

Seepage channel development in the crown pillar: Insights from induced microseismicity

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Abstract:

The stability of crown pillar is critical during the transition from open pit to underground mining. Mining-induced fractures in the pillar form water seepage channels, which can cause potential water inrush hazards. A microseismicity-based method to establish seepage channel network and assess damage state of rock mass in the pillar is proposed. The formation processes of seepage channels and associated rock failure mechanism were analyzed. First, the spatiotemporal evolution of the microseismic (MS) events was presented, based on which the development process of the fractured zone was determined. Second, moment tensor inversion (MTI) was utilized to interpret the focal mechanism of the MS events. A 3D rose diagram was utilized to measure the fracture orientations and determine the main fracture surfaces, and a fracture network was subsequently established. Meanwhile, the distribution characteristics of the fracture radii and volumes were discussed. The results show that shear fractures were dominant in pillar and accounted for more than 90% of all MS events. The overall damage tensor of the pillar was subsequently assessed based on the MS-derived fractures, and the maximum damage direction was determined. Third, a fast chronological expansion method was proposed to iteratively build a connected network with a combination of MS event locations and the corresponding fracture orientations. The MS-derived connected network was used to estimate the distances of event-to-event seepage, from which the shortest seepage channel from each individual event to the network is

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26 determined in chronological order. Seepage channels between hydraulic recharge and discharge points
27 were inferred. These results could be helpful for better characterization of seepage channel development
28 and the implementation of pillar reinforcement.

29

30 **Key words:**

31 Microseismic monitoring; Crown pillar; Moment tensor inversion; Fracture network; Seepage channel

32

33 **1. Introduction**

34 A crown pillar is defined as the in-situ rock or transition region between the pit bottom and
35 an underground opening due to a transition from open pit to underground mining ¹. Such
36 structure is used to support the overburden and provide a safe working environment for
37 personnel and equipment. Thus, ensuring the stability of crown pillar has become one of the
38 most challenging problems for mines during a transition from open pit to underground mining
39 ². Water seepage and buried faults are two main factors that threaten the instability of crown
40 pillar. Many cases of water inrush have been documented in mines throughout the world. To
41 avoid potential water inrush hazards, both the long-term monitoring of the stability of crown
42 pillar and analysis of the formation processes of seepage channels are required.

43 A conventional method that is often used to assess the stability of crown pillar is the
44 calculation of the factor of safety (FoS). The FoS is defined as the ratio of a pillar's estimated
45 strength to the pillar's stress ^{3,4}. Tributary area theory ⁵, numerical simulation ⁶ and empirical
46 method ⁷ have been developed to estimate the strengths of such pillars. However, some
47 problems still exist when calculating the FoS. First, pillars are typically irregular, and the stress
48 in a pillar is difficult to estimate. Second, the overburden is supported by an array of pillars, but
49 the FoS is the property of an individual pillar. Third, water seepage and discontinuous structures
50 like faults, joints and fissures are seldom considered.

51 Over the last decade, several attempts have been carried out to monitor the stability of
52 pillar. Tawadrous and Katsabanis ⁸ investigated the stability of crown pillar based on artificial
53 neural networks, within which input parameters are required for training and then to predict the
54 crown pillar behavior. In their study, the proper choice of parameters is significant and it may

55 make substantial differences in the results. Moreover, some factors, such as the water seepage
56 path and the distribution pattern of stopes, are difficult to describe using input parameters.
57 Zaidel et al. ⁹ applied the finite difference software MODFLOW to simulate the water seepage
58 path throughout the workings of a mine and discussed the numerical errors induced by finite-
59 difference grids. The determination of the mechanical parameters in a numerical model is
60 difficult but vital ¹⁰, and a large number of in-situ rock mass tests and laboratory tests are
61 required ¹¹. Due to the computational limits, the numerical model must be simplified, and many
62 factors regarding the complexity of the rock mass are consequently ignored. Meanwhile, the
63 simulation results also highly depend on the chosen constitutive model. Although numerical
64 methods have proven effective, differences still exist in the results. Therefore, numerical
65 simulations should be combined with field monitoring data to reveal the actual state of rock
66 mass.

67 MS monitoring is a burgeoning non-destructive field monitoring technology that has been
68 widely used in many rock engineerings, such as tunnelling ¹²⁻¹⁴, slope control ¹⁵⁻¹⁸, oil and gas
69 exploitation ¹⁹⁻²¹, underground nuclear waste repository ^{22, 23} and mining ²⁴⁻²⁶. MS monitoring
70 systems are capable of constantly detecting elastic waves in a rock mass and providing feedback
71 on the properties of the sources of failure, including the hypocenter location and source
72 parameters ^{27, 28}. Thus, it is an efficient tool for detecting buried fault dislocations and seepage
73 channel formations, which is resulted from mining activities and occurs in deeply buried rock
74 masses ^{29, 30}. Seepage paths and hydraulic sources are both important in understanding the
75 mechanism of water inrush incidents. The conventional methods to analyze seepage channels
76 are physical similitude modeling ³¹, numerical simulation and groundwater boreholes ³². Zhao
77 et al. ²⁵ proposed a method to inverse the seepage channels using intersections of MS-derived
78 fractures. This method assumes that the rock mass is strictly impermeable and water is forced
79 to flow between fractures via their intersection points. It may underestimate the number of
80 seepage channels for the ignorance of water seepage in rock mass. And if a fracture intersects
81 with several fractures, there will be ill-conditioned seepage channels on fracture surfaces.
82 Moreover, this method does not consider the chronological effect of the MS data which will
83 significantly affect the inversion result of seepage channels.

84 The aim of this study is to **propose** a method for analyzing the development processes of
 85 seepage channels in crown pillar using MS technology. Based on the method, the
 86 spatiotemporal evolution of the MS events with moment magnitude information was presented.
 87 Then, the failure types of the MS events were discerned via MTI. The fracture orientations were
 88 measured using the proposed 3D rose diagrams. After that, the main fracture surfaces were
 89 derived. The distribution characteristics of the source radii and failure volumes were discussed.
 90 Finally, the connectivity among the MS sources was analyzed based on a proposed connected
 91 network. The formation processes of the seepage channels, seepage paths, discharge areas and
 92 hydraulic recharge sources were determined.

93

94 **2. Theory of moment tensor inversion**

95 The MS source can be mathematically represented by a moment tensor (MT), which can
 96 be calculated by the MTI method. As presented in Fig. 1, the components of the MT denote
 97 different moments at the source. A seismic source induced by rock fracturing can be expressed
 98 as a linear combination of the moments. To satisfy the moment equilibrium, MTs are usually
 99 symmetric, i.e., $M_{ij} = M_{ji}$. MTs can be used to determine the failure types of rock fractures ³³
 100 and help understand rock failure mechanism ³⁴.

101

102

[Fig. 1 goes here]

103

104 An MT can be expressed as $\mathbf{GM} = \mathbf{u}$ ³⁵, where \mathbf{u} is a vector representing the far-field
 105 displacement, \mathbf{M} is the moment tensor, and \mathbf{G} is the Green's function. Therefore, this equation
 106 can be expanded as follows:

$$107 \begin{pmatrix} G_{1,1}^1 & G_{2,2}^1 & G_{3,3}^1 & G_{2,3}^1 + G_{3,2}^1 & G_{1,3}^1 + G_{3,1}^1 & G_{1,2}^1 + G_{2,1}^1 \\ G_{1,1}^2 & G_{2,2}^2 & G_{3,3}^2 & G_{2,3}^2 + G_{3,2}^2 & G_{1,3}^2 + G_{3,1}^2 & G_{1,2}^2 + G_{2,1}^2 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ G_{1,1}^N & G_{2,2}^N & G_{3,3}^N & G_{2,3}^N + G_{3,2}^N & G_{1,3}^N + G_{3,1}^N & G_{1,2}^N + G_{2,1}^N \end{pmatrix} \begin{pmatrix} M_{11} \\ M_{22} \\ M_{33} \\ M_{23} \\ M_{13} \\ M_{12} \end{pmatrix} = \begin{pmatrix} u_1 \\ u_2 \\ \vdots \\ u_N \end{pmatrix} \quad (1)$$

108 where $G_{k,m}^N$ is the displacement along the m direction recorded by the N th sensor, and k is the
 109 direction of a unit-force source. Thus, \mathbf{M} can be computed when more than six sensors are
 110 triggered.

111 For single-component sensors, the value of \mathbf{u} in Eq. (1) is difficult to obtain. Thus, a
 112 relative MTI method was proposed based on experimental tests³⁶. When only considering the
 113 far-field term of the P -phase, \mathbf{u} can be rewritten as follows:

$$114 \quad u_i = \frac{r_i r_p r_q}{4\pi v_p^3 \rho R} M_{pq}, i, p, q = 1, 2, 3 \quad (2)$$

115 where u_i is the P -phase first motion with respect to the i th-axis, $\mathbf{r} = (r_1, r_2, r_3)$ represents the
 116 direction vector from the source to the sensors, R is the hypocentral distance and ρ is the rock
 117 density.

118 The sensors used at the Shirengou iron mine are recyclable and are emplaced on the
 119 surfaces of **hole** bottoms without concrete. Therefore, the effects of both reflection and
 120 attenuation must be considered. The motion u_0 induced by a unit-source force $f(t)$ can be
 121 determined by the following:

$$122 \quad u_0 = \frac{C'_s R e(\mathbf{t}, \mathbf{r}) e^{-\alpha R}}{R} f(t) = \frac{C'_s R e(\mathbf{t}, \mathbf{r})}{R} e^{-\frac{\pi f}{v_p Q} R} f(t) \quad (3)$$

123 where C'_s is the sensor sensitivity, $R_c(t, r)$ is the reflection coefficient, \mathbf{t} is the direction normal
 124 to the sensor, α is the attenuation coefficient, Q is the P -phase quality factor, and f is the corner
 125 frequency. The values of C'_s for each sensor are determined via calibration. Then, Eq. (1) can
 126 be rewritten as follows:

$$127 \quad \begin{pmatrix} c^1 r_1^1 r_1^1 & c^1 r_2^1 r_2^1 & c^1 r_3^1 r_3^1 & c^1 2r_2^1 r_3^1 & c^1 2r_1^1 r_3^1 & c^1 2r_1^1 r_2^1 \\ c^2 r_1^2 r_1^2 & c^2 r_2^2 r_2^2 & c^2 r_3^2 r_3^2 & c^2 2r_2^2 r_3^2 & c^2 2r_1^2 r_3^2 & c^2 2r_1^2 r_2^2 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ c^N r_1^N r_1^N & c^N r_2^N r_2^N & c^N r_3^N r_3^N & c^N 2r_2^N r_3^N & c^N 2r_1^N r_3^N & c^N 2r_1^N r_2^N \end{pmatrix} \begin{pmatrix} M_{11} \\ M_{22} \\ M_{33} \\ M_{23} \\ M_{13} \\ M_{12} \end{pmatrix} = \begin{pmatrix} u_1 \\ u_2 \\ \vdots \\ u_N \end{pmatrix} \quad (4)$$

$$128 \quad \text{where } c^i = \frac{C_s^i R e^i(\mathbf{t}^i, \mathbf{r}^i)}{R^i} e^{-\frac{\pi f_i R^i}{v_p Q^i}}, i = 1, \dots, N.$$

129 The full moment tensor \mathbf{M} of an event then can be obtained by Eq. (4). Considering the
 130 eigenvalues m_1, m_2, m_3 and orthonormal eigenvectors $\mathbf{e}_i = (e_{ix}, e_{iy}, e_{iz})^T$ of the moment
 131 tensor, \mathbf{M} can be rewritten as

$$132 \quad \mathbf{M} = [\mathbf{e}_1, \mathbf{e}_2, \mathbf{e}_3] \mathbf{m} [\mathbf{e}_1, \mathbf{e}_2, \mathbf{e}_3]^T \quad (5)$$

133 where $\mathbf{m} = \begin{bmatrix} m_1 & 0 & 0 \\ 0 & m_2 & 0 \\ 0 & 0 & m_3 \end{bmatrix}$ is the diagonalized moment tensor. Following Knopoff and
 134 Randall³⁷ and Fitch et al.³⁸, a moment tensor \mathbf{m} can be decomposed into a double-couple (DC)
 135 components, an isotropic (ISO) components and a compensated linear vector dipole (CLVD)
 136 component:

$$137 \quad \mathbf{m} = \mathbf{m}^{\text{ISO}} + \mathbf{m}^{\text{DC}} + \mathbf{m}^{\text{CLVD}} \quad (6)$$

138 where \mathbf{m}^{ISO} represents a volume change in the source, and \mathbf{m}^{DC} represents double-couple shear
 139 dislocation. The complete decomposition of \mathbf{m} is as follows:

$$140 \quad \mathbf{m} = \frac{\text{tr}(\mathbf{m})}{3} \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} + m_3^*(1-2\epsilon) \begin{bmatrix} 0 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{bmatrix} + m_3^*\epsilon \begin{bmatrix} -1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 2 \end{bmatrix} \quad (7)$$

141 where $\text{tr}(\mathbf{m}) = m_1 + m_2 + m_3$ is the trace of the moment tensor, $m_i^* = m_i - \frac{1}{3}\text{tr}(\mathbf{m})$ is the
 142 purely deviatoric eigenvalues of the moment tensor. Assume $|m_3^*| \geq |m_2^*| \geq |m_1^*|$, $\epsilon =$
 143 $-m_1^*/m_3^*$ is the ratio of the minimum eigenvalue to the maximum eigenvalue. For the
 144 deviatoric condition $\sum m_i^* = 0$, we can get $0.5 \geq \epsilon \geq 0$. Since ϵ changes from 0 to 0.5, the
 145 seismic source changes from pure DC to pure CLVD.

