

# VOLA: A Compact Volumetric Format for 3D Mapping and Embedded Systems

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Abstract:

The Volumetric Accelerator (VOLA) format is a compact data structure that unifies computer vision and 3D rendering and allows for the rapid calculation of connected components, per-voxel census/accounting, Deep Learning and Convolutional Neural Network (CNN) inference, path planning and obstacle avoidance. Using a hierarchical bit array format allows it to run efficiently on embedded systems and maximize the level of data compression for network transmission. The proposed format allows massive scale volumetric data to be used in embedded applications where it would be inconceivable to utilize point-clouds due to memory constraints. Furthermore, geographical and qualitative data is embedded in the file structure to allow it to be used in place of standard point cloud formats. This work examines the reduction in file size when encoding 3D data using the VOLA format. Four real world Light Detection and Ranging (LiDAR) datasets are converted and produced data an order of magnitude smaller than the current binary standard for point cloud data. Additionally, a new metric based on a neighborhood lookup is developed that measures an accurate resolution for a point cloud dataset.

## 1 Introduction

The worlds of computer vision and graphics, although separate, are slowly being merged in the field of robotics. Computer vision is taking input from systems, such as Light Detection and Ranging (LiDAR), structured light or camera systems and generating point clouds or depth maps of the environment. The data must then be represented internally for the environment to be interpreted correctly. Unfortunately the amount of data generated by modern sensors quickly becomes too large for embedded systems. An example of the amount of memory required by dense representations is SLAMbench (Nardi et al., 2015) (kFusion) which requires 512 MiB to represent a 5m<sup>3</sup> volume with 1 cm accuracy (Mutto et al., 2012). A terrestrial LiDAR scanner generates a million unique points per second (Geosystems, 2015) and an hour long aerial survey can generate upwards of a billion unique points.

The result of having such vast quantities of data is that it quickly becomes impossible to

process, let alone visualize the data on all but the most powerful systems. Consequently it is rarely used directly. It is simplified by decimation, flattened into a 2.5D Digital Elevation Model (DEM), or meshed using a technique such as Delaunay triangulation or Poisson reconstruction. The original intention of VOLA was to develop a format that was small enough to be stored on an embedded system and enable it to process 3D data as an internalized model. The model could then be easily and rapidly queried for navigation of the environment as it partitions space based on its occupancy. This paper focuses on the compression rates using the format on different datasets.

Four publicly available large scale LiDAR datasets were examined in this work. The data was obtained by an aerial LiDAR system for San Francisco, New York state, Montreal and Dublin respectively. Although the quality and resolution of the data varies, they present a realistic representation of what would be processed by an embedded system in the real world, except on a

much larger scale. This work examines the effect of point density versus compression depth on the data for both dense and sparse mappings and then compares the VOLA format against the original dataset. Our findings show that there are dramatic reductions in file size with a minimal loss of information. Another finding of this work is that average point cloud density is a poor metric for choosing a resolution for the voxel model as it can be biased by the underlying clusters in the data distribution. An efficient and easily calculated metric based on block occupancy is presented that takes into account the voxel neighborhood when choosing a resolution.

## 2 Related Research

There exist several techniques for organizing point cloud data and converting it to a solid geometry. Point clouds are essentially a list of coordinates, with each line containing positional information as well as color, intensity, number of returns and other attributes. Although the list can be sorted using the coordinate values, normally a spatial partitioning algorithm is applied to facilitate searching and sorting the data. Commonly used approaches are the octree (Meagher, 1982) and the KD-Tree (Bentley, 1975).

Octrees are based in three dimensional space and so they naturally lend themselves to 3D visualization. There are examples where the octree itself is used for visualizing 3D data, such as the Octomap (Hornung et al., 2013). Octrees are normally composed of pointers to locations in memory which makes it difficult to save the structure as a binary. One notable exception is the DMGoctree (Girardeau-Montaut, 2006) which uses a binary encoding for the position of the point in the octree. Three bits are used as a unique identifier for each level of the octree. The DMGoctree uses a 32 or 64 bit encoding for each point to indicate the location in the tree to a depth of 10 or 20 respectively.

