The Third Generation Partnership Project’s Long Term Evolution-Advanced (3GPP-LTE-Advanced) group is developing a new standard for mobile broadband access that will meet the throughput and coverage requirements of a fourth generation cellular technology [1]. One of the main challenges faced by the developing standard is providing high throughput at the cell edge. Technologies like multiple input multiple output (MIMO), orthogonal frequency division multiplexing (OFDM), and advanced error control codes enhance per-link throughput but do not inherently mitigate the effects of interference. Cell edge performance is becoming more important as cellular systems employ higher bandwidths with the same amount of transmit power and use higher carrier frequencies with infrastructure designed for lower carrier frequencies [2]. One solution to improve coverage is the use of fixed relays, pieces of infrastructure without a wired backhaul connection, that relay messages between the base station (BS) and mobile stations (MSs) through multihop communication [3–11].

Many different relay transmission techniques have been developed over the past ten years. The simplest strategy (already deployed in commercial systems) is the analog repeater, which uses a combination of directional antennas and a power amplifier to repeat the transmit signal [12]. More advanced strategies use signal processing of the received signal. Amplify-and-forward relays apply linear transformation to the received signal [13–15] while decode-and-forward relays decode the signal then re-encode for transmission [16]. Other hybrid types of transmission are possible including the information-theoretic compress-and-forward [17] and the more practical demodulate-and-forward [18]. In research, relays are often assumed to be half-duplex (they can either send or receive but not at the same time) or full-duplex (can send and receive at the same time) [19]. While full-duplex relays are under investigation, practical systems are considering half-duplex relay operation.
which incur a rate penalty since they require two (or more timeslots) to relay a message. Two-way relays avoid the half-duplex assumption by using a form of analog network coding that allows two messages to be sent and received in two time-slots [20]. Relaying has been combined with multiple antennas in the MIMO relay channel [21, 22], and the multiuser MIMO relay [23]. Despite extensive work on relaying, prior work has not as extensively investigated the impact of interference as seen in cellular systems. One exception is [24], which utilizes resource allocation to avoid interference. Conversely, this paper considers exploiting the interference using increased spatial dimensions via extra antennas at the relay.

The first commercial wireless network to incorporate multihop communication was IEEE 802.16j [25]. Its architecture constrained the relays for being served by a single base station and allowed them to communicate in only one direction at a time (i.e., either uplink or downlink). From a design perspective, unfortunately, IEEE 802.16j had several restrictions that drastically limited its capability, for example, the transparent mode that supports relaying-ignorant mobile subscribers. Further, the relays were not designed to specifically mitigate interference. Consequently, LTE-advanced may consider more sophisticated relay strategies and thus may expect larger performance gains from the inclusion of relaying.

Investigation into the possible relaying architecture for LTE-Advanced has begun. The coverage and throughput gains for an OFDMA network have been numerically analyzed using both idealized terrain [26] and ray tracing software applied to particular urban areas [27, 28]. The types of relaying strategies considered in these papers were relatively simple, considering only one-way single-antenna decode-and-forward relaying. The general conclusion is that multihop relaying is a cost-efficient solution to achieving the systemwide goals of next generation OFDMA networks.

In this paper, we evaluate the benefits of several promising relaying strategies for 3GPP-LTE-Advanced. We consider three specific strategies including one-way relays, two-way relays, and shared relays. The one-way relay possesses only a single antenna and is deployed once in every sector. It performs a decode-and-forward operation and must aid the uplink and downlink using orthogonal resources. The shared relay concept was recently proposed in IEEE 802.16m [29] but is readily applicable to GPP. The idea is to place a multiple antenna relay at the intersection of two or more cells. The relay decodes the signals from the intersecting base stations using the multiple receive antennas to cancel interference and retransmits to multiple users using MIMO broadcast methods. The two-way relay, also called analog network coding [30] and bidirectional relaying [31], is a way of avoiding the half-duplex loss of one-way relays [32]. The key idea with the two-way relay is that both the base station and mobile station transmit to the relay at the same time in the first time slot. Then, in the second time slot, the relay rebroadcasts what it received to the base station and mobile station. Using channel state information and knowledge of their own messages, the base and mobile stations are able to decode information sent from the other party.

To study the performance of each relaying strategy we derive expressions for their achievable rate assuming Gaussian signaling. The rate expressions illustrate how other-sector and other-cell interferences impact performance and allow for efficient network simulation. For example, the analysis shows that two-way relaying has the potential for severe interference enhancement since (i) there are more sources of interference and (ii) it performs an amplify and forward that rebroadcasts the received interference. Shared relaying seems to offer the most resilience to interference since it exploits the MIMO MAC (multiple access) channel to decode three signals cochannel and the MIMO broadcast channel to deliver three interference-free signals. The direct path is neglected in each of the relaying scenarios as the area under consideration is mainly the cell edge.

