# Performance Modeling and Comparison of NFV Integrated with SDN: Under or Aside?

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Abstract—Software Defined Networking (SDN) focuses on the separation of data and control plane, while network function virtualization (NFV) decouples network functions from underlying hardware. Combining SDN with NFV would have many benefits, but the problem is how to integrate them. There are two possible architectures for such integration: the controller interacts with virtualized network functions (VNFs), or the switch interacts with VNFs. In this paper, the former is referred to as NFV under the controller (NFV\_C) while the latter is called NFV aside the controller (NFV\_AC). To the best of our knowledge, there is no analytical model for mathematically investigating the performance of such architectures. This paper therefore reports on the analytical modeling of SDN with NFV under or aside the controller. We model and analyze these two SDN+NFV architectures using an M/M/1 queuing model and validate our analysis with various simulations. We show that the analytical results match the simulation results very well. Furthermore, a packet delay reduction of 68.83% can be achieved for NFV\_AC over NFV\_C, meaning that NFV\_AC is a better architecture for integrating SDN with NFV. We also consider feedback from the VNF to the switch. For low loads there is delay increase of 35.42% for high feedback (90%) in comparison with low feedback (10%). In the case of high loads we recorded a delay increase of 66.64%.

Index Terms—Software-defined networking, Network function virtualization, M/M/1 queuing model, OpenFlow.

## I. INTRODUCTION

Traditionally a network is built on dedicated hardware, such as routers and switches, with network software provided by the network vendor. A network engineer's capacity to modify the network software is considerably constrained and is for the most part confined by the network vendor. This has prompted the idea of Software Defined Networking (SDN), where adaptability and dynamism have been presented in the virtualization of the control plane [1]–[4]. The fundamental approach is to separate a network into a control plane and a data plane, which then have the capacity to oversee different network devices centrally. The primary advantage of the SDN concept is the programability of controlling the network devices. This has empowered network engineers to change network configurations and the rationale of data flow as a business requires. A control plane communicates to a data plane through a southbound interface, commonly known as OpenFlow protocol, which was first proposed in [5] and subsequently standardized by the Open Networking Foundation (ONF). Network Function Virtualization (NFV) is however a new approach which deploys or designs various different network functions [6], [7]. It decouples the network functions, so as NAT, DNS caching and so forth from their proprietary hardware appliances, so that they can be executed in virtual machines, enhancing their service quality.

SDN concentrates on the partition of the network control plane from the physical routers' data plane. SDN is dealt with as the control software that sits atop a cluster of physical devices with which it communicates through interfaces. There are several works [8]–[18] on SDN modeling, but none of these has considered NFV in their analytical modeling. On the other hand, NFV is tied with virtualizing various resources into network functions (in software), so that we need not be concerned about any specific physical devices devoted for specific network functions. SDN virtualizes the control plane and configures the data plane, while NFV virtualizes the data plane that are connected to switches.

Recent works [19], [20] have shown that both SDN and NFV can be consolidated to give more centralized control software and generic hardware where the utilities of SDN can be acknowledged through virtualized robust network functions provided by NFV. Two recent works [19], [20] have investigated the performance of coexisting SDN and NFV architecture using simulation and experimentation. However, no analytical model has been developed for the SDN architecture combined with NFV. This work is the *first* to model the architecture that combines SDN with NFV, as well as analyzing its performance.

There are different ways to deal with consolidating SDN with NFV. Since a controller determines which instance of a virtualized network function (VNF) serves the packets which need network functions (NFV packets for short), the NFV packets can be redirected to the controller from the switch. The controller then advances these packets to the proper VNF to execute the required network functions - the NFV packets will pass through the controller. This approach is called SDN with NFV under the controller (NFV\_C). Another approach is that some of the NFV packets are sent to the controller, the controller determines which instance of the VNF will serve these packets, and will set in motion the appropriate actions for the switch. Consequent the NFV packets belonging to the same flow can be directly redirected to the determined instance of VNF without the controller. We term this approach SDN with NFV aside the controller (NFV\_AC).