Another recent development is Octnet (Riegler et al., 2016). Their work uses a hybrid grid octree to enable sparsification of voxel data. A binary format is used for representing a set of shallow octrees that, while not as memory efficient as a standard octree still allows for significant compression. Furthermore they developed a highly efficient convolution operator that reduced the number of multiplications and allowed for faster network operations when

carrying out 3D inference.

Another technique for solidifying and simplifying a point cloud is to generate a surface that encloses the points. A commonly used approach that locally fits triangles to a set of points is Delaunay triangulation (Boissonnat, 1984). It maximizes the minimum angle for all angles in the triangulation. Triangular Irregular Networks (TIN) (Peucker et al., 1978) are extensively used in Geographical Information Systems (GIS) and are based on Delaunay triangulation. One issue is that the approach noise and overlapping points can cause the algorithm to make spurious surfaces.

A more modern and accurate meshing algorithm is Poisson surface reconstruction (Kazhdan et al., 2006). The space is hierarchically partitioned and information on the orientation of the points is used to generate a 3D model. It has been shown to generate accurate models and it is able to handle noise due to the combination of global and local point information. Poisson reconstruction will always output a watertight mesh but this can be problematic when there are gaps in the data. In an attempt to fill areas with little information, assumptions are made about the shape which can lead to significant distortions. There are also problems with small, pointed surface features which tend to be rounded off or removed by the meshing algorithm.

Finally there are volumetric techniques encoding point clouds. Traditionally used for rasterizing 3D data for rendering (Hughes et al., 2014), the data is fitted to a 3D grid and occupancy of a point is represented using a volumetric element, or “voxel”. Voxels allow the data to be quickly searched and traversed due to being fitted to a grid. While it simplifies the data and may merge many points into a single voxel, each point will have a representative voxel. Unlike meshing algorithms, voxels will not leave out features but conversely may be more sensitive to noise. The primary issue with voxel representations is that they encode for everything, including open space. This means that as the resolution is increased or the area covered is doubled then the memory requirements increase by a factor of 8. An investigation into using sparse voxel approaches to accomplish efficient rendering of large volumetric objects was carried out by (Laine and Karras, 2011). The work used sparse voxel octrees and mipmaps in conjunction with frustrum culling to render volumetric scenes in real time. This work was further developed under the name Gi-

	VOLA	octree
Implementation	Bit Sequence	Pointer Based
Traversal Arithmetic	Modular	Pointer
Variable Depth	Yes	Yes
Dense Search Complexity	$O(1)$	$O(h)$
Sparse search complexity	$O(h)$	$O(h)$
Embedded System Support	Yes	No
Look Up Table (LUT) Support	Yes	No
Easily Save to File	Yes	No
File Structure	Implicit	Explicit
Cacheable	Yes	No
Hierarchical Memory Structure	No	Yes

Table 1: A comparison between VOLA and octrees.

gavoxel (Crassin et al., 2009).

VOLA combines the hierarchical structure of octrees with traditional volumetric approaches, enabling it to only encode for occupied voxels. Although there is much similarity with traditional octrees this approach has several noticeable differences outlined in Table 1. The approach is described in detail below.

### 3 The VOLA Format

VOLA is unique in that it combines the benefits of partitioning algorithms with a minimal voxel format. It hierarchically encodes 3D data using modular arithmetic and bit counting operations applied to a bit array. The simplicity of this approach means that it is highly compact and can be run on hardware with simple instruction sets. The choice of a 64 bit integer as the minimum unit of computation means that modern processor operations are already optimized to handle the format. While octree formats either need to be fully dense to be serialized or require bespoke serialization code for sparse data, the VOLA bit array is immediately readable without header information.

VOLA is built on the concept of hierarchically defining occupied space using “one bit per voxel” within a standard unsigned 64 bit integer. The one-dimensional bit array that makes up the integer value is mapped to three-dimensional space using modular arithmetic. The bounding box containing the points is divided into 64 cells. If there are points contained within a cell the bit is then set to 1 otherwise it is set to zero. The result of the first division is shown in Figure 1.

