of soil are predominant phenomenon that affects water flow.

The geostatistical studies for soil moisture variability [8-13] are carried out at the scales of small catchments areas (1-5 km²). S. G. Reynolds [14] found a close relation between sizes on soil moisture variability, with R² of 0.7 considered to be best. To reduce uncertainty, O. R. Dani and R. J. Hanks [15] used state space models for soil water...
balance and evapotranspiration in application to spatial and temporal estimation methods. B. P. Mohanty, et al. [16] analyzed and mapped field scale soil moisture variability using high resolution ground based data. J. A. Huisman [17] studied ground penetrating radar for mapping soil water content at intermediate scales between point and remote sensing measurements.

A variogram, a central concept in geostatistics, is used to analyze the structure of spatial variation of soil moisture. The experimental variogram characterizes the spatial variability in the measured data. This variogram is used in Kriging to determine soil moisture values at unsampled locations. This section first describes the effect of selection of active separation distance for best model fitting. The variogram structure consists of the nugget (the variance at zero lag distance), sill (the variance to which the variogram asymptotically rises), and decorrelation length (range of spatial dependence). The decorrelation length varies based on minimum distance between sampling locations and size of sampled area [13]. In this study the average grid resolution (40 m × 40 m) of soil moisture data layer – wise up to 60 cm depths were analyzed. One of the major issues in variographic analysis is the selection of total lag distance for variogram fitting to experimental data. As the separation distance increases, after half of the total separation distance, the variogram starts to decompose at larger separation distances due to the reduced availability of pairs. Thus to obtain robust estimation of the variogram, we ignored pairs at larger separation distances that usually have smaller variance. The separation distance is selected based on the criterion that 95% pairs should have been used for variogram model fitting. Kriging is an interpolation technique based on the theory of regionalized variables developed by G. Matheron [18]. Kriging offers a wide and flexible variety of tools that provide estimates for unsampled locations using weighted average of neighboring field values falling within a certain distance called the range of influence. Kriging requires a variogram model to compute variable values for any possible sampling interval. The variogram functionality in conjunction with kriging allows us to estimate the accuracy with which a value at an unsampled location can be predicted given the sample values at other locations [19-21]. Kriging provides optimal interpolation of soil moisture at grid points in a spatial domain based on autocorrelation in the variograms. The theoretical variogram model (Gaussian, spherical, exponential, or linear) that best fits the experimental variogram was selected for soil moisture mapping using the block Kriging technique [22].

We are not aware of any documented study on layerwise soil moisture mapping available for study area. Hence, the study of spatial and temporal distribution of soil moisture helps in mapping soil properties across the field and variability in irrigation requirement, which is helpful in real time management at field scale.

2. Material and Methods

2.1. Measurement of Soil Moisture

The instructional farm of CTAE, Udaipur having an area of 2.16 hectare was selected for soil sampling. The area was surrounded by vegetation and the field was bare at the time of observation. Grid having a size of 40 m × 40 m was formed in that area. Soil samples were taken at each grid point at the depths of 7.5 cm, 15 cm, 30 cm, 45 cm and 60 cm. These soil moisture data were then used for analysis of spatial and temporal variability. One set of soil moisture was recorded prior to irrigation and the other, after irrigation.

2.2. Autocovariance and Autocorrelation

Representation of variability of soil properties by frequency distribution does not assume that the values are random and independent. Physically, it is expected that the values of any properties of two neighboring points will be closer to each other then those at two distant points.

Limiting consideration of spatial relationship only to the second order, i.e., second moment, the relationship expressed by the auto covariance as a function of separation distance \(C(h)\) can be presented mathematically, thus,

\[ C(h) = E \left[ (Z(X) - \mu) (Z(X+h) - \mu) \right] \]  

\[ = E \left[ Z(X) - Z(X+h) \right] - \mu^2 \]  

The computational form of \(C(h)\) is

\[ \gamma(h) = \frac{1}{2N(h)} \sum_{i=1}^{N(h)} (z(x_i) - z(x_i+h))^2 \]  

where, \(\gamma(h)\) = Semi-variance for interval distance class \(h\), \(z_i\) = measured sample value at point \(i\), \(z_i+h\) = measured sample value at point \(i+h\), and \(N(h)\) = total number of sample couples for the separation interval \(h\).