Fig. 1. Traditional SDN architecture where NFV is under controller.



Fig. 2. SDN architecture where NFV is aside controller.

The fundamental *objective* of this work is to carry out analytical modeling of NFV\_C and NFV\_AC. We also provide a comparison between the two architectures based on the delay of NFV packets. Our work covers: (i) developing the analytical models for the two architectures, (ii) carrying out simulations to validate our analytical model, and (iii) making sensitivity analysis of certain system parameters (such as arrival rates, service rates, etc.) on the performance of these two architectures.

The rest of the paper is organized as follows. In Section II, we briefly explain the two SDN architectures along with related works on SDN modeling; in Section III we present our analytical models for the two SDN architectures, and in Section IV we present the analytical and simulation results. Finally, Section V contains the concluding remarks.

#### II. PRELIMINARIES

Here we briefly explain the two SDN architectures where NFV is under or aside the controller, followed by the current work on SDN modeling.

In the NFV\_C architecture shown in Fig. 1, the controller interacts directly with VNFs. The overall procedure is as follows. First, the NFV packet enters the switch. Then, depending on the action in the flow table, the NFV packet is forwarded to the controller. The controller will determine which instance of

VNF serves it and forwards it to the selected instance. After the NFV packet receives its required network function, it returns to the controller and the controller sends it back the switch. Since the action in the flow table is redirected to the controller, all NFV packets belonging to the same flow will be sent to the controller. The main advantage of this architecture is that NFV packets can be dispatched to different instances of VNF for load balancing.

In NFV\_AC architecture, shown in Fig. 2 [20], the switch interacts directly with VNFs. There is a service chaining module, which selects the proper instances of VNFs and determines the order of chaining. Service chaining module communicates with the controller via northbound interfaces. In this architecture, the controller is responsible for extracting network events, collecting statistics, and analyzing payload to select the proper instances of VNFs and their chaining to support NFV. If table miss of a NFV packet happens, the packet visits the service chaining module through the controller. After receiving a response from the service chaining module, the controller initiates the proper action for the switch and sends this NFV packet back the switch. This packet, experiencing the service chaining module, still needs to go to VNF from the switch to obtain its required network function. Subsequent NFV packets belonging to the same flow can be directly redirected from the switch to determined instances of VNF without the controller. The main advantage of this architecture is that most NFV packets can be directly forwarded to VNF, significantly reducing the controller's loading. However most NFV packets belonging to the same flow will be forwarded to the same instance. Thus the instances of VNFs are not load balanced, resulting in a greater delay in providing network functions. In a real system, there is still a need to have a control plane module on the controller side, doing service chaining to configure the paths among switches and VNF modules for the data plane traffic. The data plane VNF modules of course would be placed to switches on the data plane.

NFV\_C serves as the baseline architecture to see how much NFV\_AC would differ. Many applications would split their functions into control plane placed on the controller side, i.e., as NFV\_C, and data plane placed on the switch side, i.e., as NFV\_AC. If a significant percentage of functions need to be placed as NFV\_C, the performance impact needs to be evaluated. Thus, NFV\_C serves not only as the baseline architecture but also could be used to evaluate the performance impact of functions implemented in the control plane.

## A. Related works on SDN modeling

There have been a few works on the analytical modeling of SDN. In Table I we summarize the key points of such works, together with their methodologies and performances matrices.

First, modeling on SDN was carried out in [8], where feedback orientated queueing theory was used to show the interaction between the control plane and the data plane. In [9], network calculus was used to develop an analytical model of an SDN network. This work developed the buffer size bound and packet delay bound. Mahmood et al. [10] presented an improvement on [8] by modeling SDN as a modified Jackson network. They estimated the packet rate from the controller to the switch, so that the overall packet arrival rate into the switch could actually be obtained. They further extended their previous work to propose an analytical model for the SDN with multiple switches [11]. In this model they calculated the average path delay from the source to the destination, rather than the average packet delay in a switch.