For the next level each occupied cell is assigned an additional 64 bit integer and the space is further subdivided into 64 cells. Any unoccupied cells on the upper levels are ignored allowing each 64 bit integer to only encode for occupied space. The bits are again set based on occupancy

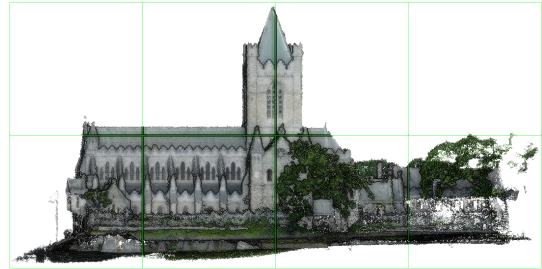
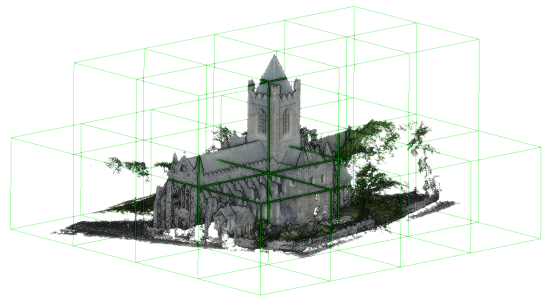


Figure 1: Tree depth one, the space is subdivided into 64 cells. The occupied cells are shown in green.

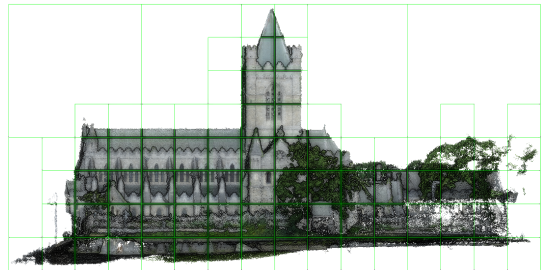
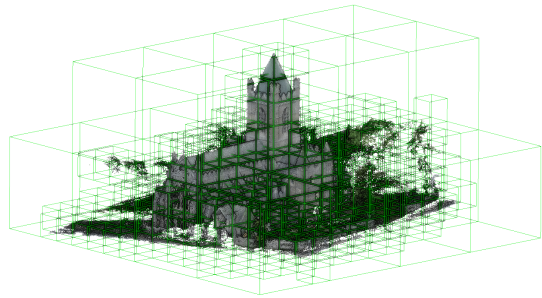


Figure 2: Tree depth two. Each occupied cell is subdivided into 64 smaller cells.

and appended to the bit array. The number of integers in each level can be computed by summing the number of occupied bits in the previous level. The resolution increases fourfold for each additional level as shown in figure 2

The process is repeated with each level increasing the resolution of the representation by four until a resolution suitable for the data is reached. This depends on the resolution of the

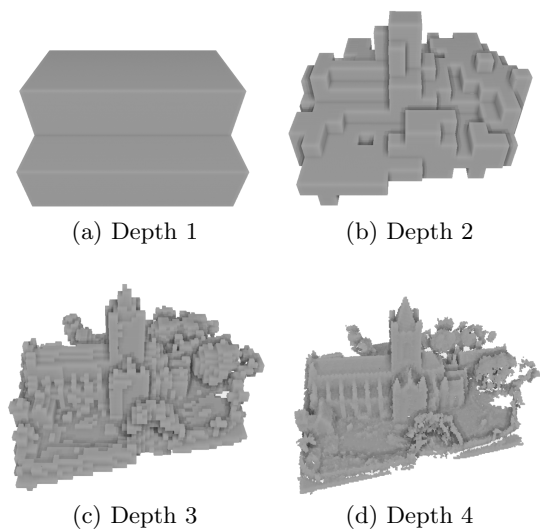


Figure 3: The output obtained for different tree depths. The resolution increases by 4 for each axis on every successive subdivision.

data itself. The traditional approach used is to compute the average points per meter of the dataset and use this to compute a suitable tree depth. One of the issues raised in this work is that the non-uniform distribution of points makes this a poor metric. A new approach that approximates voxel neighborhood is found to more accurately reflect the dataset is discussed in Section 7.