To compare the performance of different relay strategies, we compare their performance using a system simulator. Channel models from the IEEE 802.16j specification [33] are used since they include models for fixed relays. The simulator places users in fixed locations in each sector and computes the sum rates derived in this paper assuming that the channel is fixed over the length of the packet. These rates are reasonable in that they are nearly achievable in real slow-fading systems with powerful coding and aggressive adaptive modulation. Comparing the performance of different relaying strategies in a single set of simulations provides extensive comparability that is not possible when comparing different references.

As a baseline for performance comparison we compare with several different cellular configurations including sectoring and frequency reuse. To be fair, we also compare with an emerging transmission technique known as base station coordination [34–37]. The idea is that by coordinating the transmission of multiple base stations, sharing data and channel state information, it is possible to eliminate interference by effectively having the multiple base stations act as one single transceiver. Several suboptimal strategies have been proposed to realize base station coordination such as coordinated resource allocation [38] or clustered coordination [39]. Such strategies have made base station coordination a viable technology for GPP that may be complementary to relaying or a more complex alternative.

The main conclusions of this paper are as follows. The one-way relay enhances capacity near the cell edge but is very limited by interference. The shared relay is able to remove much of the dominant interference and provides much of the gain of localized base station coordination, which gives the highest rates of the strategies compared in this paper. The two-way relay struggles to get any rate to the mobile-to-base station link unless the relay is very close to the mobile station because of interference from adjacent base stations. Further research into this area is warranted, however, by the success of the two-way relay in the downlink combined with its simplicity. In all cases, frequency reuse 1 (where each sector and each cell use the same spectrum) outperformed frequency reuse 6 (where the spectrum is divided into six bands, one for each sector).
The rest of this paper is organized as follows. Section 2 introduces the general cellular model considered in this paper. Section 3 discusses the one-way architecture as a baseline of comparison for the rest of the paper. Section 4 considers two-way relaying and derives the sum rate over a number of different CSI assumptions. Section 5 presents a transmission strategy for shared relaying and derives the sum rate. Section 6 discusses base station coordination over a limited area. Section 7 compares all of the presented strategies under different frequency reuse plans. Section 8 gives a discussion of the results from the previous section while Section 9 summarizes the main results in the paper and provides directions for future work.

This paper uses the following notation. The log refers to \( \log_2 \). Bold uppercase letters, such as \( \mathbf{A} \), denote matrices, bold lowercase letters, such as \( \mathbf{a} \), denote column vectors, and normal letters \( a \) denote scalars. The notation \( \mathbf{A}^\dagger \) denotes the Hermitian transpose of matrix \( \mathbf{A} \). The letter \( E \) denotes expectation, \( \min\{a, b\} \) denotes the minimum of \( a \) and \( b \), \( |a| \) is the magnitude of the complex number \( a \), and \( \|a\| \) is the Euclidean norm of vector \( a \).

## 2. System Model

In the analysis we consider an arbitrary hexagonal cellular network with at least three cells as shown in Figure 1; the simulations will include an extra tier of total interference (see Section 7 for details). The base stations are located in the center of each cell and consist of six directional antennas, each serving a different sector of the cell. The antenna patterns are those specified in the IEEE 802.16j channel models [33]. The channel is assumed static over the length of the packet, and perfect transmit CSI is assumed in each case to allow for comparison of capacity expressions. Thus, each cell has \( S = 6 \) sectors. The multiple access strategy in each sector is orthogonal such that each antenna is serving one user in any given time/frequency resource. We assume that the channels are narrowband in each time/frequency resource, constant over the length of a packet, and independent for each packet. This is known as the block fading model. These assumptions correspond to one ideal LTE OFDM subchannel and, although unrealistic in practice, are useful for deriving capacity equations that can be used for deciding the actual data rate and for simulations deriving an upper bound on throughput.

Most of the analysis in this paper will focus on downlink communication, but a similar analysis can be applied to the uplink in each case. In the one-way and shared relay cases, communication takes place in two orthogonal phases. In the first phase, the base station transmits while the relay receives (the mobile may or may not receive), and in the second phase the relay transmits while the mobile receives. There will be a capacity penalty due to the use of two phases to transmit the same information. We assume that the phases are synchronized so that the first phase and second phase occur simultaneously in all cells. In the two-way case, the base station and mobile stations both transmit in the first phase, while the relay transmits in the second phase, as will be explained in Section 4.