Wang et al. [12] adopted the concept of hierarchicalcontroller architecture, which has a root controller and some local controllers for improving flexibility of the control plane. With this architecture, they analyzed the average packet delay spent in the controllers. However, this paper did not consider switches. On the other hand, Xiong et al. [13] thought that packet arrivals should have batch characteristics, be considered as a Poisson process. Thus, their model is of packet batch arrivals following a Poisson process, with the number of packets in a batch conforming to a Poisson distribution. Finally, they model the behaviors of switches and the controller as the queueing systems  $M^X/M/1$  and M/G/1, respectively.

Bozakov et al. [14] used a queueing model to characterize the behavior of the control interface between the controller and a switch in terms of the number of serviced messages over different time scales, and provided a calculus-based approach to derive an estimate of the corresponding service curves. They also proposed a simple interface extension for controller frameworks which enabled operators to configure time delay bounds for transmitted control messages. However, the model does not consider the feedback between the data plane and the control plane. This shortcoming of feedback modeling is addressed by Azodolmolky et al. [15] who derived a mathematical framework based on network calculus to deal with scalable SDN deployment. Assuming cumulative arriving process at SDN controller, they evaluated the upper bound of the transmission latency and buffer sizing of the root SDN controller.

Goto et al. [16] considered the switches to have two queues: a high-priority queue for those packets sent back from the controller and a low-priority queue for newly-arrived packets from other switches. Those packets coming back from the controller then have a higher priority for delivery in order to reduce their delay. A three-dimensional state (controller's queue length, high-priority queue length, and low-priority queue length) was created to represent this system. The authors derived state transition probabilities and tried to reduce the complexity of obtaining the steady state probability.

Miao et al. [17] proposed a pre-emption-based (PQ system) packet-scheduling scheme to improve the global fairness and reduce the packet loss rate in SDN data plane. They also developed an analytical model to quantitatively evaluate the scheduling scheme and pinpoint performances bottleneck in the SDN architecture. They assumed two queues in the switch: one with low priority (with infinite buffer), and another with high priority (with finite buffer); for controller a M/M/1 queue with finite buffer is used.

TABLE I Related Works on SDN Modeling

Paper	Device	#	Methodology	Performance metric
[8]	Controller	1	M/M/1/k	Avg. packet delay
	Switch	1	M/M/1	Avg. packet delay
[9]	Controller	1	Net. Calculus	Buffer size bound
	Switch	Ν	Net. Calculus	Packet delay bound
[10]	Controller	1	M/M/1	Avg. packet delay
	Switch	1	M/M/1 (adjusted $\lambda$ )	Avg. packet delay
[11]	Controller	1	M/M/1/k	Avg. packet delay
	Switch	Ν	M/M/1	Avg. path delay
[12]	Root controller	1	M/M/1	Avg. packet delay
	Local controller	Ν	M/M/1/k	Avg. packet delay
[13]	Controller	1	M/G/1	Avg. packet delay
[13]	Switch	Ν	$M^X/M/1$	Avg. packet delay
[14]	Controller	1	Net. Calculus	Message delay bound
	Switch	1	Net. Calculus	
[15]	Controller	1	Net. Calculus	Buffer size bound
	Switch	Ν	Net. Calculus	Packet delay bound
[16]	Controller	1	3D state	Avg. packet delay
	Switch	1	(controller, HPQ, LPQ)	Avg. packet delay
				Packet loss prob.
[17]	Controller	1	M/M/1/m	Packet loss probability
	Switch	1	HPQ: M/M/1/m	Avg. packet delay
			LPQ: M/M/1/m	Avg. throughput
[18]	Controller	1	MMPP/M/1	Ave. packet delay
	Switch	1	HPQ: MMPP/M/1	Avg. packet delay
			LPQ: MMPP/M/1/k	Avg. throughput

Miao et al. [18] considered the realistic nature of multimedia traffic and used a Markov Modulated Poisson Process (MMPP) to model a burst of packet arrivals. They also adopted two queues: a high-priority queue and a low-priority queue in the switch, which is similar to that in [16]. They solved this problem by using MMPP/M/1 for the high-priority queue and MMPP/M/1/k for the low-priority queue.