146 The ratio of the pure shear component K indicates the contribution of the maximum shear
 147 moment³⁶. The ratio can be expressed as follows:

$$148 \quad \begin{cases} K = k_2 / \sum k_i \\ k_1 = \text{tr}(\mathbf{m}) / 3 \\ k_2 = m_3^*(1-2\epsilon) \\ k_3 = m_3^*\epsilon \end{cases} \quad (8)$$

149 where k_i is the coefficient of each components on the right side of Eq. (7).

150 A fracture is classified as a shear fracture when $K > 60\%$. In contrast, fractures are
 151 classified as mixed-mode and tensile fractures when $60\% \geq K \geq 40\%$ and $K < 40\%$, respectively.
 152 Moreover, the fracture orientation \mathbf{n} and the slip direction \mathbf{l} can be determined by the following:

$$153 \quad \begin{cases} \mathbf{l} = \sqrt{\frac{m_3-m_2}{m_3-m_1}} \mathbf{e}_3 + \sqrt{\frac{m_2-m_1}{m_3-m_1}} \mathbf{e}_1 \\ \mathbf{n} = \sqrt{\frac{m_3-m_2}{m_3-m_1}} \mathbf{e}_3 - \sqrt{\frac{m_2-m_1}{m_3-m_1}} \mathbf{e}_1 \end{cases} \quad (9)$$

154 where \mathbf{e}_1 and \mathbf{e}_3 are the corresponding eigenvectors of the moment tensor. It should be noted
 155 that \mathbf{n} and \mathbf{l} are changeable. An ambiguity is presented because it is hard to distinguish the real
 156 fracture direction from the slip direction.

157 Fig. 2 shows the focal mechanism for three types of MS sources, where the red, blue and
 158 green colors represent tension, shear and mixed-mode failure types, respectively. In the
 159 following sections, these failure types are represented by simplified beach ball diagrams in the
 160 right panel of the figure. The seismic sources can be ideally simplified as two plates. Rock
 161 fractures are caused by dislocations along the two plates, and the failure types can be
 162 differentiated via the relations among the two direction vectors \mathbf{n} and \mathbf{l} . In the case of a tensile
 163 fracture, \mathbf{n} and \mathbf{l} are nearly parallel. A tensile fracture and its orientation can be seen in the
 164 tensile beach ball diagram. For a shear fracture, \mathbf{n} is nearly perpendicular to \mathbf{l} . For \mathbf{n} and \mathbf{l} are
 165 changeable, there are two possible fracture planes and slip directions in a focal mechanism
 166 solution, as shown in the shear beach ball diagram. Either of them could represent the real
 167 fracture if a geological survey is not conducted for verification. Accordingly, the mixed-mode
 168 fracture type is a combination of pure tension and shear, and two possible fractures are shown
 169 in the mixed-mode beach ball.

170
 171 [Fig. 2 goes here]
 172

173 Ohtsu³⁶ suggested that the fracture volume ΔV could be obtained through the MT:

$$174 \quad \Delta V = M_{kk} / [(3\lambda + 2\mu)l_k n_k] \quad (10)$$

175 where M_{kk} is the trace of the MT, λ and μ are Lamé constants, and l_k and n_k are the components
 176 of \mathbf{n} and \mathbf{l} , respectively. The source radius r_s can be determined by the following³⁹:

$$177 \quad r_s = \frac{K_c v_s}{2\pi f_c} \quad (11)$$

178 where K_c is a constant 2.34 for the Brune model, v_s is the shear-wave velocity, and f_c is the
 179 dominant frequency of the seismic wave. For seismic sources that are assumed to be product of
 180 differential movement along plates, the thickness D of a fracture can be calculated as follows:

$$181 \quad D = \frac{\Delta V}{\pi r_s^2} \quad (12)$$

182 3. Engineering situation and MS system

183 3.1 Engineering situation

184 The Shirengou iron mine is located approximately 90 km away from the city of Tangshan,

185 China. It is one of the largest iron mines in China with a length of nearly 2800 m from north to
186 south and a width of 230 m from east to west. Since 2004, the mining area has transitioned from
187 open pit to underground mining. The yellow surface in Fig. 3 represents the open pit, the blue
188 and brown blocks below the surface denote stopes, and the cyan, green, blue and red tunnels
189 represent 0 m, -60 m, -120 m and -180 m drifts, respectively. The stability of the crown pillar
190 has attracted much attention.

191 A typical location in the mine (shown in Fig. 4) was chosen as the study area for five
192 important reasons. First, the slopes on either side are relatively steeper than in other places.
193 Second, a backfill plant, which is critical for stope backfill, is constructed on the eastern slope,
194 and the main backfill pipe is fixed on the slope surface. Third, after rain events, water gathers
195 in the pit bottom and then seeps downward into the underground openings. **The water depth in
196 the open pit bottom is about 3 m and 16 m in the dry season and rainy season, respectively.**
197 Fourth, the crown pillar in this area is the thinnest throughout the mine. Fifth, several
198 unrecognized and illegal mined-out areas are distributed in the study area. These reasons make
199 the stability in the study area significantly challenging.

200

201 [Fig. 3 goes here]

202

203 [Fig. 4 goes here]

204

205 3.2 MS system profile

206 An MS monitoring system was established in 2006. Thirty-one sensors are installed along
207 the strike of the mine. **In this study, eleven single-component sensors and one three-component
208 sensor contained in the study area was used to monitor microseismicity in the crown pillar**
209 (shown in Fig. 5). Three illegal goafs that have been detected (brown block) and six stopes
210 (blue blocks) are located within the 0 m and -60 m drifts. A potential buried fault (purple surface)
211 is highlighted. The study area was fully covered by the sensor array to ensure that the recorded
212 signals have good quality.

213

214

[Fig. 5 goes here]

215 4. Data analysis and discussions

216 4.1 Reliability analysis

217 After denoising, the autoregressive Akaike information criterion (AR-AIC) method ⁴⁰ or
218 the short-term average to long-term average ratio (*STA/LTA*) method ⁴¹ can be applied to
219 determine the phase arrival time. Then, MS sources can be further located via the Geiger
220 method ⁴². The location error (l_{err}) can be calculated by:

$$221 \quad l_{err} = v_p t_{err} = v_p \|t_0 - t_i + R_i/v_p\|_2 \quad (13)$$

222 where t_0 is the origin time, t_i represents the *P*-wave arrival time recorded by the *i*th sensor, R_i is
223 the distance between the MS source and the *i*th sensor, v_p is the *P*-wave velocity, and t_{err} is the
224 time error.

225 We adopted MS data that occurred from October 28, 2009 to March 21, 2010. Generally,
226 the events can be classified into five different types: blasting vibrations, mechanical vibrations
227 (MVs), MS events, background noise (BN), and impulse voltage (IV). The MS events were
228 manually picked based on the waveform database ⁴³. Thus, the reliability of those results was
229 confirmed. The distribution of the location errors is shown in Fig. 6. From the front view, the
230 errors in the area among the stopes varied from 5 m to 22 m. Meanwhile, the errors in the east
231 and west were relatively high. From the side view, the errors along the buried fault and above
232 stopes No.1 and No.2 ranged from 5 m to 15 m, which are relatively low. These higher location
233 errors are primarily attributable to the locations of events outside of the sensor array that had
234 less sensor coverage.

235

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[Fig. 6 goes here]

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238 4.2 Spatiotemporal evolution of MS events

239 The development process of the MS events can be divided into five stages, as shown in
240 Fig. 7. Each row shows the distribution of cumulative events among different stages. MS events
241 are colored and scaled according to the moment magnitude. The orange lines indicate the
242 boundary of the event cluster. At the first stage, the events induced by mining activities occurred

243 within two main regions. The eastern region was located in the hanging wall of the buried fault,
244 and the western part was situated above the roof of stope No.2. The moment magnitudes in this
245 stage were low and varied from -0.7 to -0.175. At the second stage, the two regions expanded
246 along the buried fault. Additionally, the events started to cluster around the crown pillar (i.e.,
247 the region between the 0 m drift and the pit bottom). This region, which is located immediately
248 under the water pool in Fig. 2, was affected by water seepage and pressure from the slope. At
249 the third stage, the upper region developed downward, and the first two regions extended
250 towards each other. Eight events with low moment magnitudes of -0.7 ~ -0.3 occurred above
251 the southern sidewall of goaf No.4. This indicates that a weak hydraulic linkage formed between
252 the goaf and the fault. At the fourth stage, the central and upper regions continued to expand,
253 after which they became connected. The moment magnitudes in the center of this region were
254 smaller (-0.7 ~ -0.2) while those along the edge of the region were larger, especially in the upper
255 and lower parts (-0.7 ~ 0.1). The events were mainly clustered within the foot wall of the fault
256 and near the east sidewall and roof of stope No.2. Six events with a low moment magnitude of
257 -0.5 occurred near the north sidewall of goaf No.3. At the final stage, the central event region
258 developed upward towards goaf No.3 and formed a hydraulic linkage. MS activities were very
259 **high** both in the crown pillar and near the junction between the fault and the 0 m drift. Events
260 with relatively low moment magnitudes of 0.05 ~ 0.4 were clustered throughout the lower part
261 of the buried fault and in the roof of the -60 m drift. Twelve events with moment magnitudes of
262 -0.6 ~ 0.17 occurred in the western portion of goaf No.3. Several smaller events with moment
263 magnitudes of -0.7 ~ -0.6 occurred above stope No.1. The white arrows in Fig. 7 illustrate the
264 seepage paths in the study area. Water originating from both goaf No.3 and the surface seeped
265 downward via the buried fault and concentrated in an area located 30 m above stope No.2. Most
266 of the water then percolated downward through the roof into stope No.2. A part of the water
267 seeped into the -60 m drift, while the remaining quantity of water infiltrated into stope No.1.

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[Fig. 7 goes here]

270

271 4.3 MT inversion analysis

272 MT analysis is an effective way to reveal the failure mechanism of inner rock mass. The
273 MTs were calculated using Eqs. (1) ~ (7). The results are presented in Fig. 8. Red, blue and
274 green beach balls represent tension, shear and mixed-mode failures, respectively. In particular,
275 tension fractures were rare during stages III and IV. Failures are primarily compression-induced
276 shear fractures^{44, 45}. Tension fractures are mainly resulted by the subsequent propagation of
277 fractures and the concentration of tensile stress along the roofs of openings.

278 During the first stage, shear fractures started to develop within the central part, especially
279 in the foot wall. This indicates the presence of a slight dislocation in this area. Tension fractures
280 and mixed-mode fractures occurred along the east sidewall of stope No.2, and an isolated tensile
281 fracture was found within the crown pillar.

282 During stage II, coincident with the mining activities, shear fractures were observed above
283 stope No.1 and along the east sidewall of stope No.2, which is coincident with the mining
284 activities. Near the surface, the rock masses were subjected to waterlogging and the weights of
285 the slopes, Thus, shear failures together with mixed-mode failures appeared. Shear and tensile
286 fractures alternately occurred near the east sidewall of stope No.2.

287 During stage III, additional shear failures occurred in the crown pillar. Water seeped
288 downward through these failures and entered the buried fault. Water intruded into the primary
289 discontinuity, thereby inducing a decrease of its shear strength. In addition, combined with the
290 effects of blasting disturbances, shear failure continued to occur constantly. Nascent shear
291 fractures clustered along the roof and floor of the northern part of the 0 m drift.