## 4 Aerial LiDAR Datasets

Real world data obtained from aerial LiDAR scans is used in this work as it analogous to point cloud data that would be obtained from an embedded system used for 3D navigation, such as in a drone or a self driving car. The four datasets examined in this work are:

- The 2010 ARRA LiDAR Golden Gate Survey ([san](#), )
- The 2013-2014 U.S. Geological Survey CMGP LiDAR: Post Sandy ([new](#), )
- The Montreal 2012 LiDAR Aerien Survey ([mon](#), [a](#))
- The ALS 2015 Dublin survey ([Laefer et al.](#), )

The datasets were chosen as they model complex built up urban environments and they are publicly available open data ([sfl](#), ; [nyl](#), ; [mon](#), [b](#); [dub](#), ). The density of the point clouds varies significantly between the datasets due to the flight

paths used to gather the LiDAR data. Traditional GIS applications are only concerned with generating Digital Elevation Models which only requires a single height value per grid point. Accordingly the amount of overlap between flight paths was reduced to cover the maximum area in the least time and the resulting models are sparse. The San Francisco, Montreal and New York datasets followed this approach and so have a low point density. The San Francisco dataset proving to be the sparsest at 0.2 points per meter, followed by New York with 1.5 points per meter and Montreal with 8 points per meter, as shown in Figures 4, 5, and 6. The Dublin dataset was gathered by the Urban Modelling group which research techniques for maximizing 3D data and model generation ([Truong-Hong et al.](#), 2013). They used up to 60% overlap in order to increase the point density to 190 points per meter. The data was captured at an altitude of 300m using a TopEye system S/N 443. It consists over 600 million points with an average point density of  $348.43 \text{ points/m}^2$ . It covered an area of  $2 \text{ km}^2$  in Dublin city center.

One issue that is obvious with the datasets is that point distribution is not uniform. Aerial LiDAR scans are inherently biased due to the angle and height at which the data is gathered. This is clearly highlighted in Figures 6 and 7 where the roofs are bright green and red, representing a higher point density. There are more point returns generated by higher flatter surfaces, such as the roofs of buildings, rather than occluded street level structures. The average point density does not give an accurate representation of the underlying data which is necessary for choosing the correct level of subdivision when voxelizing the dataset.

Our experiments show that the block occupancy, which is analogous to a voxel neighborhood, gives a more realistic metric of the point density by finding the level of subdivision where the voxels become separated due to insufficient point density. The metric will be explained in more detail in the Section 7.

## 5 Experiments

Two experiments are carried out in this work. The first experiment examines the difference between a traditional dense mapping of the space using a 1 bit per voxel representation versus the hierarchical sparse mapping used by VOLA. The



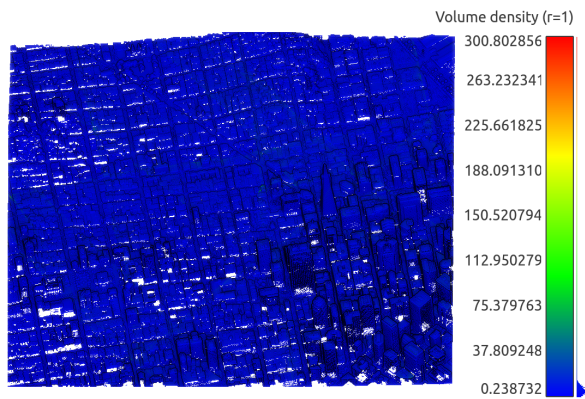


Figure 4: San Francisco LiDAR scan density. The points are uniformly distributed with an average density is 0.2 points per meter.