Other than the SDN modeling papers [8]–[18] listed in Table I, there are a few works which had performed SDN implementations and simulations, no mathematical analyses were performed. Kuo et al. [21] considered a service chain consisting of a sequence of virtualized network functions (VNFs). They showed that the process overhead on a computation node is linear to the total amount of flows processed. They have considered flow based arrival and developed an approximation algorithm of service chain embedding. Hawilo et al. [22] considered a NFV framework and examined the challenges and prerequisites of its use in cellular networks by proposing virtual environment. They proposed a criterion to bundle different functions of a virtualized evolved packet core in a single physical device or a group of adjacent devices to decrease signaling traffic and accomplish better performance. Muhammad et al. [23] explained technologies, architectures, applications, underlying protocols, and deployments of SDN network. Omnes et al. [24] proposed a multi-layered IoT architecture involving SDN and NFV to cope with different challenges in IoT ecosystem. Ferrús et al. [25] explained how SDN/NFV technologies can be collaborated with satellite communications in order to implement 5G. In the satellite ground segment domain, they proposed three scenarios and showed the possibilities of improvement after introducing SDN/NFV technologies. Basta et al. [26] explained the functions placement problem within a widely-spanned mobile network. An NFV deployment with all functions virtualized will be helpful for some areas of the mobile network, while for other areas, an SDN deployment with functions decomposition is more favorable in terms of load and delay. They proposed a model to deal with functions placement problem and minimize load overhead of transport network. Yuan et al. [27] explained that in terms of performance and scalability a single controller of SDN has many drawbacks. They investigated the detailed design architectures of SDN with multiple controllers and benefits and challenges of multiple controllers. Lorenz et al. [28] explained that dynamic resource allocation of the network can cause serious security issue. For enterprise networks, they proposed different architectural design patterns which provide a SDN/NFV-based security solutions. Rahim et al. [29] investigated the three planes of SDN such as data plane, control plane and application plane and examined the challenges and the latest technologies related to SDN. Deval et al. [30] demonstrated the importance of service function chaining(SFC) as a major enabler for NFV and its importance to improve the performance of NFV. They also developed optimization strategies for SFC architecture providing a flexible and economical approach.

However, none of the SDN modeling works [8]–[18] considered both SDN and NFV in their models. In this paper, we have developed analytical models for combining SDN with NFV. To the best of our knowledge, this work is the *first* that considers the presence of NFV while modeling the performance of SDN.

## III. SYSTEM MODEL

We have used classical queueing theory to develop mathematical models for the NFV\_C (case I) and NFV\_AC (case II). The queueing model of NFV\_C is shown in Fig. 3, where it has three M/M/1 queues. For NFV\_AC the model has four queues, as shown in Fig. 4.

The flow of NFV packets in the two SDN architectures are illustrated through the phase diagrams in Fig. 5 and Fig. 6. These show the way a NFV packet progresses through the system in two cases.  $T_s$ ,  $T_c$ ,  $T_f$  and  $T_{sc}$  represent the average packet delay at the switch, controller, VNF and service chaining module, respectively.

## A. Assumptions and Notations

Following are the assumptions of the model:

• The data arrival process at a switch is a Poisson process.



Fig. 3. Case I: queueing model for NFV\_C.



Fig. 4. Case II: queueing model for NFV\_AC.

- The service time of packets in a switch, controller and VNF are assumed to follow exponential distributions.
- For switch, controller, VNF and service chaining module, the queue size is infinite.

For the analytical model we consider M/M/1 queues for switch, controller, VNF and service chaining module independently, but arrival rates of these queues depend on the feedback of other queues.

The notations used in the analysis are listed in Table II. To denote different parameters, we have used superscript 1 and 2 for NFV\_C and NFV\_AC, respectively. Moreover, we have used subscript X to indicate devices where X can be replaced by s, c, f and sc for switch, controller, VNF and service chaining module, respectively.