292 During stage IV, the shear zones near the northern bottom part of goaf No.3 markedly
293 expanded. Goaf No.3, which was 17 m wide and 93 m long with a capacity of more than 32000
294 m³, was perennially flooded. Based on the distribution pattern of the shear fractures, water in
295 the goaf seeped into the 0 m level drift from the northern corner and simultaneously infiltrated
296 into the fault from the west side, thereby forming a secondary recharge source in the study
297 area. Shear fractures clustered around the junction between the crown pillar and the fault.
298 Meanwhile, the hydraulic conductivity and recharge rate increased rapidly during this period.

299 During stage V, shear fractures occurred within the roof of the eastern part of the -60 m
300 level drift. The shear zone extended slightly downward. New shear failures appeared more

301 frequently in the hanging wall than in the foot wall. Moreover, the shear dislocations became
302 more densely spaced with greater intensities in the crown pillar.

303

304 [Fig. 8 goes here]

305

306 5. MS-derived fracture network analysis

307 An MT can indicate the presence of a fracture at a given location, which is illustrated in
308 Fig. 2. For a non-tensile source (i.e., a shear or mixed-mode source), two nodal planes with
309 normal n and l can be obtained. However, only one of them is the real fracture plane. To invert
310 fracture normals, we must have a method that is capable of correctly distinguishing the fracture
311 planes from the auxiliary planes. The most effective way to distinguish the fracture planes from
312 the auxiliary planes is by geological survey. However, this method is difficult because MS
313 fractures are incredibly small in scale and are buried within inner rock masses. Zhao et al. ²⁵
314 proposed a strategy to distinguish the real fracture by comparing the traction related to stress
315 field on two possible fracture surfaces. In the case the stress field is unspecified, stress tensor
316 can be inverted by the focal mechanisms following the method presented by Vavryčuk ⁴⁶. In
317 order to recover the shape ratio of the principal stresses, the trace of the stress tensor is usually
318 assumed to be zero, i.e., $\sigma_1 + \sigma_2 + \sigma_3 = 0$, which means the ISO component m^{ISO} in Eq. (6)
319 of the moment tensor should be zero ⁴⁷. Zero ISO component indicates a pure double couple
320 MS source. This assumption has some limitations when dealing with MS events in mines
321 because tensile component of MS events in mines is usually larger than the natural earthquake
322 and cannot be ignored. Thus, we proposed a straightforward method to estimate the fracture
323 normals of events.

324 5.1 Implementation of a 3D rose diagram

325 A 3D rose diagram was developed to analyze the main orientations of the fractures. The
326 principle used to construct a 3D rose diagram is presented in Fig. 9. The first step is to make a
327 base sphere and divide it into small facets. These facets can take many forms, such as longitude-
328 and-latitude grids, quadrilaterals and hexagons. For a longitude-and-latitude grid, the facet sizes
329 will decrease closer to the poles, which may make the results appear unrealistic. Quadrilateral

330 shapes are feasible, but they are not sufficiently uniform. Meanwhile, hexagons can form a
331 honeycomb-like structure, which is more natural and homogeneous. The base sphere can be
332 divided into facets with different sizes (i.e., high, normal or low resolutions) according to the
333 requirements or the amount of vectors to be counted. The vector v_i from the sphere center to
334 the facet center can then be calculated. Given a vector v_c , the absolute value of the minimum
335 included angle between v_c and v_i can be determined. Then, the corresponding facet is
336 extruded by one unit. To make the results appear conspicuous, facets are colored according to
337 their extruded lengths.

338

339

[Fig. 9 goes here]

340

341 5.2 Inversion of fracture network

342 The fractures were assumed to originate from the differential dislocation of two plates
343 (shown in Fig. 2). As discussed before, only one vector can be counted for a tensile fracture,
344 while two vectors (i.e., two nodal planes) can be observed for a shear fracture or a mixed-mode
345 fracture. For shear and mixed-mode fractures, it is hard to distinguish the real fracture planes n
346 from “fake” planes l . Therefore, we regard both the two vectors as the normals of fractures at
347 first and count all fracture normals in the 3D rose diagram. The extrusion length would be the
348 longest in the direction that has the largest amount of normal vectors. The directions with long
349 extrusion lengths are marked as the normals of potential fracture surfaces. If more than one
350 potential fracture surfaces are found, geological structures should be considered to determine
351 which is the most reasonable main fracture surface.

352 Fig. 10 shows the 3D rose diagram of the normal vectors of fractures from 290 MS events
353 Fractures in the hanging wall (south of the fault) and in the foot wall (north of the fault) were
354 counted separately. The number of vectors in each direction varied from 0 to 30. Thus, the 3D
355 rose diagrams in this case were always centrosymmetric. Two and three principal directions
356 were observed for the hanging wall and foot wall, respectively. These results could essentially
357 represent the buried fault.

358

359

[Fig. 10 goes here]

360

361 Based on the 3D rose diagrams, the main fracture surfaces perpendicular to the main
362 directions were obtained, the results of which were presented in Fig. 11. For clarity, the rose
363 diagrams and the fault were separated, and the fracture surfaces were shown using colored
364 annuluses. The fault was subdivided into two branches, i.e., F₁ and F₂. The fracture orientations
365 were in an NEU (north, east and up) coordinate system, and they were presented at the bottom
366 of the figure. The table in the bottom right showed the included angles between the potential
367 main fractures and the corresponding fault branches. In the hanging wall, the blue and golden
368 fractures exhibited included angles of 32.7° and 26.5° with F₁, respectively. Meanwhile, in the
369 foot wall, the green, blue and golden fractures had included angles of 60.5°, 16.6° and 34.6°
370 with F₂, respectively. These events were induced by the activation of the faults F1 and F2 under
371 disturbances from dynamic loadings. We assumed the mechanism for the fault dislocation and
372 the derived MS events was similar based on the classic MTI theory⁴⁸. The one with the smallest
373 angle with the buried fault was chosen as the main fracture surface. Then, for each shear and
374 mixed-mode fracture, the plane with a smaller angle with the main fracture surface was the
375 reasonable real fracture. Thus, the two golden fractures that more effectively matched with the
376 buried fault were assumed to be the principal fractures.

377

378

[Fig. 11 goes here]

379

380 Aki and Richards³⁵ suggested that the normal vector \mathbf{n} of a fracture could be written as
381 follows:

$$382 \quad \mathbf{n} = -\sin\delta\sin\phi_s\mathbf{e}_N + \sin\delta\cos\phi_s\mathbf{e}_E + \cos\delta\mathbf{e}_U \quad (14)$$

383 where \mathbf{e}_N , \mathbf{e}_E and \mathbf{e}_U are the unit vectors in NEU coordinate, δ is the dip angle and ϕ_s is the strike.
384 Accordingly, the dip ϕ_d can be derived. The orientations of the main fractures were subsequently
385 projected to an equal-angle lower-hemisphere plot, as shown in Fig. 12. The colors of the
386 fractures and the faults are preserved. The dip and dip angle of the main fracture in the hanging
387 wall were 202.04° \angle 87.94°, respectively. The dip and dip angle of the main fracture in the foot

388 wall were $189.78^\circ \angle 59.22^\circ$, respectively. The rose diagram can be regarded as a 3D version of
389 the stereographic diagram to some extent. Compared to the stereographic diagram, the rose
390 diagram is intuitive to count and show the orientations of the fractures in 3D scenes.

391

392

[Fig. 12 goes here]

393

394 For shear and mixed-mode fractures, the surface that exhibited a smaller included angle
395 with the main fracture was the real fracture plane. Here, the reference surface used to calculate
396 the included angles was the selected main fracture rather than the fault. The main fracture was
397 able to ensure that the generated fracture network had the same distribution regularity with the
398 same main orientation. The fracture network was subsequently generated using MS data, as
399 illustrated in Fig. 13. The resulting network exhibits realistic shapes of fracture growth patterns.
400 The fractures were indicated by circular plates and colored according to the order of occurrence
401 for the first row and the fracture volumes for the second row. The source radius and fracture
402 aperture are the two important factors that affect the hydraulic conductivity. A fracture with a
403 larger radius can connect with other fractures more easily, and vice versa. Meanwhile, a larger
404 fracture aperture can significantly increase the hydraulic conductivity when a hydraulic source
405 is connected. The source radii and fracture aperture were calculated using Eqs. (8) ~ (10). The
406 white arrows illustrated the propagation paths of the fractures. The center area and the open-pit
407 bottom were the two main places where the fractures initiated. Fractures in the center part were
408 densely spaced with relatively small source radii (0 ~ 8 m) and moderate volumes (0.06 ~ 100
409 m³). The rock mass was relatively intact prior to the onset of mining activities. Thus, few
410 primary fractures were available to provide space for the rock mass to shear even if there were
411 concentrated stresses. So the moment magnitudes therein were relatively small. In contrast,
412 goaf No.3 was flooded for a long time before being detected. The illegal goaf had an irregular
413 shape and was instable. Primary fractures were developed therein, and thus, it was easily
414 disturbed by blasting. Then, fractures near the bottom and west sidewall of goaf No.3 had
415 relatively high radii (5 ~ 15 m). Goaf No.3 easily connected with the center part and thereafter
416 became the secondary hydraulic source. Fractures developed and expanded within the crown

417 pillar during the monitoring period. Stresses from the slopes, water seepage, mining
418 disturbances and fault activations made it unstable, making it require additional essential
419 support. The fracture radii and fracture apertures near the fault were higher than those on either
420 side. The fractures in the lower part of the network had medium radii and apertures, meaning
421 that the seepage path was developing downward. Near the area, exposed fractures with water
422 were found at the roof of the drift. The maximum water discharge rate in the drift once reached
423 5623 m³/d. Consequently, preliminary reinforcement and waterproofing measures have been
424 taken for the drift near this area. Boreholes with lengths of 2 m and diameters of 45 mm were
425 drilled on the sidewall and roof of the drift. Waterproof material made of cement paste, sodium
426 silicate and urea-formaldehyde resins was injected into the fractures through the boreholes by
427 high-pressure grouting pumps. The water discharge rate was finally controlled below 2240 m³/d
428 and the water could be pumped away in time.

429

430

[Fig. 13 goes here]

431

432 Field observations have been conducted to obtain the orientations of rock discontinuities
433 in the same study area⁴⁹. The results were presented in Fig. 14. There were three dominant sets
434 of discontinuities S1, S2, and S3 in the pillar. It is interesting to find that the orientations of the
435 main fractures, faults and the set S1 were quite close. It indicates there was some inner
436 relationship between discontinuity set S1, fault dislocation and the mechanism of induced
437 microseismicity. Considering a shear dislocation along the fault surfaces, discontinuities of
438 similar orientations would promote the generation of MS events with similar focal mechanisms
439 as a result of shear along the existing discontinuity surfaces. On the other hand, it also proves
440 that the proposed method can efficiently determine the fracture surfaces of MS events.

441

442

[Fig. 14 goes here]

443

444 5.3 Overall damage analysis of the pillar

445 Mining-induced fractures have a significant effect on the rock mass strength and

446 deformability. In order to assess the state of the crown pillar, a damage mechanical model is
447 adopted to consider the effect of MS-derived fractures on the pillar. According to the damage
448 theory of jointed rock mass, the overall damage tensor can be calculated as ⁵⁰:

$$449 \quad \boldsymbol{\omega} = \sum_{k=1}^N \boldsymbol{\omega}^k = \frac{l_a}{V} \sum_{k=1}^N a^k (\mathbf{n}^k \otimes \mathbf{n}^k) \quad (15)$$

450 where l_a is the average fracture spacing, V is the pillar volume, N is the fracture number, a^k ,
451 $\boldsymbol{\omega}^k$ and \mathbf{n}^k are the area size, damage tensor and normal vector of the k -th fracture, respectively.
452 The symbol \otimes is tensor product.

453 The overall damage tensor of the pillar considering MS-derived fractures are shown in Fig.
454 15. The principal values of the damage tensor are $d_i = [d_1, d_2, d_3] = [0.33, 0.12, 0.15]$. The
455 corresponding principal vectors are $\boldsymbol{\lambda}_1=[0.96, -0.24, 0.14]$, $\boldsymbol{\lambda}_2=[-0.26, -0.96, 0.13]$, $\boldsymbol{\lambda}_3=[-0.11,$
456 $0.16, 0.98]$ in NEU coordinate system. The largest damage d_1 0.33 occurred in the north-south
457 direction that is perpendicular to the fault. The damage value of d_1 is about two times larger
458 than those in the other two principal directions. The strength and elastic modulus of the pillar
459 in the direction perpendicular to the fault are the lowest. Disturbances like blasting and vibration
460 from this direction would have the greatest influence on the stability of the pillar and deserved
461 more attention. More rock bolts should be installed in this direction.