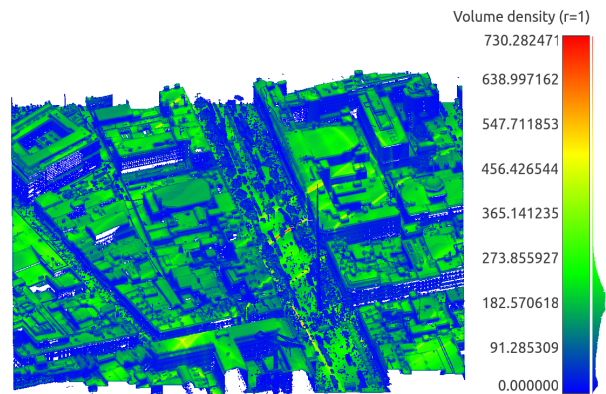


Figure 7: The Dublin LiDAR scan density is 190 points per meter and the distribution towards the rooftops is clearly visible.

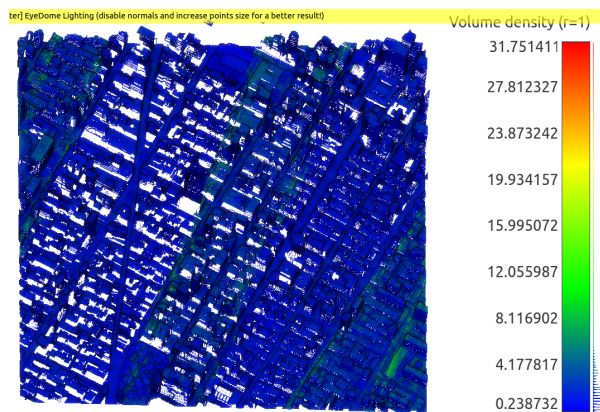


Figure 5: The New York LiDAR scan is uniform and of higher density (1.5 points per meter) than the San Francisco scan but is missing the facades on the buildings.

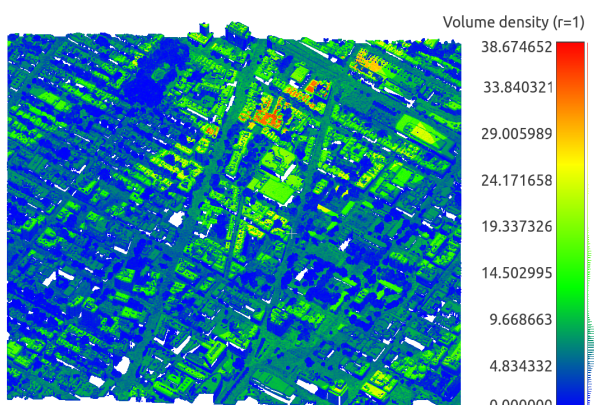


Figure 6: The Montreal LiDAR scan density is 8 points per meter and starts to show a non uniform distribution. The rooftops and overlapping scan lines show up in green and orange respectively.

second experiment compares standard and compressed VOLA to the industry standard for point cloud compression, the LAZ format.

### 5.1 Comparison of dense versus sparse mapping

VOLA combines a 1 bit per voxel representation with a hierarchical encoding. Rather than using 32 bit integer to represent a voxel as in standard approaches, the occupancy of each voxel is indicated by setting a bit to 1. This encoding step alone will make the file size 32 times smaller. What is unclear is the magnitude of reduction in file size results from a hierarchical compression. The worst case scenario, where the points uniformly throughout the bounding box, would result in dense and sparse volumes being of equal size. The experiment measures the size reduction produced by hierarchically encoding real world data. As both dense and sparse representations use one bit per voxel, the one variable effecting file size is that the sparse representation may omit empty space.