Fig. 5. Phase diagram of delays for NFV packets for NFV\_C.

TABLE II Notations Used in the Analysis

Symbol	Parameter Name		
$\lambda_0$	Arrival rate of packets at the switch		
$\Lambda_X^{(1)}$	Total arrival rate at X $\epsilon$ {s, c, f} for NFV_C		
$\Lambda_X^{(2)}$	Total arrival rate at X $\epsilon$ {s, c, f, sc} for NFV_AC		
$P_c$	The probability of redirecting to the controller from switch		
$P_{nfv}$	Probability that a packet will require service from VNF module		
$P_t$	The probability of redirecting to the switch from VNF module		
$\mu_s$	Service rate at switch		
$\mu_c$	Service rate at controller		
$\mu_f$	Service rate at VNF		
$\mu_{sc}$	Service rate at Service chaining module		
$T_X^{(1)}$	Average Packet delay at X $\epsilon$ {s, c, f} for NFV_C		
$T_X^{(2)}$	Average Packet delay at X $\epsilon$ {s, c, f, sc} for NFV_AC		
$T_{Total}^{(1)}$	Average packet delay of NFV packets for NFV_C		
$T_{Total}^{(2)}$	Average packet delay of NFV packets for NFV_AC		



Fig. 6. Phase diagram of delays for NFV packets for NFV\_AC.

# B. Analysis for NFV\_C

To calculate the average packet delay for NFV packets, we first calculate the average packet delay in different queues. For a packet requiring NFV service, at first the packet will arrive at the switch. From there, the packet will go to the controller. If the packet requires service from the VNF module, the packet will be forwarded to the VNF module from the controller. From VNF module, the packet will return back to the controller and finally from the controller, it returns to the switch.

Fig. 3 shows two types of packets entering the switch: (i) new packets arriving at the switch, and (ii) packets that are redirected from the controller go back to the switch. For the former, the packet arrival rate is  $\lambda_0$ , and for the latter, it can be carefully obtained as follows.

First, we obtain the arrival rate of NFV packets as  $P_{nfv}\lambda_0$ , because the probability of packets requiring a network function is assumed to be  $P_{nfv}$ ; then, the rate of packets sent to the controller from the switch (as a result of table miss) is  $P_c\lambda_0$ . However, these two rates slightly overlap because some NFV packets encounter table miss. Thus, we should subtract the probability of their intersection. Therefore, total arrival rate sent from the switch to the controller is  $(P_c + P_{nfv} - P_c P_{nfv})\lambda_0$ . This rate is also the rate sent from the controller to the switch because we assume, the controller has an infinite buffer having no loss. Some packets will go to the VNF module from the controller, but those packets will eventually return to the controller from VNF module. Finally, packets will return to the switch. Hence, we have obtained that all the packets that entered the controller from the switch will return to the switch after visiting the controller. Finally, the total packet rate entering into the switch is expressed as follows:

$$\Lambda_{s}^{(1)} = \lambda_{0} + (P_{c} + P_{nfv} - P_{c}P_{nfv})\lambda_{0}$$
  
= (1 + P\_{c} + P\_{nfv} - P\_{c}P\_{nfv})\lambda\_{0}. (1)

As switch is a M/M/1 queue, average packet delay at switch can be derived using the total arrival rate at switch,  $\Lambda_s^{(1)}$ , and service rate at switch,  $\mu_s$ , as

$$T_s^{(1)} = \frac{1}{\mu_s - (1 + P_c + P_{nfv} - P_c P_{nfv})\lambda_0}.$$
 (2)

Some of the packets from the controller will enter the VNF module. The probability of packets requiring a network function is assumed to be  $P_{nfv}$ . Hence, total arrival rate at VNF is as

$$\Lambda_f^{(1)} = P_{nfv}\lambda_0. \tag{3}$$

Therefore, packet delay at VNF can be expressed as

$$T_f^{(1)} = \frac{1}{\mu_f - P_{nfv}\lambda_0}.$$
(4)