The least squares best-fit criteria is used to fit a model to the experimental semi-variance data through which the nugget \((C_0)\), sill \((C_0 + C)\), and decorrelation length or range of spatial dependence \((A_0)\). From Equation (1) and (2), it is clear that \(C_0\) is the variance \(\sigma^2\) or its sample estimate of the variable. The ratio, \(C(h)/C_0\), is auto correlation, \(\gamma(h)\), having values between +1 and −1. It is also apparent that for \(C(h)\) and \(\gamma(h)\) to exist, the mean and
variance of the population must be finite and constant in the area of consideration.

2.3. Semivariance and Semivariogram

The Quantification of spatial dependence is called semi variance. The intrinsic hypothesis states that for any two locations separated by lag distance, ‘h’, the variance of the differences of the measured property is finite and dependent of its (x, y) position. The Variance depends on the lag distance (h)

\[ \text{Var}[z(x) - z(x + h)] = 2\gamma(h) \]  

(3)

Therefore, the model of soil variance is

\[ Z(x) = \mu + \epsilon(x) \]  

(4)

where, \( z(x) \) = expected value \( \mu = \) mean, \( \epsilon(x) = \) residual value

Semi variance, \( \gamma(h) \) is a function of \( h \). This equation is similar to Equation (1). Expected \( \epsilon(x) \) is spatially dependent random component with zero mean and variance defined by \( \gamma(h) \). The semi variance may be estimated as a function of \( h \) by Equation (2). The semi variogram is a graphical model that indicates the spatial relationship between measured values. The common characteristics of semivariogram are that they will increase from some minimum value called the nugget at a zero separation distance to some finite maximum value as the separation distance increases. The maximum value of a variogram is typically an estimate of variance. The distance at which the variogram first reaches the sill is termed as the range. The range is an estimate of the distance over which the measurements are spatially correlated and may reflect the physical extent of similar soil bodies.

2.4. Selection of Model

Before estimation of soil moisture, a mathematical model has to be fitted to it. Selection of model is based on sill, range and nugget of the experimental semivariogram model. From the various models, i.e., random model, spherical model, linear model, logarithmic model and parabolic model, considered for the observations of the present study, the spherical model was found to be best suited for the purpose.

Spherical model is probably the most commonly used model. It has a simple polynomial expression and its shape matches well with the observed data. The model ensures almost a linear growth up to a certain distance before stabilizing. The tangent at origin intersects the sill at a point with an abscissa \((2/3 \times a)\) and slope of this tangent originates at \(3c/2a\). This can be useful while fitting models. It is characterized by two parameters \( c \) and \( a \), and mathematically represented by an equation as:

\[ \gamma(h) = C \left( \frac{3h}{2a} - \frac{h^3}{2a^3} \right) \text{ for } h < a \]

\[ \gamma(h) = C \text{ for } (h > a) \]

After selecting the model, kriging technique was used for interpolation of values. In the present study, block kriging is used for estimating the kriged value. The grid system was developed to create a common reference point for all information.

Kriging is the application of geostatistical techniques for interpolation. The estimation fulfills the following conditions (Cuenca, and Amegee, 1987).

1) Linearity: Kriging estimate is formed from a linear combination of measured data at surrounding points. It can be expressed as:

\[ K(X_p) = \lambda_1 K(X_1) + \lambda_2 K(X_2) + \lambda_3 K(X_3) + \ldots + \lambda_n K(X_n) \]

where, \( K(X) = \) value of parameter at (X), \( \lambda_i = \) weight assigned to each measured value of estimation

2) Unbiasedness: The condition of unbiasedness is that mean of the estimates should be equal to the mean of the measured value, that is:

\[ E[K'(X)] = E[K(X)] = m \]

But

\[ E[K'(X)] = m \sum_{i=1}^{n} \lambda_i \]

where, \( m = \) mean. The above equation gives the following result \( \sum_{i=1}^{n} \lambda_i = 1 \), that is, the sum of individual weight \( \lambda_i \) must be equal to unity.