We consider different rates of frequency reuse. For a reuse of \( r \), the spectrum is divided into \( r \) orthogonal bands where each one will be used in a regular pattern \( M/r \) times over an area covering \( M \) cells. We refer to this as \( M \times r \) reuse. In this paper we will consider only \( 1 \times 1 \) reuse and \( 1 \times 6 \) reuse, and thus for simplicity we will henceforth drop the \( M \) from the notation and refer to only reuse \( r \). In this case, mutual information will be scaled by \( 1/r \) to make fair comparisons. Different patterns of frequency reuse are used in different scenarios as shown in Figure 2. For shared relaying and base station coordination, the interfering sectors share the same frequency. For the one-way relay and the two-way relay, the interfering sectors use different frequencies. The analysis assumes that one user per sector has been arbitrarily scheduled, meaning that the exact scheduler is not considered since we are not analyzing multiuser diversity.

The system details of each specific architecture are explained in their respective sections. Specifically, we compare each transmission model with frequency reuse factors of 1 and 6. The one-way model consists of one single-antenna relay per sector serving only users in its sector. The shared relay is shared among three sectors in three adjacent cells (e.g., the sectors making up the center triangle in Figure 1), allowing it to serve users in each of those sectors. The two-way model consists of a single amplify-and-forward relay per sector and allows simultaneous uplink/downlink communication, removing the half-duplex loss of conventional relaying. Base station coordination assumes a lossless, zero-delay fiber link between adjacent sectors (the same ones serving the shared relay) and allows the base stations to cooperatively transmit in the downlink and receive in the uplink as if they were one large multiple-antenna transceiver.
Each of these models is discussed in the remainder of this paper.

Each hop of communication is assumed to use ideal coding and adaptive modulation so that mutual information may be used. This does not, however, guarantee that the end-to-end capacity is reached as the relays are performing a strictly suboptimal strategy (decode-and-forward for the shared and one-way relays, amplify-and-forward for the two-way relay). Other-sector and other-cell interference is assumed Gaussian and treated as noise unless specifically treated as in the shared relay case. All RF receive chains are assumed to have identical noise variance \( \sigma^2_N \).

3. One-Way Relaying Model

In this section we introduce the one-way transmission model, which resembles IEEE 802.16j relaying. As with IEEE 802.16j, each relay has a single “parent” base station, creating a tree architecture. The relay, which decodes its receives signal, is thus a part of the cell its parent BS serves. Further, the uplink and downlink are divided orthogonally in time or frequency, depending on the duplexing method. Finally, the mobile station is unable to exploit the direct link. To simplify the notation, we can assume a large number of cells and make the interference will change from block to block but will be constant over the packet. (We assume no knowledge of \( h \), and thus each interfering term is unlikely to be truly Gaussian, although the sum over many interferers helps in this regard. This assumption is an ideality in order to treat the interference as noise and is made frequently in the literature. Further, the variance of the interference will change from block to block but will be constant over the packet.)

The relay then re-encodes \( s \) into \( x \) with rate \( R_2 \) and transmits \( x \) in the second phase of transmission. The mobile receives

\[
y_M = g x + g_i x_l + v_M - R_2 R_2 \leq \log \left( 1 + \frac{|g|^2 + \sigma^2_i}{\sigma^2_R + \sigma^2_N} \right). \tag{4}
\]

We assume that the normalized durations of two phases of transmission are \( t \) and \( 1 - t \) with \( 0 \leq t \leq 1 \). The capacity of the two-hop transmission is defined as the bottleneck of the two hops with the optimal time sharing as \([40]\)

\[
R = \min_{0 \leq t \leq 1} \{ t R_1, (1 - t) R_2 \}. \tag{5}
\]

Given \( R_1 \) and \( R_2 \), while \( t R_1 \) is an increasing function of \( t \), \( (1 - t) R_2 \) is decreasing with \( t \). The time sharing is thus optimal when the two terms are equal, which results in the optimal time sharing \( t^* = R_2/(R_1 + R_2) \). When using optimal time-sharing, the rate of the two-hop scenario is

\[
r_{\text{OW,DL}} = \frac{R_1 R_2}{R_1 + R_2}. \tag{6}
\]

Here, the subscripts \( \text{OW} \) and \( \text{DL} \) refer to one-way relaying and downlink transmission, respectively. Further, the letter \( r \) is used to refer to the rate of a single user rather than a sum of users.

The rate in (6) is the downlink rate of one user in one sector of the network. In the simulations of Section 7, we will focus on the sum rate over adjacent sectors, which will simply be the sum of (6) over those users. The main assumptions and parameters for the two-way model are given in Table 1.