462

463 [Fig. 15 goes here]

464

465 6. MS-derived connected network analysis

466 Each MS event represents a fracture in the rock mass with a certain source radius and
467 failure volume. The fractures were connected with one another, which is an important reason
468 for the observed increase in the hydraulic conductivity. However, using only intersecting penny-
469 shaped fractures as proxies to determine the seepage channels may greatly underestimate the
470 number of seepage channels due to the ignorance of water seepage in rock mass. In this section,
471 a fast chronological expansion method is proposed to build a connected network based on MS
472 events and their source orientations, as an extension of the method from Hugot et al. ¹⁹. It is
473 applicable even if the MS events are sparsely distributed. Here we define two distances for an

474 event, i.e., the impact distance l_i and the receptive distance l_r . Rock mass activities within l_i to
475 a newly occurred event are very intense, so the new event is connected with the nearest existing
476 fracture. In a distance from l_i to l_r , the fracture surface normal should be considered as a
477 connection criterion. The included angle between the surface normal of the new event and the
478 direction vector from event to event should be larger than β . In a distance larger than l_r , events
479 would not be connected. Events are calculated and connected in chronological order, details of
480 the building process are presented in Fig. 16. The blue and red circles in each step denote l_i and
481 l_r , respectively.

482
483 [Fig. 16 goes here]
484

485 The results of the subsequent connected network of MS events are shown in Fig. 17. l_i , l_r
486 and β are set to r_s , $2r_s$ and 60° . The connections among MS-derived fractures form a seepage
487 network in the pillar. In each step, a new MS event would be connected with the closest event
488 that meet the connection criteria. It means that each connection bond can represent the shortest
489 seepage path from the new MS event to the existing seepage networks. A small length denotes
490 a strong bond, and vice versa. Additionally, bonds that were longer than the limiting distance L
491 ($L = 30$ m in this case) were ignored. The bonds were classified into three types according to
492 their lengths: 0 m ~ 6 m denoted a strong bond (0% ~ 20% of L), 6 m ~ 13.5 m denoted a medium
493 bond (20% ~ 45% of L) and 13.5 m ~ 30 m denoted a weak bond (45% to 100% of L). In the
494 study area, the bonds were generally distributed along the fault, and their lengths generally
495 ranged from 1 m to 8 m. The strong bonds observed in the central part were dense and well
496 developed, indicating that the fault was activated by mining activities. Beneath the northern
497 bottom part of goaf No.3, strong bonds were clustered and connected with the central part. The
498 crown pillar in the upper and western parts of the fault was full of strong and medium bonds.
499 These bonds were connected with the water pool at the open-pit bottom, which constituted the
500 main water recharge source. The roof of stope No.2 and the east sidewall of stope No.1 were
501 the nearest areas of inrush from the central part. Strong bonds were also developed in the roof
502 of the eastern part of the -60 m drift, and the nearby medium bonds extended downward and

503 potentially affected the deeper working faces. During the monitoring period, goaf No.4 seemed
504 to exhibit medium hydraulic bonds with the open-pit bottom and few bonds with the fault.
505 Additionally, there was no precursor for the downward penetration of water within goaf No.4.

506

507

[Fig. 17 goes here]

508

509 **7. Conclusions**

510 We presented a microseismicity-based method to study the development of seepage
511 channels. This method considers the chronological order and the focal mechanism of MS events
512 in the inversion procedure of seepage channels. It is applicable even if the stress field is
513 unspecified and MS events are sparsely distributed. The method was implemented to study the
514 seepage channel development in the crown pillar beneath an open-pit to underground mining
515 transition. The spatiotemporal evolution of the MS events, source mechanisms, fracture
516 network, source radii, fault volumes, damage tensor and connected network were analyzed.

517 MS activities were very **high** in the crown pillar. The center area and the open-pit bottom
518 were the two main places where the mining-induced fractures first initiated with small source
519 radii and medium failure volumes. Fractures expanded as mining activities advanced to form
520 the final seepage channels. Water from the open-pit bottom and upper goaf seeped downward
521 along the fault and penetrated into the crown pillar. After gathering within the center part of the
522 faults, most of the water flowed downward into stope No.2. Two main hydraulic recharge
523 sources and three discharge points were localized. The seepage channels between hydraulic
524 recharge and discharge points were inferred.

525 Shear fractures were dominant in the crown pillar and accounted for more than 90% of all
526 MS events. As the MS events are induced by the fault activation under disturbances from
527 mining, a similar mechanism assumption was made to determine the fracture surfaces of non-
528 tensile MS events. MS-derived fractures with average orientations of $202.04^\circ \angle 87.94^\circ$ and
529 $189.78^\circ \angle 59.22^\circ$ were obtained in the hanging wall and footwall of the faults, respectively. A
530 set of discontinuities with similar orientations were obtained by field observations in the pillars.
531 The existence of the discontinuities was found to be an important factor affecting the focal

532 mechanism of the MS events besides the mining activities. The overall damage state of the
533 pillar was assessed based on the MS-derived fracture network. The direction with the largest
534 damage value was approximately perpendicular to the faults. Mining-induced fractures
535 compromised the overall stability of the crown pillar, which could form seepage channels and
536 might subsequently lead to water inrush.

537 A fast chronological expansion method was proposed to build a connected network based
538 on MS locations and their source orientations obtained from MTI. The approach provided a
539 convenient way to efficiently reveal the pattern of seepage channels. The distances of event-to-
540 event seepage were estimated and the shortest seepage channel from each individual event to
541 the network was determined in chronological order.

542 Although the approach provides a convenient way to perform seepage channel
543 development analysis, the method is highly dependent on high-quality seismic records. Poor-
544 quality, unreliable and non-representative events should be carefully eliminated. MS event
545 **location** is the second factor that has a serious impact on the reliability of results. Precise
546 location of MS event in a complex engineering rock mass is challenging so far. Ray-tracing
547 based locating method might be helpful to improve the accuracy of the connected network.

548

549 **Declaration of competing interest**

550 The authors declared that they have no conflicts of interest to this work.

551

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555

556 **References**

- 557 1. Ghasemi E, Kalhori H, Bagherpour R. Stability assessment of hard rock pillars using two intelligent
558 classification techniques: A comparative study. *Tunnelling and Underground Space Technology*.
559 2017;68: 32-37.
- 560 2. Esterhuizen GS, Dolinar DR, Ellenberger JL. Pillar strength in underground stone mines in the
561 United States. *International Journal of Rock Mechanics and Mining Sciences*. 2011;48(1): 42-50.

- 562 3. Galvin J. Considerations Associated with the Application of the UNSW and Other Pillar Design
563 Formulae. *Golden Rocks 2006, The 41st U.S. Symposium on Rock Mechanics (USRMS)*. Golden,
564 Colorado: American Rock Mechanics Association; 2006:9.
- 565 4. Poulsen BA. Coal pillar load calculation by pressure arch theory and near field extraction ratio.
566 *International Journal of Rock Mechanics and Mining Sciences*. 2010;47(7): 1158-1165.
- 567 5. Ghasemi E, Shahriar K. A new coal pillars design method in order to enhance safety of the retreat
568 mining in room and pillar mines. *Safety Science*. 2012;50(3): 579-585.
- 569 6. Martin CD, Maybee WG. The strength of hard-rock pillars. *International Journal of Rock*
570 *Mechanics and Mining Sciences*. 2000;37(8): 1239-1246.
- 571 7. Lunder P, Pakalnis R. Determination of the strength of hard-rock mine pillars. *World Mining*
572 *Express*. 1998;14(4): 24-28.
- 573 8. Tawadrous AS, Katsabanis PD. Prediction of surface crown pillar stability using artificial neural
574 networks. *International Journal for Numerical and Analytical Methods in Geomechanics*. 2007;31(7):
575 917-931.
- 576 9. Zaidel J, Markham B, Bleiker D. Simulating Seepage into Mine Shafts and Tunnels with
577 MODFLOW. *Groundwater*. 2010;48(3): 390-400.
- 578 10. Yang TH, Wang PT, Xu T, et al. Anisotropic characteristics of jointed rock mass: A case study at
579 Shirengou iron ore mine in China. *Tunnelling & Underground Space Technology*. 2015;48: 129-139.
- 580 11. Liu Y-C, Chen C-S. A new approach for application of rock mass classification on rock slope
581 stability assessment. *Engineering Geology*. 2007;89(1): 129-143.
- 582 12. Feng GL, Feng XT, Chen BR, Xiao YX. Performance and feasibility analysis of two microseismic
583 location methods used in tunnel engineering. *Tunnelling and Underground Space Technology*. 2017;63:
584 183-193.
- 585 13. Xiao YX, Feng XT, Chen BR, Feng GL, Yao ZB, Hu LX. Excavation-induced microseismicity in
586 the columnar jointed basalt of an underground hydropower station. *International Journal of Rock*
587 *Mechanics and Mining Sciences*. 2017;97: 99-109.
- 588 14. Li B, Xu N, Dai F, Zhang G, Xiao P. Dynamic analysis of rock mass deformation in large
589 underground caverns considering microseismic data. *International Journal of Rock Mechanics and*
590 *Mining Sciences*. 2019;122: 104078.
- 591 15. Xu NW, Dai F, Liang ZZ, Zhou Z, Sha C, Tang CA. The dynamic evaluation of rock slope stability
592 considering the effects of microseismic damage. *Rock Mechanics and Rock Engineering*. 2014;47(2):
593 621-642.
- 594 16. Salvoni M, Dight PM. Rock damage assessment in a large unstable slope from microseismic
595 monitoring - MMG Century mine (Queensland, Australia) case study. *Engineering Geology*. 2016;210:
596 45-56.
- 597 17. Ma K, Tang CA, Liang ZZ, Zhuang DY, Zhang QB. Stability analysis and reinforcement evaluation
598 of high-steep rock slope by microseismic monitoring. *Engineering Geology*. 2017;218: 22-38.
- 599 18. Dai F, Jiang P, Xu N, Chen W, Tan Y. Focal mechanism determination for microseismic events and
600 its application to the left bank slope of the Baihetan hydropower station in China. *Environmental Earth*
601 *Sciences*. 2018;77(7): 268.
- 602 19. Hugot A, Dulac J-C, Gringarten E, Haouesse A. Connecting the Dots: Microseismic-Derived
603 Connectivity for Estimating Volumes in Low-Permeability Reservoirs. *Unconventional Resources*
604 *Technology Conference*. San Antonio, Texas, USA: Unconventional Resources Technology Conference;
605 2015:12.