3) Best Criterion: As per the third constraint, the variance should be minimum, i.e., the error between the kriging estimates and the true value is minimized. To fulfill this condition, derivatives of the variance with respect to weights \( \lambda_i \) should be zero. As there are \( n \) weights, the above procedure will produce \( n \) equations with \( n \) unknown weights. Since there is one more Equation, i.e.,

\[ \sum_{i=1}^{n} \lambda_i = 1 \]

hence, there is \( n + 1 \) equation with \( n \) unknown. To mitigate the situation, one new unknown, i.e., Lagrangian multiplier a constant equal to zero has to be added. For convenience Lagrangian multiplier has been taken as \( \mu \).

Therefore, kriging system of equation in terms of semi variance function appears as:

\[ \lambda_1 \gamma(h_1) + \lambda_2 \gamma(h_2) + \lambda_3 \gamma(h_3) + \ldots + \lambda_n \gamma(h_n) + \mu = \gamma(h_p) \]

\[ \lambda_1 \gamma(h_1) + \lambda_2 \gamma(h_2) + \lambda_3 \gamma(h_3) + \ldots + \lambda_n \gamma(h_n) + \mu = \gamma(h_p) \]

\[ \ldots \]

\[ \lambda_1 \gamma(h_n) + \lambda_2 \gamma(h_n) + \lambda_3 \gamma(h_n) + \ldots + \lambda_n \gamma(h_n) + \mu = \gamma(h_p) \]
By solving the above system all the assigned weights are determined and value of soil moisture is estimated at any point \( p \).

2.5. Cross Validation

The estimated krigged values are subjected to cross validation. For a cross validation at each point, the reduced estimation error is obtained by dividing the estimation error by the standard deviation of estimation. The goodness of estimation is expressed by two conditions on the reduced estimation errors: 1) minimum, nearly zero mean and 2) variance near to unity.

3. Results and Discussion

3.1. Statistical Analysis of Observed Data

This was conducted in two stages
1) The traditional summary of statistics, i.e., mean, standard deviation, coefficient of variation, skewness and kurtosis were estimated
2) Semi variance was defined and difference in nugget, sill and range were examined for each depth.

3.2. Summary Statistics of the Soil Moisture Data

The different statistical properties for the soil moisture at different depths and for both observations were calculated. It was observed that before irrigation the soil was very dry with mean moisture content of 2.89% to 8.68%. After irrigation, this has been a drastic increase from 10.16% to 11.88%. At lower depths, the variation in mean is almost constant before and after irrigation.

3.3. Estimation of Geostatistical Parameters

The semi variance was computed using Equation (3) for different lag distance. Using the data (Table 1) experimental semivariograms for different lags was plotted. A model was fitted to the plotted experimental semivariograms. The parameters of the fitted model are given in Table 2. The fitted spherical model can be expressed as:

\[
\gamma(h) = C_o + C_1 \left[ \frac{3}{2} \left( \frac{h}{r} \right) - \frac{1}{2} \left( \frac{h}{r} \right)^3 \right] \quad \text{For } 0 < h < r
\]

\[
\gamma(h) = C_o + C_1 \quad \text{For } h > r
\]

The experimental semivariogram and fitted model layer-wise upto 60 cms depth as shown in Figures 1(a) to 5(b). Nugget indicates error of estimation of parameter at the smallest sampling interval. If nugget expressed as a percent of sill, is less than 24 percent, the variable may be considered showing a strong spatial dependence; if it is between 25 to 75 percent, it is considered as moderately dependent and if it exceeds 75 percent spatially, it is said to have poor dependence.

3.4. Contour Maps of Soil Moisture Variability

Contour maps were prepared for all the depths and for both dry and wet condition, using surfer. Surfer uses the inverse distance technique for interpolating irregularly spaced measured data to a specified grid size.

In first set of observations (dry condition), it was observed that for 7.5 cm depth maximum variability is observed at the corner of the field, which is mainly due to vegetation, which reduce evaporation. In the centre of