The sparse mapping discards any 64 blocks that exclusively contain zeros. This means that empty space is not encoded for but it adds an additional overhead in processing time when packing and unpacking the structure. Theoretically the worst case for a sparse mapping, where points are uniformly distributed throughout the space, would result in the dense mapping and sparse mapping having equal size. Fortunately points clouds based on real world data generally have non-uniform distributions with most point clouds consisting of empty space. (Klingensmith et al., 2015) found that only 7% of the space in a typical

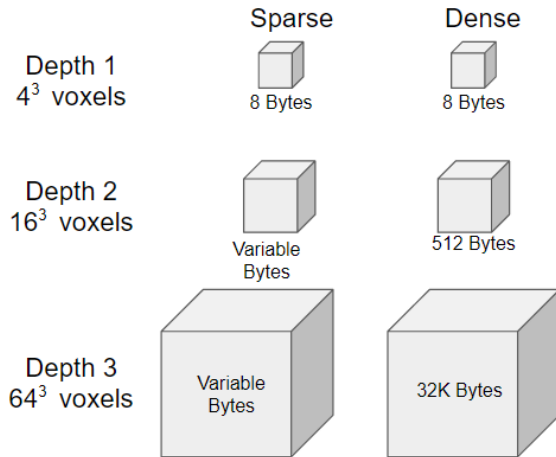


Figure 8: Sparse versus Dense Encoding.

indoor scene is in fact occupied. The density of the Dublin LiDAR scan, for example, has an average occupancy of 1.36% per 100 meter tile. This work examines the levels of compression obtained when converting a point cloud to both dense and sparse representations and how this is effected by the depth.

## 5.2 Comparison with LAS File Format

The VOLA format is compared to commonly used industry standard for LiDAR data, the LAS file format. LAS is a binary format originally released by the American Society of Photogrammetry and Remote Sensing (ASPRS) for exchanging point cloud data. LAS was designed as an alternative to proprietary formats or the commonly used generic ASCII format. It has the ability to embed information on the dataset and the points themselves, such as coordinate reference system, number of returns, scan angle, etc. An addition to this format is the compressed LAZ format developed by (Isenburg, 2013). It is a lossless format that takes advantage of the fact that LAS stores the coordinates using a fixed point format to compress the data. The resulting files are between 7% and 25% of the original size. LAZ is now become the de facto standard for point cloud formats.

The comparison with VOLA has two caveats: firstly, converting a point cloud to a voxel format will implicitly simplify the distribution to a binary grid distribution. A voxel is placed in the grid if there is at least 1 point in the grid location. A voxel could result from a single point or 1000

points and so information on high point concentrations is lost. The result is that the conversion to a voxel format is lossy.

The second consideration is that the LiDAR format contains meta-data about the points themselves, such as color, intensity, number of returns, scan angle, etc. Using 1 bit per voxel VOLA means that only the occupancy is recorded. In order to carry out a fairer comparison, 2 Bits per voxel VOLA is used to represent the point meta-data. The meta-data is encoded in byte blocks which means the resolution of the values is reduced from 32 bits to 8 bits but as much of this data is normally limited to this range (intensity, number of returns) then there is no loss of information. There is data loss on the resolution of the data as 2 bits per voxel records the information for a 64 bit occupancy block rather than the individual voxels.

In order to compare point cloud compression with VOLA compression we used a standard compression algorithm on the VOLA format. While VOLA is compact it is not compressed and so there is still significant room for further file size reduction, whereas the LAZ cannot be reduced further. The standard gzip (Deutsch and Gailly, 1996) library was used to compress the files. Gzip uses the deflate algorithm for compression (Deutsch, 1996). The resolution of the data used in this comparison was chosen by the occupancy as calculated in the dense versus sparse experiments. A resolution was chosen where the average block occupancy is above 15% which means that there is a increased likelihood that the voxels are connected.

## 6 Dense Versus Sparse Comparison Results

Each dataset was computed to multiple depths (and therefore resolutions) in order to understand how the file size compression was effected by the resolution. The file size in megabytes was recorded for both the dense and sparse representation. The improvement in compression was computed by dividing the dense file size by the sparse file size. An additional measure of occupancy was computed by summing the bits in each 64 bit block in the sparse representation. This does not give the actual neighborhood of a voxel, e.g., a neighboring voxel could be contained in an adjoining block, it does give an approximate measure of occupancy.

The results for the San Francisco dataset are shown in Table 2. Although this is the least dense dataset it contains the largest number of tiles. The magnitude reduction increases as the depth (and accordingly resolution) increases. The maximum compression is 38 times smaller than the dense representation.