For the controller, packet arrival occurs in two ways. First, some packets from switch enter the controller. Second, all the packets leaving VNF enter the controller queue. The former has a rate  $(P_c + P_{nfv} - P_c P_{nfv})\lambda_0$ , as described above. The latter is  $P_{nfv}\lambda_0$ . Combining the two cases, the total arrival rate at controller can be written as

$$\Lambda_{c}^{(1)} = (P_{c} + P_{nfv} - P_{c}P_{nfv})\lambda_{0} + P_{nfv}\lambda_{0}$$
  
=  $(2P_{nfv} + P_{c} - P_{c}P_{nfv})\lambda_{0}.$  (5)

As the controller is a M/M/1 queue, packet delay at controller can be calculated as

$$T_c^{(1)} = \frac{1}{\mu_c - (2P_{nfv} + P_c - P_c P_{nfv})\lambda_0}.$$
 (6)

Since each NFV packet has to visit switch and controller queue twice and VNF module queue once, we can calculate average packet delay for NFV packets using Eqns. (2), (4) and (6) as

$$T_{Total}^{(1)} = 2T_s^{(1)} + 2T_c^{(1)} + T_f^{(1)}.$$
 (7)

# C. Analysis for NFV\_AC

In case of NFV\_AC, at first NFV packets (requiring NFV service) enters the switch. If there are no information about the packet in the switch (which means table miss for NFV packets), then the packet will be forwarded to the controller. The packet will visit the service chaining module through the controller. After receiving a response from the service chaining module, the controller initiates the proper action for the switch and sends this NFV packet back to the switch. This packet, experiencing the service chaining module, still needs

to go to VNF (from the switch) to obtain its required network function. Subsequent NFV packets belonging to the same flow can be directly redirected from the switch to determined instances of VNF (without invloving the controller). If there are information about a NFV packet in the switch (that is, table hit for NFV packet), the packet will directly go to the VNF module from the switch. Some of the NFV packets will return to switch from the VNF module after getting required network function.

As shown in Fig. 4, there are three types of packets that enter the switch: (i) new packets to the switch, (ii) packets that are redirected from the controller, and (iii) packets that are redirected from the VNF module. After getting service from VNF module, some packets may return to network (switch) again, depending on the value of  $P_t$ . For the former, the packet arrival rate is  $\lambda_0$ , and for the latter, it can be carefully obtained as follows. From the switch depending on characteristic some packet will go the controller, some will go to the VNF module and some packet will leave the switch after service. As the probability of going to the controller is  $P_c$ . Therefore, arrival rate from switch to controller is  $P_c \lambda_0$ . Since controller and service chaining module have infinite buffer, all the packets that enter the controller will return to the switch. All those packet that do not need service from controller but need service from VNF module will directly enter the VNF module from switch with a rate of  $P_{nfv}(1-P_c)\lambda_0$ . After visiting the controller some packet will be directed to the VNF module from the switch at a rate of  $P_{nfv}P_c\lambda_0$  (These packets need service from both controller and service chaining module). From VNF module some packet will return to the switch at the probability of  $P_t$ . As total arriving rate of the VNF module is  $P_{nfv}\lambda_0$ , the rate at which packets will be redirected from the VNF to the switch is  $P_t P_{nfv} \lambda_0$ . Therefore, total arrival rate at switch can be calculated as

$$\Lambda_s^{(2)} = \lambda_0 + P_c \lambda_0 + P_t P_{nfv} \lambda_0$$
  
=  $(1 + P_c + P_t P_{nfv}) \lambda_0.$  (8)

Therefore, average packet delay at switch can be expressed as

$$T_s^{(2)} = \frac{1}{\mu_s - (1 + P_c + P_t P_{nfv})\lambda_0}.$$
(9)

It is easily observed that the arrival rate of NFV packets,  $\Lambda_f^{(2)}$ , is

$$\Lambda_f^{(2)} = P_{nfv} P_c \lambda_0 + P_{nfv} (1 - P_c) \lambda_0$$
  
=  $P_{nfv} \lambda_0.$  (10)