4. Two-Way Relaying

Consider the cellular network model of Figure 3 where each cell is sectorized, and each sector has a single relay station (RS) serving a single mobile station (MS). There are an arbitrary number of cells in the network, and the base station (BS) in each cell is equipped with one antenna per sector. As in previous sections, we can assume a large number of cells to allow the analysis to focus on one arbitrary sector in one arbitrary cell. The objective then is to transmit the symbol (again dropping the time index as in previous sections) \( s_i \) from the \( i \)th BS to the \( i \)th MS and the symbol \( u_l \) from the
Table 1: System parameters for one-way relay model. The main differences between the one-way relay model and the shared relay are the number of antennas per relay, the relay transmit power, and the number of relays per sector. Since over a large network there will be approximately 3 times as many relays for the one-way model than the shared relay model, they are given 1/3 the transmission power and 1/3 the antennas.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>BS TX power</td>
<td>$P_{BS}$</td>
</tr>
<tr>
<td>Relay TX power</td>
<td>$P_{BS}/3$</td>
</tr>
<tr>
<td>Antennas per BS (sector)</td>
<td>1</td>
</tr>
<tr>
<td>Antennas per relay</td>
<td>1</td>
</tr>
<tr>
<td>Relays per sector</td>
<td>1</td>
</tr>
<tr>
<td>Antennas per mobile</td>
<td>1</td>
</tr>
<tr>
<td>Relay location</td>
<td>2/3 cell radius from BS</td>
</tr>
</tbody>
</table>

In this section we consider the case where the relays are utilized as bidirectional terminals, a configuration also known as two-way relaying. Consider a single physical layer frame in IEEE 802.16j [25]. There are four distinct parts of the frame: (1) the base station transmits in the downlink, then (2) the relay transmits in the downlink, then (3) the mobile transmits in the uplink, and then (4) the relay transmits in the uplink. In two-way relaying this transmission cycle would be cut in half. That is, parts (1) and (3) could take place simultaneously in one segment of the frame, and parts (2) and (4) could take place simultaneously in the rest of the frame. During the first time slot (phase I) all information-generating nodes in the cell (BSs and MSs) transmit their signals to the relay. In the second time slot (phase II), and after proper processing, the RSs broadcast symbols from which the network nodes, that is, BSs and MSs, may extract their intended signals. This two-phase operation is shown in Figure 4.
Phase I. We consider the signals from each relay in the sector since the base station can utilize all antennas in all sectors to decode the uplink. Using Gaussian codebooks, the BSs and MSs transmit $s$ and $u$, respectively. Denote by $\hat{H}$ and $\tilde{G}$ the channels from the base station array and mobile stations to the relays, respectively. The received signal at the relays transmit, and other transceivers are able to cancel the interference they caused in the first phase. Note that the term $\hat{y}_{R,IC}$ has information about the Phase-I signals transmitted in the cell of interest even though it is an interference term. In fact, if the channels to nodes in other cells were estimated, these terms could be canceled. However, we will assume only in-cell channel state information in this paper. Since the base station can cancel the terms that explicitly contain $s$, the uplink sum rate for the whole cell is

$$R_{TW,UL} = \frac{1}{2} \log \left| I + R_{IN}^{-1} H^* \Gamma G^* \Gamma H \right|,$$

where subscript TW denotes two-way relaying, and UL denotes the uplink. The rate for any given user can be computed from this using the multiple access rates as given in Section 5.

For the downlink, the users cannot cooperatively decode, and thus we can compute the rate for the user in the sector of interest. This user will receive

$$y_M = g \hat{y}_R + q_{IS} \hat{y}_{R,JS} + q_{IC} \hat{y}_{R,IC} + v_M,$$

where $q_{IS}$ is the vector channel from the other-sector relays to the user, $q_{IC}$ is the vector from other-cell relays to the user, and $v_M$ is the noise with variance $\sigma^2_v$. Note that we distinguish between the channels between other-cell mobiles and the relays of interest $G_{IC}$, and the channels between other-cell relays and the mobile of interest $q_{IC}$. Note also that $\hat{y}_{R,JS}$ and $\hat{y}_{R,IC}$ have information about both the uplink and downlink signal. In particular, with the proper CSI, the

Figure 4: Two-way relaying operation in a single cell. In the first phase, all transceivers transmit except the relays. In the second phase, only relays transmit, and other transceivers are able to cancel the interference they caused in the first phase.
mobile could cancel its signal from $\hat{y}_{R,IS}$ and similarly use what is available of the downlink signal in these terms to help decode; however, we will not assume this complexity in this paper. The interference variance is then

$$\sigma^2_I = \|q_{IS}\hat{y}_{R,IS}\|^2 + \|q_{IC}\hat{y}_{R,JC}\|^2 + \|g\|^2\|h_I\|^2 + \|g\|^2\|g\|^2,$$