- 606 20. Kushnir A, Varypaev A. Robustness of statistical algorithms for location of microseismic sources
607 based on surface array data. *Computational Geosciences*. 2017;21(3): 459-477.
- 608 21. Chen H, Meng X, Niu F, Tang Y, Yin C, Wu F. Microseismic Monitoring of Stimulating Shale Gas
609 Reservoir in SW China: 2. Spatial Clustering Controlled by the Preexisting Faults and Fractures. *Journal*
610 *of Geophysical Research: Solid Earth*. 2018;123(2): 1659-1672.
- 611 22. Fairhurst C. Nuclear waste disposal and rock mechanics: contributions of the Underground
612 Research Laboratory (URL), Pinawa, Manitoba, Canada. *International Journal of Rock Mechanics and*
613 *Mining Sciences*. 2004;41(8): 1221-1227.
- 614 23. Martino JB, Chandler NA. Excavation-induced damage studies at the Underground Research
615 Laboratory. *International Journal of Rock Mechanics and Mining Sciences*. 2004;41(8): 1413-1426.
- 616 24. Cheng G, Li L, Zhu W, et al. Microseismic investigation of mining-induced brittle fault activation
617 in a Chinese coal mine. *International Journal of Rock Mechanics and Mining Sciences*. 2019;123:
618 104096.
- 619 25. Zhao Y, Yang T, Zhang P, Xu H, Wang S. Inversion of seepage channels based on mining-induced
620 microseismic data. *International Journal of Rock Mechanics and Mining Sciences*. 2020;126: 104180.
- 621 26. Ma K, Sun XY, Tang CA, Yuan FZ, Wang SJ, Chen T. Floor water inrush analysis based on
622 mechanical failure characters and microseismic monitoring. *Tunnelling and Underground Space*
623 *Technology*. 2020: 103698.
- 624 27. Tang CA, Wang JM, Zhang JJ. Preliminary engineering application of microseismic monitoring
625 technique to rockburst prediction in tunneling of Jinping II project. *Journal of Rock Mechanics and*
626 *Geotechnical Engineering*. 2010;2(3): 193-208.
- 627 28. Xiao YX, Feng XT, Hudson JA, Chen BR, Feng GL, Liu JP. ISRM suggested method for in situ
628 microseismic monitoring of the fracturing process in rock masses. *Rock Mechanics and Rock*
629 *Engineering*. 2016;49(1): 343-369.
- 630 29. Li T, Mei TT, Sun XH, Lv YG, Sheng JQ, Cai M. A study on a water-inrush incident at Laohutai
631 coalmine. *International Journal of Rock Mechanics and Mining Sciences*. 2013;59: 151-159.
- 632 30. Zhang PH, Yang TH, Yu QL, et al. Microseismicity induced by fault activation during the fracture
633 process of a crown pillar. *Rock Mechanics and Rock Engineering*. 2015;48(4): 1673-1682.
- 634 31. Zhang S, Guo W, Li Y, Sun W, Yin D. Experimental Simulation of Fault Water Inrush Channel
635 Evolution in a Coal Mine Floor. *Mine Water and the Environment*. 2017;36(3): 443-451.
- 636 32. Shi W, Yang T, Yu Q, Li Y, Liu H, Zhao Y. A Study of Water-Inrush Mechanisms Based on Geo-
637 Mechanical Analysis and an In-situ Groundwater Investigation in the Zhongguan Iron Mine, China.
638 *Mine Water and the Environment*. 2017;36(3): 409-417.
- 639 33. Feignier B, Young RP. Moment tensor inversion of induced microseismic events: Evidence of
640 non-shear failures in the $-4 < M < -2$ moment magnitude range. *Geophysical Research Letters*.
641 1992;19(14): 1503-1506.
- 642 34. Linzer LM. A Relative Moment Tensor Inversion Technique Applied to Seismicity Induced by
643 Mining. *Rock Mechanics and Rock Engineering*. 2005;38(2): 81-104.
- 644 35. Aki K, Richards PG. *Quantitative seismology, second edition*: University Science Books; 2002.
- 645 36. Ohtsu M. *Moment tensor analysis*: Springer Berlin Heidelberg; 2008.
- 646 37. Knopoff L, Randall MJ. The compensated linear-vector dipole: A possible mechanism for deep
647 earthquakes. *Journal of Geophysical Research (1896-1977)*. 1970;75(26): 4957-4963.
- 648 38. Fitch TJ, McCowan DW, Shields MW. Estimation of the seismic moment tensor from teleseismic

- 649 body wave data with applications to intraplate and mantle earthquakes. *Journal of Geophysical Research: Solid Earth*. 1980;85(B7): 3817-3828.
- 650
- 651 39. Mendecki DAJ. *Seismic monitoring in mines*: Chapman & Hall; 1997.
- 652 40. Akaike H. Markovian representation of stochastic processes and its application to the analysis of
- 653 autoregressive moving average processes. *Annals of the Institute of Statistical Mathematics*. 1974;26(1):
- 654 363-387.
- 655 41. Liu H, Zhang J. STA/LTA algorithm analysis and improvement of Microseismic signal automatic
- 656 detection. *Progress in Geophysics*. 2014;29(4): 1708-1714.
- 657 42. Geiger L. Probability method for the determination of earthquake epicenters from the arrival time
- 658 only. *Bulletin of Saint Louis University*. 1912;8(1): 60-71.
- 659 43. Zhou JR, Yang TH, Zhang PH, Xu T, Wei J. Formation process and mechanism of seepage channels
- 660 around grout curtain from microseismic monitoring: A case study of Zhangmatun iron mine, China.
- 661 *Engineering Geology*. 2017;226: 301-315.
- 662 44. Kao CS, Carvalho FCS, Labuz JF. Micromechanisms of fracture from acoustic emission.
- 663 *International Journal of Rock Mechanics and Mining Sciences*. 2011;48(4): 666-673.
- 664 45. Mahdevari S, Shahriar K, Sharifzadeh M, Tannant DD. Assessment of failure mechanisms in deep
- 665 longwall faces based on mining-induced seismicity. *Arabian Journal of Geosciences*. 2016;9(18): 709.
- 666 46. Vavryčuk V. Iterative joint inversion for stress and fault orientations from focal mechanisms.
- 667 *Geophysical Journal International*. 2014;199(1): 69-77.
- 668 47. Hardebeck JL, Michael AJ. Damped regional-scale stress inversions: Methodology and examples
- 669 for southern California and the Coalinga aftershock sequence. *Journal of Geophysical Research: Solid*
- 670 *Earth*. 2006;111(B11).
- 671 48. Capuano P, Zollo A, Singh SK. Source characteristics of moderate size events using empirical
- 672 Green functions: an application to some Guerrero (Mexico) subduction zone earthquakes. *Annals of*
- 673 *Geophysics*. 1994;37(6): 1659-1677.
- 674 49. Zhou JR, Wei J, Yang TH, Zhu WC, Li LC, Zhang PH. Damage analysis of rock mass coupling
- 675 joints, water and microseismicity. *Tunnelling and Underground Space Technology*. 2018;71: 366-381.
- 676 50. Liu H, Yuan X. A damage constitutive model for rock mass with persistent joints considering joint
- 677 shear strength. *Canadian Geotechnical Journal*. 2015;52(8): 1136-1143.

$$M = \begin{pmatrix} M_{11} & M_{12} & M_{13} \\ M_{21} & M_{22} & M_{23} \\ M_{31} & M_{32} & M_{33} \end{pmatrix} = \begin{pmatrix} \begin{array}{c} \text{Diagram 1} \\ \text{Diagram 2} \\ \text{Diagram 3} \end{array} & \begin{array}{c} \text{Diagram 4} \\ \text{Diagram 5} \\ \text{Diagram 6} \end{array} & \begin{array}{c} \text{Diagram 7} \\ \text{Diagram 8} \\ \text{Diagram 9} \end{array} \end{pmatrix}$$

Fig. 1 Components of a moment tensor

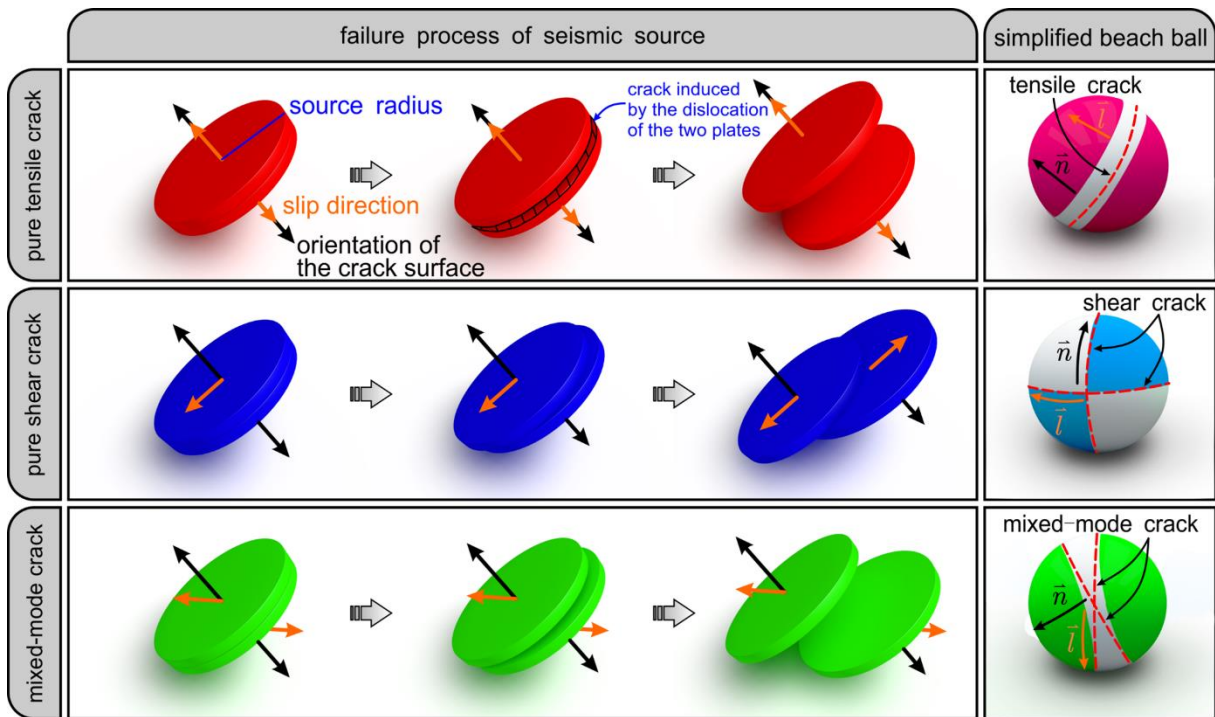


Fig. 2 Failure process and characterization of microseismic sources

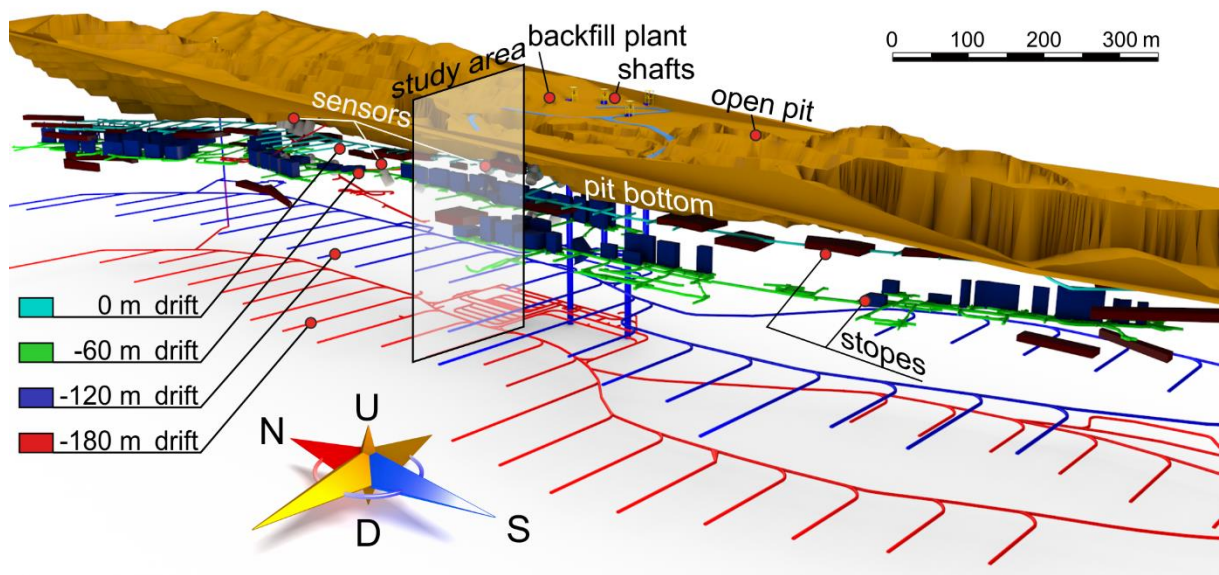


Fig. 3 Diagram of the mine. The abbreviations N, S, U and D near the compass represent north, south, up and down, respectively



Fig. 4 Photograph of the study area

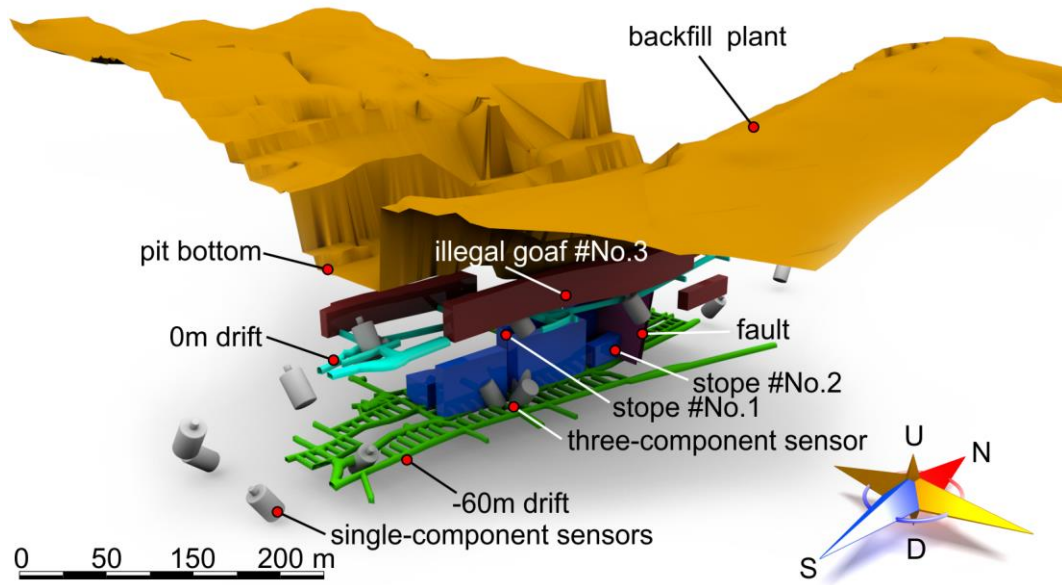


Fig. 5 Diagram of the study area and sensor array. Blue (■) and brown (■) blocks below the surface denote stopes, and the cyan (■) and green (■) tunnels represent 0 m and -60 m drifts, respectively