| Lag | Average Distance (m) | 7.5 | 15 | 30 | 45 | 60 | 7.5 | 15 | 30 | 45 | 60 |
|-----|---------------------|-----|----|----|----|----|-----|----|----|----|----|----|
| 1   | 40.00               | 2.8 | 2.45 | 3.59 | 8.46 | 15.87 | 16.73 | 3.62 | 5.79 | 9.74 | 8.04 |
| 2   | 56.57               | 2.04 | 2.34 | 2.72 | 6.43 | 11.64 | 20.32 | 3.54 | 6.03 | 8.05 | 8.58 |
| 3   | 80.00               | 3.04 | 2.33 | 2.90 | 5.32 | 11.35 | 17.57 | 4.37 | 6.08 | 10.07 | 7.85 |
| 4   | 89.44               | 2.41 | 1.85 | 2.17 | 3.81 | 7.68 | 14.42 | 3.95 | 6.85 | 8.32 | 9.86 |
| 5   | 113.14              | 5.86 | 5.24 | 7.21 | 15.70 | 30.01 | 4.92 | 4.12 | 5.46 | 11.82 | 9.46 |
| 6   | 120.00              | 4.47 | 5.17 | 6.09 | 10.84 | 17.54 | 15.24 | 6.11 | 11.69 | 6.94 | 9.46 |
| 7   | 126.49              | 3.63 | 2.46 | 3.37 | 5.95 | 9.68 | 26.00 | 7.05 | 14.09 | 7.47 | 9.05 |
| 8   | 144.22              | 1.23 | 5.24 | 3.51 | 2.50 | 3.89 | 7.37 | 6.35 | 9.18 | 8.51 | 3.77 |
| 9   | 162.81              | 4.82 | 4.39 | 3.36 | 2.42 | 7.41 | 19.93 | 11.31 | 14.74 | 7.47 | 7.33 |
| 11  | 202.26              | 6.91 | 4.43 | 3.06 | 4.99 | 5.27 | 6.09 | 8.04 | 7.45 | 2.39 | 1.17 |
| 12  | 215.41              | 9.22 | 7.95 | 4.48 | 0.38 | 0.56 | 11.55 | 13.83 | 14.83 | 6.22 | 4.08 |
Table 2. Different parameters of the fitted model of semivariogram.

<table>
<thead>
<tr>
<th>S.No</th>
<th>Depth (cm)</th>
<th>Type of Model</th>
<th>Range</th>
<th>Nugget</th>
<th>Sill</th>
<th>Nugget as % of Sill</th>
<th>Spatial Dependence</th>
</tr>
</thead>
<tbody>
<tr>
<td>First Observation</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>7.5</td>
<td>Spherical</td>
<td>125</td>
<td>0.45</td>
<td>3.05</td>
<td>14.75</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>2</td>
<td>15</td>
<td>Spherical</td>
<td>113.1</td>
<td>0.327</td>
<td>2.947</td>
<td>11.09</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>3</td>
<td>30</td>
<td>Spherical</td>
<td>110</td>
<td>0.46</td>
<td>3.1</td>
<td>14.84</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>4</td>
<td>45</td>
<td>Spherical</td>
<td>113.09</td>
<td>0.638</td>
<td>5.748</td>
<td>11.09</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>5</td>
<td>60</td>
<td>Spherical</td>
<td>113.09</td>
<td>1.1787</td>
<td>10.61</td>
<td>11.10</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>Second Observation</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>1</td>
<td>7.5</td>
<td>Spherical</td>
<td>125</td>
<td>2.1</td>
<td>14</td>
<td>15</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>2</td>
<td>15</td>
<td>Spherical</td>
<td>113.09</td>
<td>0.548</td>
<td>4.94</td>
<td>11.09</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>3</td>
<td>30</td>
<td>Spherical</td>
<td>113.09</td>
<td>0.836</td>
<td>7.525</td>
<td>11.10</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>4</td>
<td>45</td>
<td>Spherical</td>
<td>113.09</td>
<td>0.848</td>
<td>7.634</td>
<td>11.10</td>
<td>Strongly dependent</td>
</tr>
<tr>
<td>5</td>
<td>60</td>
<td>Spherical</td>
<td>113.09</td>
<td>0.804</td>
<td>7.244</td>
<td>11.09</td>
<td>Strongly dependent</td>
</tr>
</tbody>
</table>

In the field, soil moisture is almost constant Figure 6(a), which is due to the bare field, which provides a free evaporation surface.

As shown in Figure 7(a) for 15 cm depth, variability is large as compared to 7.5 cm depth, but the same pattern is observed at this depth, i.e., maximum in the corners and minimum at the centre. Mean moisture content at 15 cm depth is higher than 7.5 cm depth.