(12)

where $h_I$ is the vector channel of interferers seen by the relay in Phase I (relative to the downlink transmitted symbol $s$), and $g$ is the vector of interferers seen by the relay in Phase I (relative to the uplink transmitted symbol $u$). Thus, the downlink rate for this user is

$$r_{TW,DL} = \frac{1}{2} \log \left( 1 + \frac{|g|h_I|^2}{\sigma^2_I + \sigma^2_N} \right).$$

(13)

We use the notation $r$ instead of $R$ to refer to a single user rather than the sum over users.

The main assumptions and parameters for the two-way model are identical to those for the one-way model and are given in Table 1.

5. Shared Relaying

A shared relay is a relay that is the subordinate of multiple base stations—the base stations share the relay. As discussed in Section 3, IEEE 802.16j does not permit this architecture, but shared relaying has distinct advantages over the one-way model. The relay has $KM$ antennas, where $M$ is the number of base station antennas serving each sector, and $K$ is the number of base stations sharing the relay. For simplicity in our analysis, $M = 1$, but the model is readily extendable to $M > 1$. Figure 5 shows a typical configuration for a shared relay under the general cellular model presented in Section 2. The relay is placed at the corner of three adjacent cells (hence $K = 3$, so that each base station has a sector pointing directly at the shared relay).

By placing many antennas at the shared relay, interference can be canceled in both hops of communication. The shared relay behaves as a coordination of many single-antenna relays and thus alleviates the need for coordination among base stations. As will be shown in Section 7, the shared relay achieves much of the capacity gain of base station coordination without the need for expensive information-passing between distributed base stations.

As in the one-way model, downlink communication occurs in two time slots (since we assume no base station coordination, even among sectors, the uplink analysis is identical to that of the downlink with lower transmit power at the mobile). In the first hop, the relay receives

$$y_R = \sum_{k=1}^{K} h_{k}s_k + h_I s_I + v_R,$$

(14)

where $h_k$ is the channel from the $k$th parent base station to the relay, $s_k$ is the symbol transmitted by the $k$th base station (intended for the $k$th user being served by the shared relay), $H_I$ is the matrix of channel coefficients from interfering base stations, $s_I$ is the vector of symbols transmitted by the interferers, and $v_R$ is spatially white zero-mean additive white Gaussian noise at the relay.

This first hop of communication is the MIMO multiple access channel, and its capacity can be achieved via multiuser detection at the relay. That is, no coordination is necessary among the base stations beyond frame synchronization. Assuming, without loss of generality, that the users are ordered relative to channel SNR (i.e., $\|h_1\| > \|h_2\| > \cdots > \|h_K\|$), we will decode $s_1$ first, and so on, so that $s_K$ is decoded in the midst of interference from only the $(k+1)$ through $K$th streams (and the term $H_{f,S}$ which is common to all streams).

Then the mutual information for user $k$ in the first hop is

$$R_{1k} = \log \left| I + A_k^{-1} R_{1k}^* h_k h_k^* \right|,$$

(15)

where $R_{11} = H_I H_I^* + \sigma^2_M I$ and $A_k$ is defined recursively as

$$A_k = I + A_{k+1}^{-1} R_{1k}^* h_{k+1} h_{k+1}^*,$$

$$A_K = I.$$  

(16)

Now that the relay has decoded the first hop, it can transmit the $\{s_k\}$ to the mobiles in the second hop at a different rate than the first hop. It thus re-encodes the $\{s_k\}$ into another vector $\{x_k\}$ at the highest rate the second hop can support. Note that this is the Gaussian MIMO broadcast channel, and its capacity can be achieved by performing an LQ factorization on the aggregate channel matrix, performing dirty paper coding on the interfering signals, and waterfilling over the signals [41]. The user receives only its signal from the relay, plus interference from the external interferers. This is modeled as

$$y_{M,k} = g_{k} x_k + g_{k}^H_{f,k} y_k + v_{M,k},$$

(17)

where $g_k$ is the effective channel after precoding, waterfilling, and dirty paper coding between the relay and the $k$th mobile station, $g_{f,k}$ is the vector channel from all the interferers to the $k$th mobile, $x_k$ is the transmitted vector at the interferers during the second hop, and $v_{M,k}$ is the additive white Gaussian noise at mobile $k$.