The initial occupancy is 46% at depth 1 which then increases at depth 2 before decreasing again. This is because the majority of bounding box is empty space with most of the points having low height values.

It is also noted at depth 4 that the initial occupancy of the voxel blocks falls below 10%. Each voxel in a block can have up to 26 neighboring voxels of which 6 can be contiguous, i.e., sharing a common face. As the occupancy drops the likelihood of contiguity also decreases. This is covered in more detail in Section 7.

Lvl	Dense(MB)	Sparse(MB)	Mag Red	Block Occup
1	1.87	1.87	1	46.77%
2	122.14	40.2	3.04	51.93%
3	7818.92	881.3	8.87	29.70%
4	500412.66	12918.8	38.74	7.3%

Table 2: Depth results for San Francisco dataset for 234887 tiles.

The New York dataset in Table 3 shows a similar reduction in file size for increasing depth with a similar magnitude reduction for depth 4. There is also the same increase in block occupancy at depth 2 before it decreases and is less than 10% at depth 4.

Lvl	Dense(MB)	Sparse(MB)	Mag Red	Block Occup
1	0.694	0.694	1	39.15%
2	45.138	13.197	3.42	60.42%
3	2889.53	318.82	9.06	31.25%
4	184930.71	4858.55	38.06	9.62%

Table 3: Depth results for New York dataset for 86804 tiles.

The Montreal dataset results in Table 4 shows a slightly more pronounced reduction in file size initially but is only 34 times smaller by depth 4. The occupancy again spikes at depth 2 and reaches 15% at depth 4. This would imply that more detailed features are captured in the higher resolution.

The Dublin dataset results are shown in Table 5. Due to the significantly higher point density it was decided to increase the maximum depth to 5. This is equivalent to each voxel representing a 9.7cm<sup>3</sup> cube in the dataset. There is

Lvl	Dense(MB)	Sparse(MB)	Mag Red	Block Occup
1	0.53	0.53	1	35.62%
2	34.47	9.44	3.65	62.52%
3	2206.96	233.08	9.47	37.97%
4	141246.04	4106.08	34.4	15.62%

Table 4: Depth results for Montreal dataset for 66299 tiles.

a smaller reduction in the file size for successive depths compared to the previous datasets but this increases to 70 times smaller at depth 5. The occupancy spikes at 87% at depth 2 and then drops off to a minimum of 14.72%.

Lvl	Dense(MB)	Sparse(MB)	Mag Red	Block Occup
1	0.0028	0.0028	1	52.5%
2	0.185	0.065	2.82	87.14%
3	11.85	1.96	6.05	48.33%
4	758.43	40.84	18.57	35.46%
5	48539.947	684.36	70.93	14.72%

Table 5: Depth results for Dublin dataset for 356 tiles

## 6.1 Discussion

As stated earlier, if the data was distributed uniformly throughout the bounding box this would result in dense and sparse volumes being of equal size. The experiments show that this is not the case with real world data. There is an initial low occupancy for the highest level encoding as the majority of points in each 100m<sup>3</sup> tile are in the lowest third on the vertical axis. Once this has been removed the remaining space is largely occupied but then decreases for each successive increase in resolution.

The magnitude of the reduction decreased for more dense datasets but this was offset by a marked increase in the magnitude of reduction for greater depths. Although higher resolution datasets require higher resolution VOLA models, increasing the resolution of sparse models increased the magnitude of the space saving.

There was also a point with all the datasets where the resolution increased to the point that the voxels were no longer connected. The result is a voxel representation where the number of voxels is the same as the number of points (which is essentially a lossless encoding of the data) but is not useful when computing collisions and navigation information. We shall go into more detail on this in the next section.



## 7 Block Occupancy

Increasing the resolution resulted in greater number of the points being disconnected. Although this means that it more accurately represents the underlying point cloud, it is less useful when using the representation for navigation or using machine learning on the dataset. For example, analyzing a building facade or detecting buildings using a 3D CNN require that the data be connected into a contiguous object.