As shown in Figures 8(a), Figure 9(a) and Figure 10(a) shows a uniform spatial variability with 30 cm depth, 45 cm depth and 60 cm depth respectively. Mean moisture content was found higher at 60 cm depth than other depths.

In the second set of observations, it was observed that for 7.5 cm depth, moisture content at the corner of the fields is almost constant whereas in the middle it is very high which shows non uniform supply of water as shown in Figure 6(c).

For 15 cm depth, high spatial variability is obtained as compared to 7.5 cm depth Figure 6(c). In the middle, the moisture content is very high at 7.5 cm depth due to the same reason of non uniform supply of water as shown in Figure 7(c).

For 30 cm depth, 45 cm depth and 60 cm depth the variability is almost same Figure 8(c), 9(c) and 10(c), respectively.

From the maps, it was observed that in the first set of observation high spatial variability was observed as compared to the second set of observation. This is because of the reason that the second sets of observation were taken after irrigation. Soil profile is almost saturated with water. Some variability was observed, which shows the non uniform supply of irrigation water. The maximum variability is observed up to 30 cm depth where as for 45 cm and 60 cm depths, variability is almost constant in both sets of observations. In both sets of observations maximum spatial variability was observed at 30 cm depth (Figures 8(a) and 8(c)).
Figure 2. (a) Experimental semivariogram of first observation at 15 cm depth and fitted model; (b) Experimental semivariogram of second observation at 15 cm depth and fitted model.

Figure 3. (a) Experimental semivariogram of first observation at 30 cm depth and fitted model; (b) Experimental semivariogram of second observation at 30 cm depth and fitted model.

Figure 4. (a) Experimental semivariogram of first observation at 45 cm depth and fitted model; (b) Experimental semivariogram of second observation at 45 cm depth and fitted model.
Figure 5. (a) Experimental semivariogram of first observation at 60 cm depth and fitted model; (b) Experimental semivariogram of second observation at 60 cm depth and fitted model.

Table 3. Statistical parameters of measured and krigged values of soil moisture.

<table>
<thead>
<tr>
<th>Depth</th>
<th>Observation</th>
<th>Max. (%)</th>
<th>Min. (%)</th>
<th>Range (%)</th>
<th>Mean (%)</th>
<th>Var. (%)</th>
<th>S.D (%)</th>
<th>C.V</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
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<td></td>
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<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>7.5</td>
<td>Measured</td>
<td>7.89</td>
<td>0.92</td>
<td>6.97</td>
<td>2.93</td>
<td>3.50</td>
<td>1.87</td>
<td>0.64</td>
</tr>
<tr>
<td></td>
<td>Krigged</td>
<td>5.29</td>
<td>1.12</td>
<td>4.17</td>
<td>2.87</td>
<td>1.55</td>
<td>1.25</td>
<td>0.43</td>
</tr>
<tr>
<td>15</td>
<td>Measured</td>
<td>18.98</td>
<td>7.16</td>
<td>11.82</td>
<td>10.54</td>
<td>8.11</td>
<td>2.85</td>
<td>0.27</td>
</tr>
<tr>
<td></td>
<td>Krigged</td>
<td>14.55</td>
<td>5.89</td>
<td>8.66</td>
<td>10.48</td>
<td>5.90</td>
<td>2.43</td>
<td>0.23</td>
</tr>
<tr>
<td>30</td>
<td>Measured</td>
<td>7.67</td>
<td>1.44</td>
<td>6.23</td>
<td>4.07</td>
<td>3.27</td>
<td>1.81</td>
<td>0.44</td>
</tr>
<tr>
<td></td>
<td>Krigged</td>
<td>6.16</td>
<td>2.30</td>
<td>3.86</td>
<td>4.05</td>
<td>1.64</td>
<td>1.28</td>
<td>0.32</td>
</tr>
<tr>
<td>45</td>
<td>Measured</td>
<td>15.12</td>
<td>7.26</td>
<td>7.86</td>
<td>10.16</td>
<td>4.90</td>
<td>2.21</td>
<td>0.22</td>
</tr>
<tr>
<td></td>
<td>Krigged</td>
<td>13.53</td>
<td>7.70</td>
<td>5.83</td>
<td>10.15</td>
<td>2.91</td>
<td>1.71</td>
<td>0.17</td>
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<tr>
<td>60</td>
<td>Measured</td>
<td>9.30</td>
<td>2.63</td>
<td>6.67</td>
<td>5.38</td>
<td>3.56</td>
<td>1.89</td>
<td>0.35</td>
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<tr>
<td></td>
<td>Krigged</td>
<td>7.68</td>
<td>3.33</td>
<td>4.35</td>
<td>5.33</td>
<td>1.91</td>
<td>1.38</td>
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</tbody>
</table>
3.5. Kriging of Soil Moisture