For user $k$ the rate in the second hop is

$$R_{2k} = \log \left( 1 + \frac{|g_k|^2}{\|g_k\|^2 + \sigma^2_N} \right).$$

(18)

As in Section 3, we must optimize the time sharing between the two hops. In this case however, we have to optimize the sum rate and cannot optimize the rate for each user. The sum rate is

$$R_S = \max_{t \in [0,1]} \min_{k=1}^K tR_{1k} + (1-t)R_{2k}.$$  

(19)

Here we use the subscript $S$ to denote shared relaying. The main assumptions and parameters for the shared model are given in Table 2.
6. Base Station Coordination

Base station coordination allows distributed base stations to act as a single multiantenna transmitter by sharing the data to be transmitted via a high-capacity low-delay wired backbone [34]. If all base stations can coordinate their transmissions to all scheduled users, then all interference can be removed. However, full coordination over a wide area is impractical because of the complexity of coordinated transmission, and so localized coordination has been investigated recently [42]. Here, to give an interesting comparison to the shared relay, we allow coordination of sectors pointing at each other at each of the corners of the cells, as shown in Figure 6. No relaying is performed under this architecture. We assume a sum power constraint for all the coordinated antennas. Although this assumption is not practical, the pooled power constraint is a very close approximation to the per-base power constraint, with much lower complexity in calculation [43, 44].

As this channel model is again the Gaussian MIMO broadcast channel, the user rates are similar to those achieved in the second hop of the shared relay transmission in Section 5. Mobile $k$ receives

$$y = h_k s_k + h_{I,k}^* s_I + v_k,$$

(20)

where $h_k$ is the effective channel gain from the base stations to the $k$th mobile after precoding, dirty paper coding, and waterfilling, $s_k$ is the transmitted symbol intended for the $k$th mobile, $h_{I,k}$ is the vector channel from the interferers to the $k$th mobile, $s_I$ is the vector of symbols transmitted by the interferers, and $v_k$ is the additive white Gaussian noise at the $k$th mobile. The rate for user $k$ is thus

$$r_{k,BC} = \log \left( 1 + \frac{|h_k|^2}{|h_{I,k}|^2 |h_{I,k}|^2 + \sigma_k^2} \right).$$

(21)

Here we have used the subscript $BC$ to denote base station coordination and the notation $r$ instead of $R$ to refer to a single user rather than the sum of users. The rate in (21) is the rate of $K$ users in $K$ sectors and is thus directly comparable to (19) assuming that the services areas are the same for the two cases. For the uplink, the rates are that for the MIMO multiple access channel (MIMO MAC), whose forms are identical to those for the downlink but for the proper uplink channel substituted for $h_k$ and the interfering channels [45]. The base station parameters for this model are the same as previous models, and there are no relays included in this model.

**Table 2:** System parameters for shared relay model. The main differences between the shared relay model and the one-way relay are the number of antennas per relay, the relay transmit power, and the number of relays per sector. Since over a large network there will be approximately 3 times fewer relays for the shared model than the one-way relay model, shared relays are given 3 times the transmission power and 3 times the antennas.

<table>
<thead>
<tr>
<th>BS TX power</th>
<th>$P_{BS}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Relay TX power</td>
<td>$P_{RS}$</td>
</tr>
<tr>
<td>Antennas per BS (sector)</td>
<td>1</td>
</tr>
<tr>
<td>Antennas per relay</td>
<td>3</td>
</tr>
<tr>
<td>Relays per sector</td>
<td>1</td>
</tr>
<tr>
<td>Antennas per mobile</td>
<td>1</td>
</tr>
<tr>
<td>Relay location</td>
<td>cell radius from BS</td>
</tr>
</tbody>
</table>

**Figure 5:** Models of systems using shared relays with (a) frequency reuse factor of 6 or (b) frequency reuse factor of 1.
7. Simulations

Each of the systems described in the previous four sections was tested under a system-level cellular network simulation. A layer of interfering cells was wrapped around the three main cells, as shown in Figure 7. These outer cells have the same architecture as the inner cells for the respective simulations. For instance, a network implementing the shared relay will contain a relay at each vertex of each hexagonal cell, as in Figure 7. Since the sectors making up the central triangle are our area of interest, there are actually two layers of interfering relays in this case.

The metric of comparison is the achievable sum rate (derived in each architecture’s respective section) in the central triangle outlined in Figure 7. That is, the sum rate is the rate of the three users in the three sectors making up the central triangle in Figure 7, averaged over a number of fading and shadowing iterations. Since we have assumed arbitrary scheduling and orthogonal signaling inside each sector (corresponding to a single subchannel of the OFDM waveform), the sum rate is calculated over three users. The parameters of the simulation are given in Table 3.