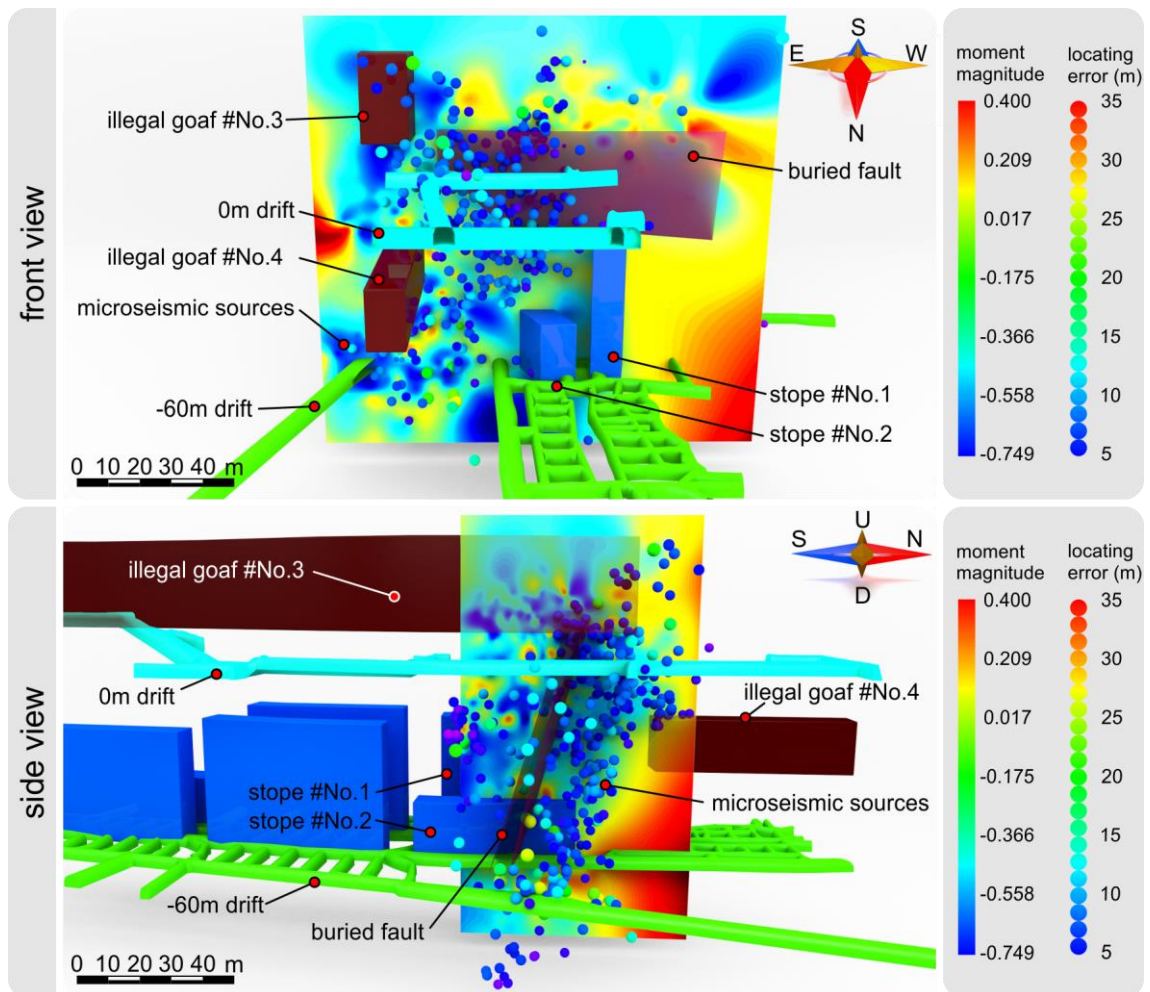


Fig. 6 Location error distribution for the MS events. Events are colored according to the moment magnitude and the distribution of the location error is shown in the colored map

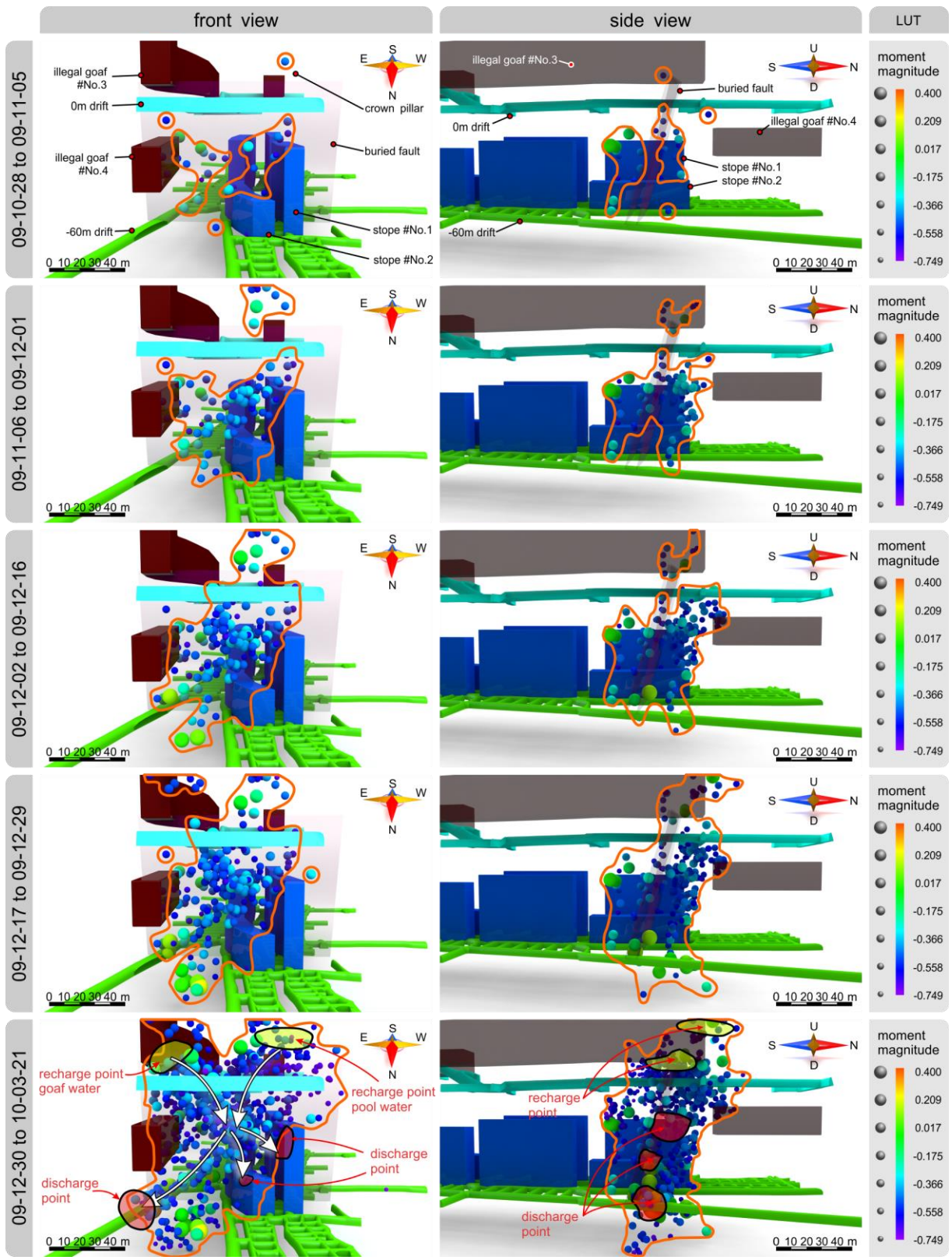


Fig. 7 Spatiotemporal evolution of the MS events

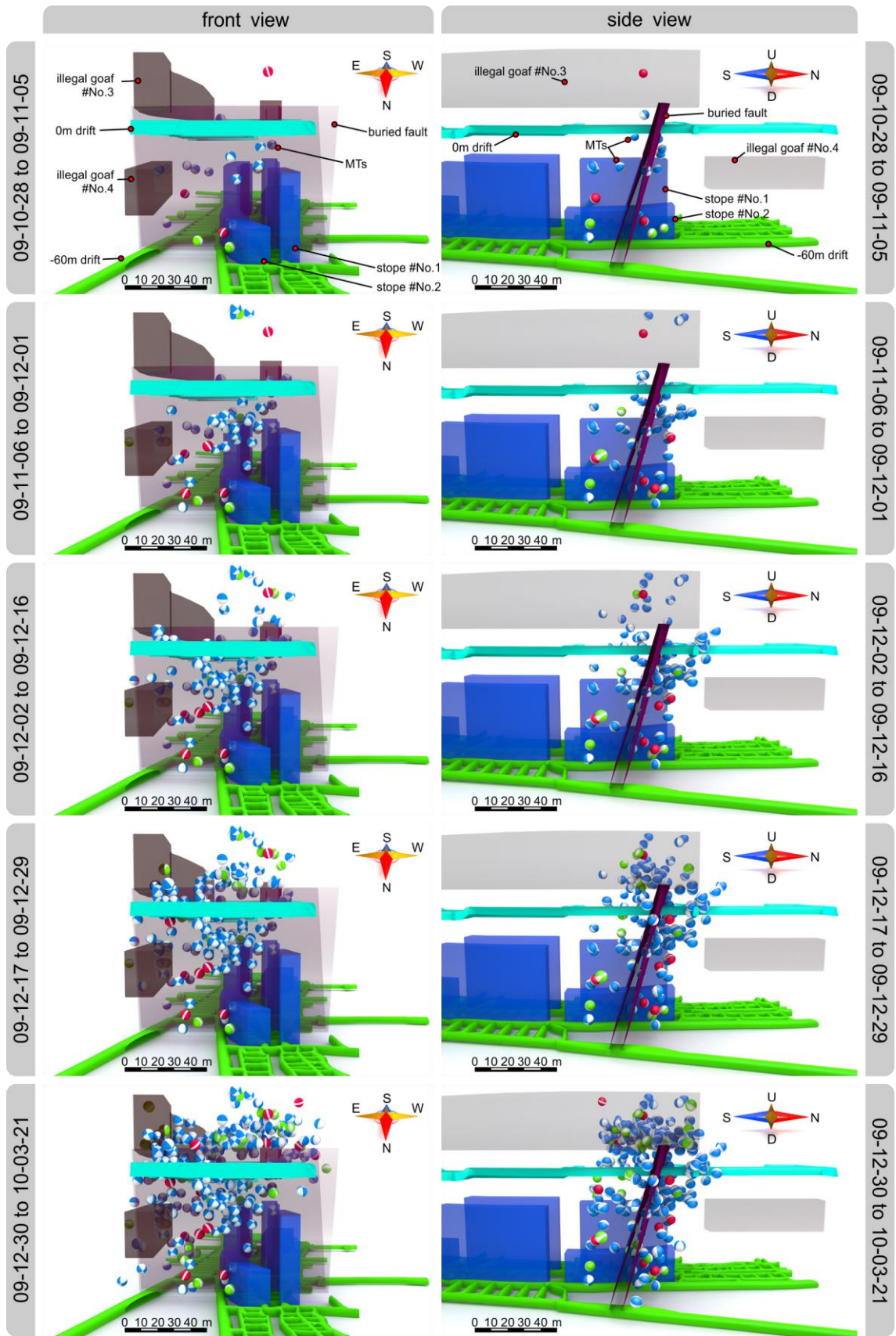


Fig. 8 Spatiotemporal evolution of MT beach balls in the study area. Red, green and blue beach balls represent tensile, mixed-mode and shear fractures, respectively