In order to estimate the soil moisture value at observation point, the searching radius was determined, which was based on spatial range observed in the fitted model of semivariogram. The searching radius indicates that the measurements within the range are to be considered to estimate the soil moisture at that point. Range for each depth as shown in Table 2.

By using Sill, range and nugget as shown in Table 1, the krigged value of soil moisture were determined at each depth with the help of Datamine software. Statistical parameters were calculated for measured and krigged soil moisture values and the parameters are presented in Table 3. Mean and measured krigged value is almost same. By analyzing the statistical parameters, i.e., variance, standard deviation and coefficient of variation, it was found that they have always been on the lower side of the krigged estimate as compared to those obtained with measured value, the trend is indicative of lesser variability in the krigged estimates of soil moisture thereby projecting more consistency and reliability. The lower value of coefficient of variation of krigged value indicates that there has been consistency in krigged estimates.

3.6. Comparison of Spatial Structure of Measured and Krigged Soil Moisture

Contour maps of soil moisture variability were plotted for measurement and krigged values for each depth and for both observations and their variability and spatial structure were compared (Figures 6(b), 6(d), 7(b), 7(d), 8(b), and 8(d), 9(b), 9(d), 10(b), 10(d)). Large variability is observed in first observation, i.e., before irrigation compared to second observation, which is spatially less variable. For first observation large variability is observed

![Figure 6](image_url)

Figure 6. (a) and (b) measured and krigged value of soil moisture at 7.5 cm depth for dry condition, (c) and (d) measured and krigged value of soil moisture at 7.5 cm depth for wet condition.
Figure 7. (a) and (b) measured and krigged value of soil moisture at 15 cm depth for dry condition; (c) and (d) measured and krigged value of soil moisture at 15 cm depth for wet condition.
Figure 8. (a) and (b) measured and krigged value of soil moisture at 30 cm depth for dry condition; (c) and (d) measured and krigged value of soil moisture at 30 cm depth for wet condition.

Figure 9. (a) and (b) measured and krigged value of soil moisture at 45 cm depth for dry condition; (c) and (d) measured and krigged value of soil moisture at 45 cm depth for wet condition.
at 30 cm depth as in Figure 8(a) and comparatively less variability is observed at 7.5 cm depth as in Figure 6(a) due to lack of moisture. After kriging, the variability was reduced as shown in krigged map. Also the range of the krigged values are less than that of the observed one (Table 3).

For second observation the largest variability was observed at 15 cm depth as in Figure 7(c), which was reduced drastically for krigged estimate whereas least variability was observed at 7.5 cm depth. The range of second observation indicates that the water is not uniformly distributed in the whole field. For the lower depths, the variability is almost same for both sets of observations for measured as well as krigged estimates, because some time is required for water to percolate down and during that time sufficient variability is observed at lower depth.

From the maps, it was observed that the spatial variability is considerably reduced after kriging for each depth, especially for second observation.

Contour maps of soil moisture for each depth were plotted. Careful comparison of the contour map of soil moisture envisaged that there has been considerable reduction in spatial variability in case of krigged estimates. On the basis of the above discussion, it can be said that the krigged values are more consistent and are true representative of soil moisture values. Therefore, contour maps developed with krigged estimates would be more precise than those developed with measured value.

4. Conclusions

Based on the findings it can be said that the krigged val-
ues are more consistent and true representative of soil moisture values. Hence, on the basis of past soil moisture values the krigged value of soil moisture at particular time and space may be estimated. Statistical parameters reflect that the variability of soil moisture reduces significantly after kriging. These estimated values help in proper irrigation scheduling along with necessary information on the crops to be grown and expected yield of the same.

5. References