Table 3: System parameters used for the simulations in this paper.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>BS TX power</td>
<td>47 dBm</td>
</tr>
<tr>
<td>BS-RS channel model</td>
<td>IEEE 802.16j, Type H [33]</td>
</tr>
<tr>
<td>BS-MS channel model</td>
<td>IEEE 802.16j, Type E [33]</td>
</tr>
<tr>
<td>RS-MS channel model</td>
<td>IEEE 802.16j, Type E [33]</td>
</tr>
<tr>
<td>Number of Realizations</td>
<td>1000</td>
</tr>
<tr>
<td>Cell radius</td>
<td>876 m</td>
</tr>
<tr>
<td>Carrier frequency</td>
<td>2 GHz</td>
</tr>
<tr>
<td>Noise power</td>
<td>−144 dBW</td>
</tr>
<tr>
<td>Mobile height</td>
<td>1 m</td>
</tr>
<tr>
<td>Relay height</td>
<td>15 m</td>
</tr>
<tr>
<td>BS height</td>
<td>30 m</td>
</tr>
<tr>
<td>Propagation environment</td>
<td>Urban</td>
</tr>
</tbody>
</table>
The Type H channel model specifies a channel from a node transmitting from above the rooftop to another node above the rooftop. The fading is Rician with K-factor 4, the carrier frequency is 2 GHz, there is no shadowing, the relay height is 15 m, and the base station height is 30 m. For the Type E channel model, for the BS-MS and RS-MS links, the mobile is located 1 m above the ground, the street width is 12 m, the roof height is 15 m, and the distance between building centers is 60 m (based on an urban environment). The noise power is $-144$ dBW, corresponding to a 10 MHz channel.

Figure 8 shows the downlink sum rate for each of the architectures presented in this paper as a function of relay transmit power for reuse factors $r = 1, 6$. For each case, $r = 1$ outperforms $r = 6$ to varying degree. Base station coordination and conventional transmission are constant across the plot because no relays are included in these system models.

Base station coordination, unsurprisingly, gives the highest downlink sum rates, a roughly 119% increase over a conventional architecture with no relaying or coordination. More striking, however, is that shared relaying achieves approximately 60% of the gains of base station coordination. When comparing the two systems, it must be emphasized that shared relaying requires no coordination between its base stations beyond that needed for synchronization in the multiple access channel of the first hop. Its main disadvantage relative to coordination is the half-duplex loss and delay associated with decode-and-forward relaying. Note that for $r = 6$ the gains of shared relaying diminish relative to $r = 1$.

The one-way architecture only gives a roughly 15% increase in rate relative to a conventional system, whereas two-way relaying performs worse than conventional in the regime plotted in Figure 8. Here, the multiplexing gain of the two-way relay is not apparent because we are considering only the downlink.

Uplink sum rates are given in Figure 9. In this regime, conventional architectures (without power control, soft handoff, or multiuser diversity which have been abstracted out of the system) have extremely low uplink SINR, resulting in almost no rate. Two-way relaying performs similarly since the interference from nearby base stations is overwhelming the mobile device’s signal unless the relay is extremely close to it (as will be discussed in the next section). The curves on this graph are flat partly because they are already in the interference-limited regime and partly because, in the case of relaying, the system is limited by the first hop, which is not a function of the relay transmit power.

In this regime, shared relaying achieves around 90% of the achievable rate of base station coordination due to the relay’s ability to remove interference and its proximity to the cell edge. The half-duplex loss is much less severe in this case. One-way relaying achieves roughly 50% of the rates of base station coordination. As in the downlink case, frequency use factor $r = 1$ drastically outperforms $r = 6$ across the board.

Figure 10 shows the downlink sum rate of coordination, shared relaying, and a conventional system with no relaying or coordination throughout an entire sector. The figure is for frequency reuse factor 6 because the curves are more separated in this case. At around half-way between the base station and shared relay (which is located at the left-most corner of the sector), direct transmission becomes more desirable than relaying. By adapting between these two cases based on the position of the mobile station, the downlink rate...
The simulations of the this section give relative performance gains between different transmission strategies in a cellular network. This section describes the insight these simulations can give and summarizes the general conclusions we can draw from them beyond the relative performances. First, having a relay act as an interference-reducing station gets nearly the gains of having BS coordination over the same area. The reason this is not obvious is because of the half-duplex nature of the relay. This is made up for by the fact that the relay can be placed in an LOS position with the BS and is closer to the MS than the BS in the regime of interest. In more precise terms, the degrees of freedom lost in performing half-duplex relaying are almost made up for by practical considerations such as RS placement, all at a reduced complexity. The second conclusion we can draw is that two-way relaying is severely limited in the uplink unless the relay is extremely close to the mobile and does not in general compensate for the half-duplex loss of one-way relaying in the simulated regime. We will discuss practical ways of overcoming this problem in the next section.