The true neighborhood of a voxel is difficult to compute when using a hierarchical encoding as it requires finding neighboring blocks when a voxel is on the edge of the current block. An alternative approach is to conduct a bitwise comparison on the voxels or to compute Euclidean distance between the voxels in a block and ignore neighboring blocks. This simplifies the problem but it is still computationally expensive due to the number of comparisons required.

A more efficient although less accurate approach is to compute the occupancy of a block, as was used in the previous experiments. The occupancy of a 64 bit block is computed by summing the bits set to one. This is not the true is only an approximation of neighborhood but it does give a clear probability of the connected components in a block. A comparison of the occupancy and its relationship with the number of connected components is shown in Table 6 and is found to closely approximate to the number of connections per block.

Occup	Contig Vox	StdDev	Connected
100%	144	0	100%
75%	80.44	3.23	55.8%
50%	35.31	3.38	24.5%
25%	8.58	2.28	5.9%
10%	1.49	1.09	0.75%

Table 6: A comparison of occupancy and the number of connected voxels within a block.

The point density is traditionally used when working out the suitable resolution for a voxelised model but this approach oversimplifies the distribution of the data. It assumes the points have a uniform density although the points tend to be biased towards areas least occluded from the scanner, e.g., aerial LiDAR data has many more times the points at the rooftops than on ground level. It also takes no account for the spread of points, i.e., points may cover a building consistently but only sparsely. Ignoring this worst case

resolution will result in fragmented voxel models. Although block occupancy may be an imperfect metric, it is easy to compute and correlates well with block contiguity. As such it provides a useful mechanism when determining what is a sufficient resolution when processing a dataset.

## 8 LAS Format Comparison Results

The VOLA format is compared against the Laszip format using a two bits per voxel representation. This allows for the meta-data about the points to be encoded. The caveats are that VOLA is not a lossless format and the resolution of the point information is reduced due to the hierarchical encoding. The point information is averaged over each 64 bit block. There is then a comparison against VOLA when compressed using a gzip, a generic compression library. The depth chosen for the data was based on the previous results where the voxels are still connected. The San Francisco, New York and Montreal datasets are at depth 3 and the Dublin dataset is at depth 4. The VOLA format now allows for an arbitrary amount of additional information to be appended to the structure, although only 2 bits are used in this example.

Dataset	LAS	LAZ	%	VOLA	%	VOLAZip	%
San Fran	224GB	33GB	14.7%	1.76GB	0.76%	799MB	0.35%
New York	126GB	22GB	17.4%	637MB	0.5%	336MB	0.26%
Montreal	167GB	27.7GB	16.5%	466MB	0.27%	189	0.11%
Dublin	36GB	3.7GB	10.27%	81.68MB	0.22%	33MB	0.091%

Table 7: A comparison of the file size reduction when using LAZ and VOLA.

The results show that VOLA can reduce the file size on the datasets to less than 1% their original size. VOLA compressed using generic methods further reduces this by up to 50%. Although LAZ offers significant lossless compression, compressed VOLA reduces the file sizes to less than 5% of the LAZ files.

## 9 Conclusions

In this work we showed that encoding real-world data using the hierarchical VOLA encoding massively reduces the file size. We also introduce a metric based on voxel block occupancy that more accurately reflects the underlying point cloud distribution than average point density. Although it is only an approximation of neighbor-



hood it is easily calculated using VOLA's block format.

We then compared the VOLA representation with point meta-data with standard LiDAR formats. The reduction of the file size when compared with the LAS format less than 1%, albeit at the loss of some resolution and point information. Using a generic compression algorithm on VOLA results in it being 5% of the file size of the compressed LAZ format.

Due to the inherent sparsity of real-world data, a hierarchical encoding that omits empty space makes sense. These results show that it is possible to store large amounts of 3D data in a memory footprint that could easily be accommodated on an embedded system for both mapping and machine learning applications.

## 10 Future work

A generic compression algorithm was used to compress the data. This could be improved using bespoke techniques developed for the underlying 3D data such as run length encoding and look up tables for self similar features. Our intention is to use such techniques to further reduce the file size.

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