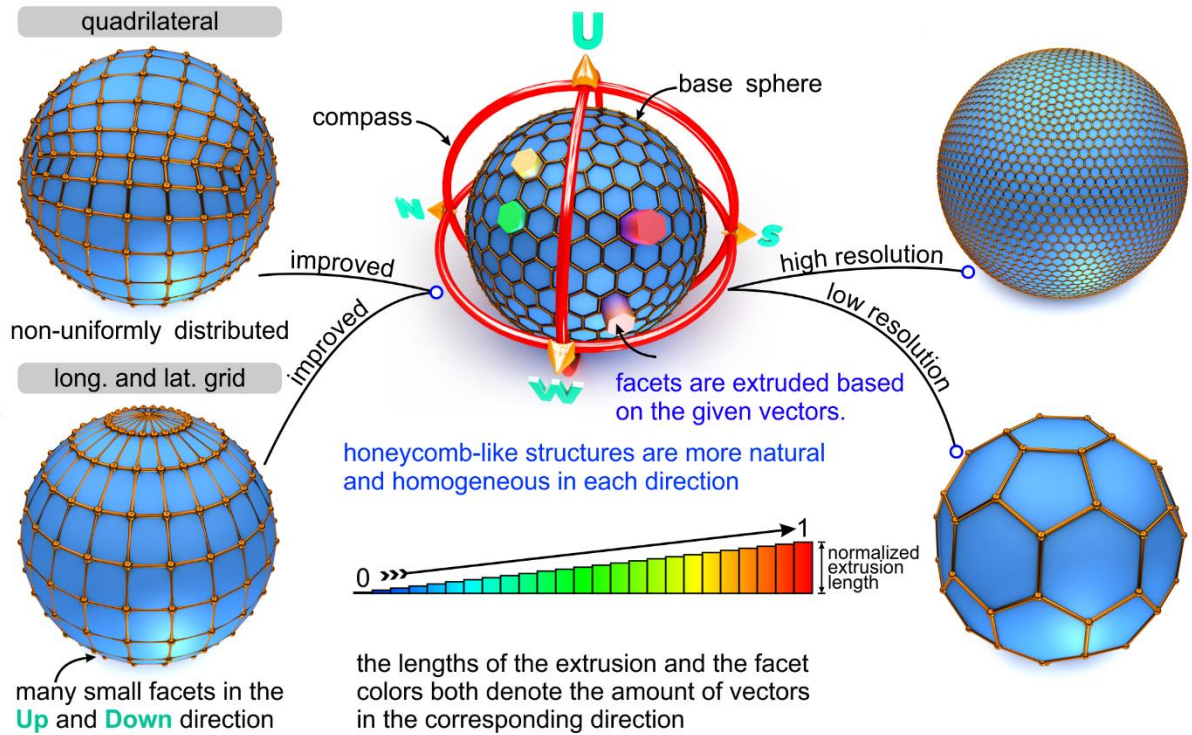


Fig. 9 Illustration of a 3D rose diagram

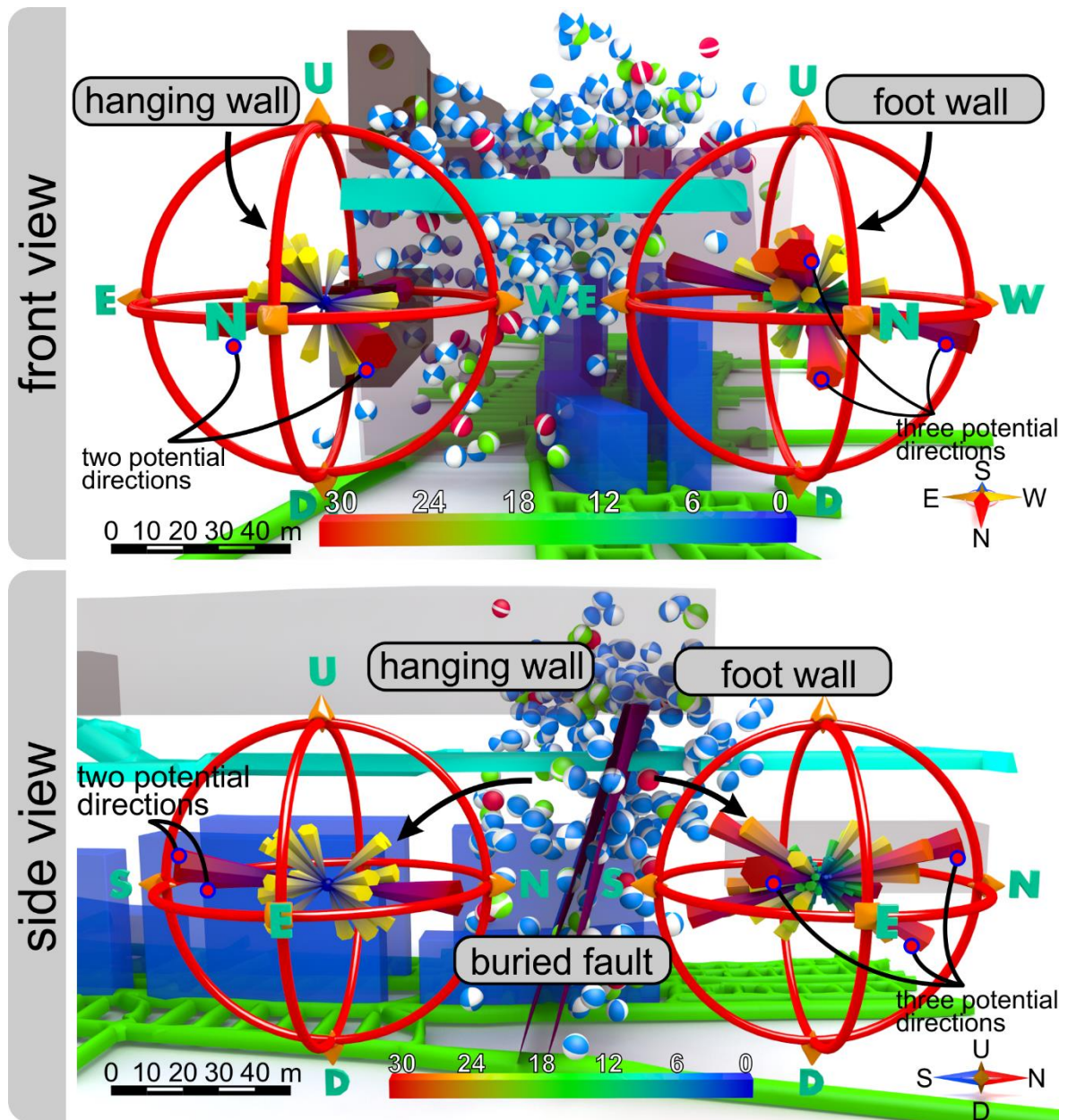


Fig. 10 3D rose diagrams of the normal vectors of fracture surfaces. The left diagram represents the fracture normal distribution in hanging wall, and the right diagram represents fracture normal distribution in the foot wall

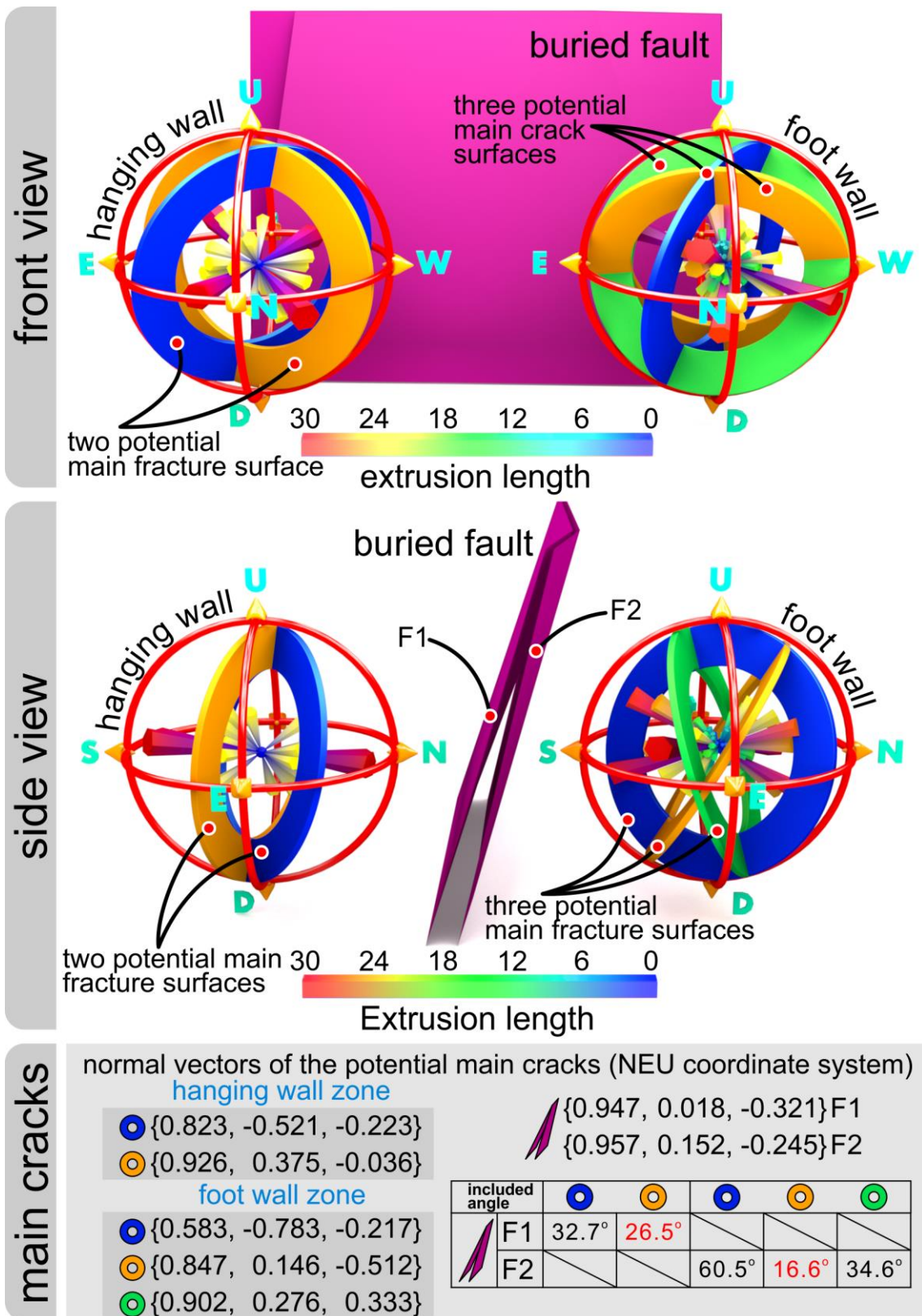


Fig. 11 Determination of the main fracture surfaces on either side of the buried fault

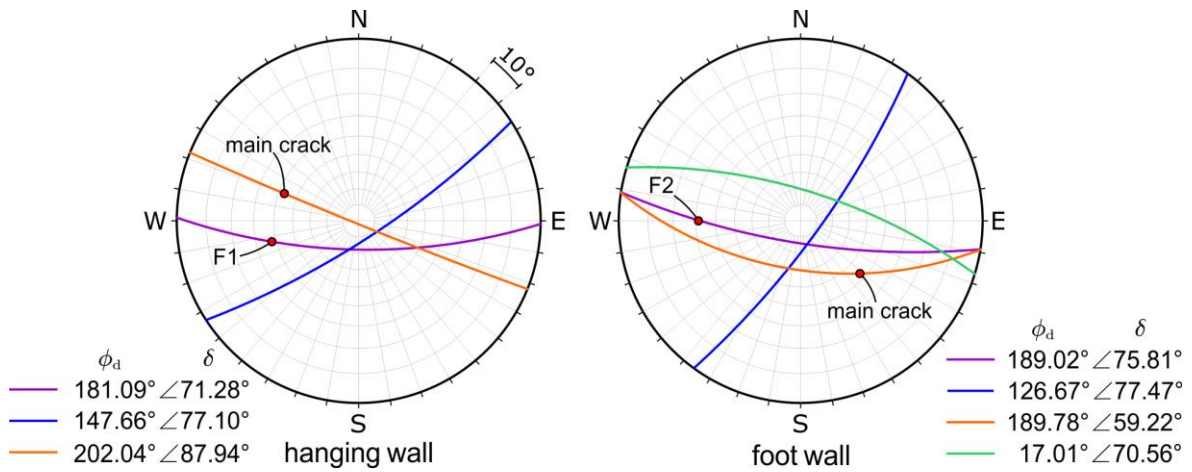


Fig. 12 Stereographic projection of the orientations of the main fractures in the hanging wall (left) and foot wall (right)