8. Discussion

In the previous section, shared relaying was shown to be a simpler alternative to base station coordination. Further, by spatially removing local interference, the shared relay outperforms one-way relaying by over 80% in the downlink. By allowing the relay to be shared among multiple base stations, the shared relay avoids the BS coordination task of associating each mobile station with multiple base stations. We now briefly discuss some practical considerations for shared relaying.

8.1. Practical Shared Relaying. We have been assuming thus far that the shared relay is moderately complex. Since it serves 3 adjacent sectors, there will be 1/3 as many relays in the network than with the one-way model (neglecting the edge of the network). Thus, an increase in unit complexity is at least partially offset by a decrease in deployment cost relative to the one-way model.

The shared relay may also mitigate the need for coordinated scheduling between the sectors. If the shared relay is allowed to transmit its own control information, as in the nontransparent relay of IEEE 802.16j [25], it can achieve a large multiuser diversity gain across sectors without the need for the base stations to share information.

It may also make handoff easier by allowing for a buffer zone where which base station a mobile is associated with is unimportant. For example, consider a mobile station moving away from a base station and toward a shared relay. As it enters the relay’s zone of service, it is now served by this relay but still associated with its original base station. As it continues past the relay and into the next cell, it is still served by the shared relay, which may signal to the original base station that it is time to handoff the mobile to the adjacent BS. So long as the handoff procedure is done before the mobile leaves the shared relay’s zone of service, the mobile will stay connected to the network.

8.2. Improving Two-Way Relaying. Recall that Figure 9 showed that uplink rates for two-way relaying were practically zero. In this scenario, since the base stations and mobile stations are transmitting simultaneously, nearby base stations are drowning out the mobile stations. This can be mitigated by only performing two-way relaying for mobiles that are very near the relay. Figure 11 shows the uplink sum rate for various transmission strategies as a function of the mobile station distance from the base station. Conversely, Figure 12 shows the downlink sum rate for the
in a mobile broadband cellular network, the uplink and downlink are inherently asymmetric, making this sum an inappropriate metric. For instance, to truly maximize the uplink plus downlink rate, one will simply allow the downlink to occur all the time.

Further, allowing adjacent base stations and mobile stations to transmit simultaneously is an inherently bad idea unless the receiver is located very close to the mobile. For example, if we allow the mobile to transmit at 23 dB below the base station power, and using simple free-space path loss, the relay would have to be approximately 36 times closer to the mobile than the nearest out-of-cell base station for a 0 dB SINR. Of course, this is a simple calculation intended only to show the nature of the problem.

One way of combating this is to use an antenna array at the relay to steer nulls toward the nearest base stations. This risks a mobile being in the same direction as the base station and being in the same null. Other strategies include conventional ways of avoiding interference in cellular systems such as power control and frequency reuse.

9. Conclusions and Future Work

We have analyzed and compared four cellular architectures for LTE-Advanced. While base station coordination between adjacent sectors in neighboring cells achieved the highest rates, it is also the most complex architecture. Sharing a multiantenna relay among the same sectors is a simpler way to achieve much of the gains of local interference mitigation but still has significant complexity within the relay itself. One-way relaying, where each relay is associated with only one base station, is unlikely to give substantial throughput gains near the cell edge because it does not directly treat interference, and two-way relaying overcomes the half-duplex loss of conventional relaying provided that the relay is extremely close to the mobile.

Future work will focus on more detailed design of shared relays, including scheduling, feedback, and dealing with mobility. Two-way relaying requires research for interference mitigation in the uplink. Finally, combining base station coordination and relaying is an emerging area that will be the subject of future research [46–50].

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References


Preliminary call for papers

The 2011 European Signal Processing Conference (EUSIPCO-2011) is the nineteenth in a series of conferences promoted by the European Association for Signal Processing (EURASIP, www.eurasip.org). This year edition will take place in Barcelona, capital city of Catalonia (Spain), and will be jointly organized by the Centre Tecnològic de Telecomunicacions de Catalunya (CTTC) and the Universitat Politècnica de Catalunya (UPC).

EUSIPCO-2011 will focus on key aspects of signal processing theory and applications as listed below. Acceptance of submissions will be based on quality, relevance and originality. Accepted papers will be published in the EUSIPCO proceedings and presented during the conference. Paper submissions, proposals for tutorials and proposals for special sessions are invited in, but not limited to, the following areas of interest.

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