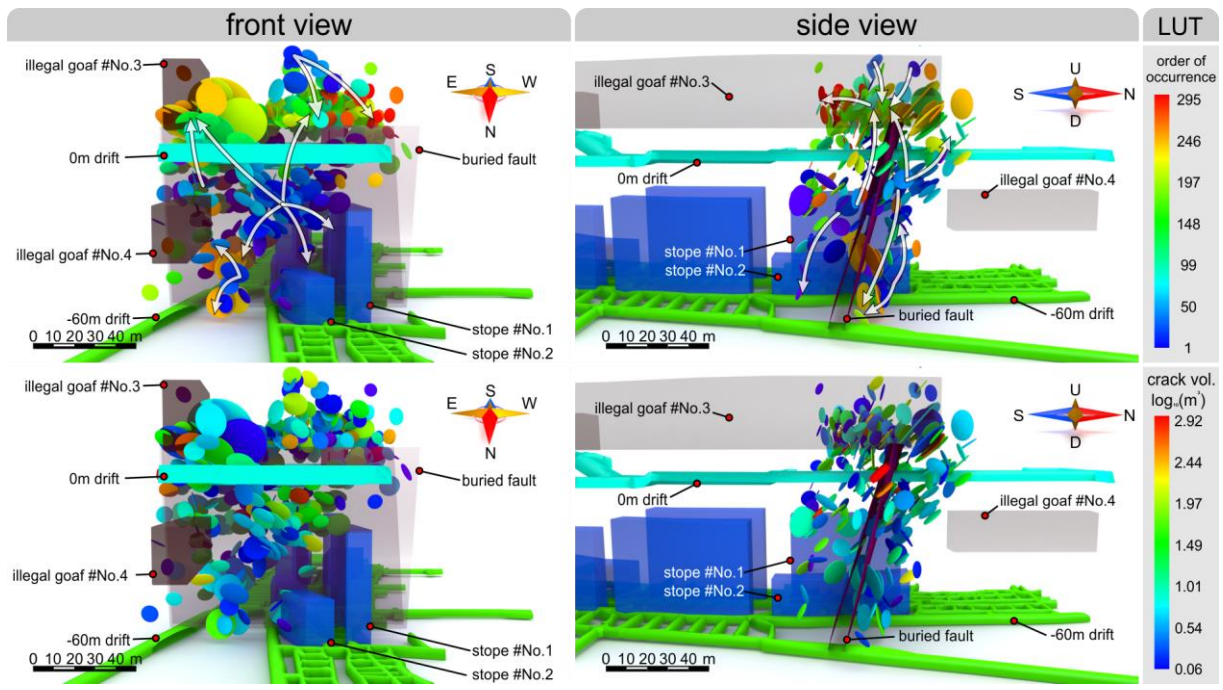


Fig. 13 Microseismic-derived fracture network in the pillars

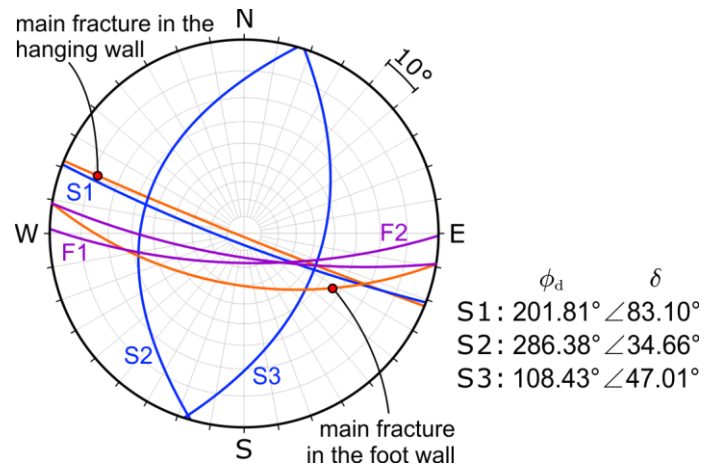


Fig. 14 Stereographic projection of the orientations of the sets of discontinuities S1, S2 and S3 in the pillar

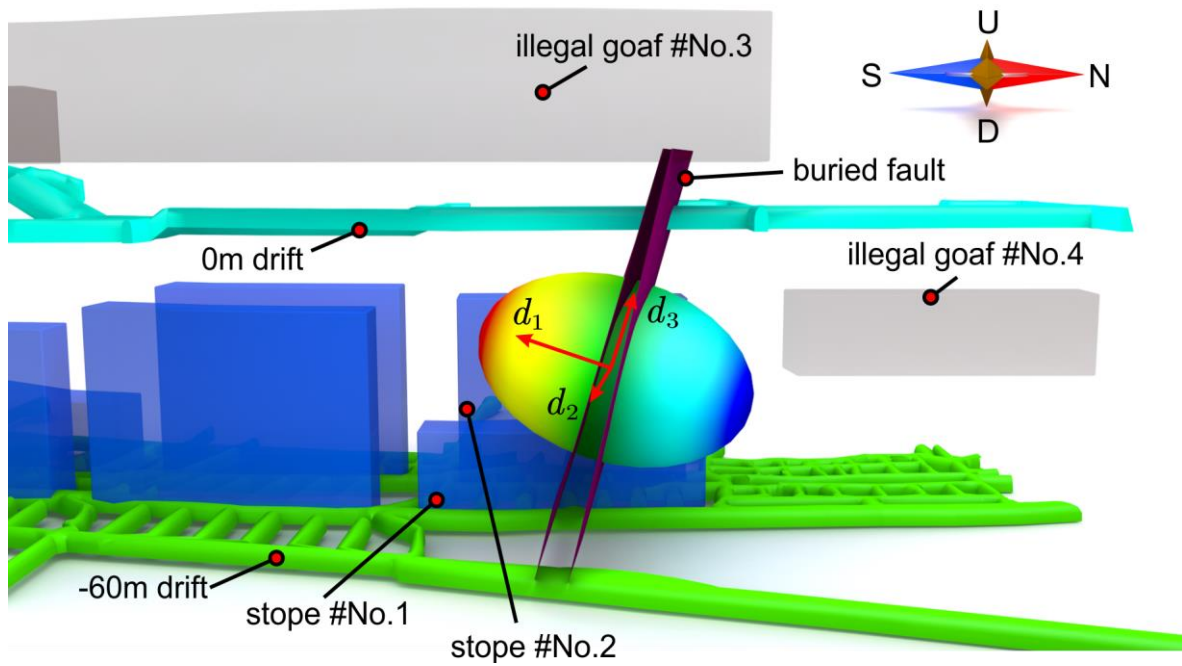


Fig. 15 Damage tensor of the pillar considering microseismic-derived fractures. The ellipsoid illustrates the damage tensor and the red arrows denote the principal directions of the damage tensor

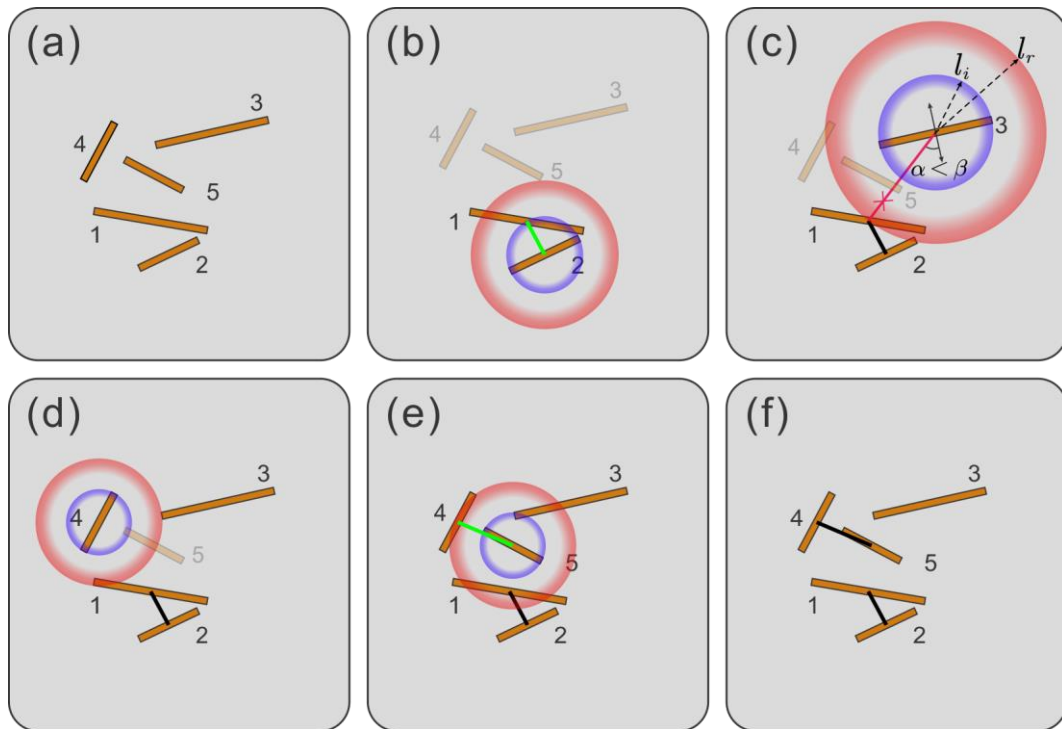


Fig. 16 Schematic view of chronological expansion of event connections. (a) Distribution of MS-derived fractures; (b) Connection within impact distance; (c) The angle is not enough to make a connection; (d) No event found within the receptive distance; (e) Make a connection when the angle criterion is satisfied; (f) Result of a connection network. Impact distance, receptive distance and β in the sketch map are set to source radius r_s , $1.9r_s$ and 70° respectively

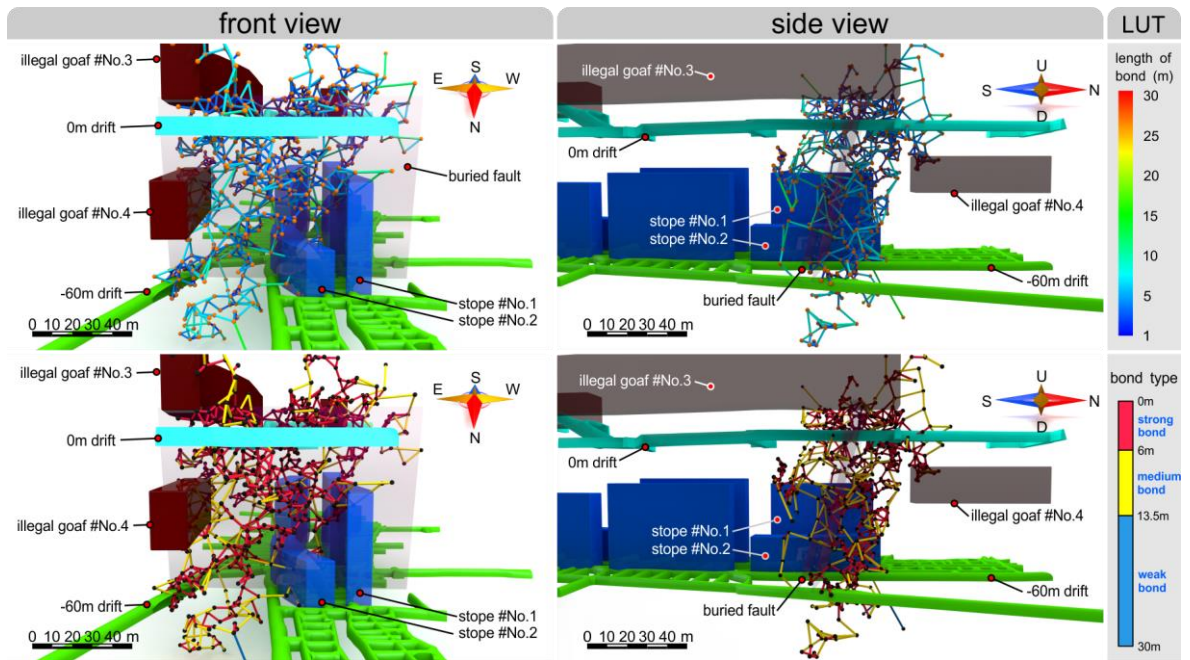


Fig. 17 MS-derived connected network in the pillars

Declaration of competing interest

The authors declared that they have no conflicts of interest to this work.