Therefore, average packet delay at VNF for NFV\_AC can be expressed as

$$T_f^{(2)} = \frac{1}{\mu_f - P_{nfv}\lambda_0}.$$
(11)

The packets that need processing from the controller have to be sent to it from the switch. Also the packets departing from the service chaining module will enter the controller's queue again. Combining these two cases, the total arrival rate at controller can be written as

$$\Lambda_c^{(2)} = P_c \lambda_0 + P_c P_{nfv} \lambda_0$$
  
=  $(1 + P_{nfv}) P_c \lambda_0.$  (12)

As the controller is a M/M/1 queue, packet delay at controller can be calculated as

$$T_c^{(2)} = \frac{1}{\mu_c - (1 + P_{nfv})P_c\lambda_0}.$$
(13)

In Fig. 4, service chaining module is connected to the controller and NFV packets will visit it depending on the probability  $P_{nfv}$ . The arrival rate of the service chaining module can be expressed as

$$\Lambda_{sc}^{(2)} = P_c P_{nfv} \lambda_0. \tag{14}$$

Therefore, average packet delay at service chaining module can be expressed as

$$T_{sc}^{(2)} = \frac{1}{\mu_{sc} - P_c P_{nfv} \lambda_0}.$$
 (15)

Using Eqns. (9), (11), (13) and (15), we can calculate the average packet delay for NFV packets as

$$T_{Total}^{(2)} = P_c(2T_s^{(2)} + 2T_c^{(2)} + T_{sc}^{(2)} + T_f^{(2)}) + (1 - P_c)(T_s^{(2)} + T_f^{(2)}) + P_t T_s^{(2)} = (1 + P_c + P_t)T_s^{(2)} + 2P_c T_c^{(2)} + P_c T_{sc}^{(2)} + T_f^{(2)}.$$
(16)

 TABLE III

 BASELINE PARAMETERS FOR THE ANALYSIS AND SIMULATION

Parameter Name	Value
Probability of redirecting to controller, $P_c$	0.04
Probability of redirecting to NFV, $P_{nfv}$	0.5
Probability of redirecting to	0.5
the switch from VNF module, $P_t$	
Arrival Rate at the Switch, $\lambda_0$	55000 pkts/sec
Service rate at switch, $\mu_s$	100000 pkts/sec
Service rate at controller, $\mu_c$	70000 pkts/sec
Service rate at NFV, $\mu_f$	95000 pkts/sec
Service rate at service chaining, $\mu_{sc}$	85000 pkts/sec

## IV. RESULTS

In order to validate our analytical model, we have implemented a custom simulator. For simulation we do not create independent packets for each queue. A new packet arrives only at a switch following Poisson distribution and then, depending on different probability and feedback result, it goes to the controller or the NFV. We used an event queue from which we pop different queueing events and execute them. We have created a packet class. For each packet, we keep track of its delay in different queues.

In this section, we present the analytical and simulation results for NFV\_C and NFV\_AC by varying different system parameters, including the probability of redirecting from switch to controller,  $P_c$ , service rate at VNF,  $\mu_f$ , the probability of NFV packets,  $P_{nfv}$  and arrival rate at the Switch,  $\lambda_0$ . We have chosen a set of parameters as baseline parameters listed in Table III and varied one at a time while keeping others fix to prove the correctness of our model. To the best of our knowledge, there exists no previous work that discusses the baseline parameters of SDN and NFV while modeling SDN. However, we used the baseline parameters similar to [31] where the author reported that in a typical OpenFlow network, the probability of new flow arrival is about 4%. Since all the packets of a network do not require service from NFV, we assume 50% packets ( $p_{nfv} = 0.5$ ) will require service from NFV module. We also assume, after getting service from VNF module 50% packets ( $p_t = 0.5$ ) will return to the switch. For simulation, 1.5 million packets are generated for stability. Our main goal is to observe the impact of different parameters in the network. As we used closed formed equation of delay of a M/M/1 queue for analytical purpose, we tried to make sure all parameters satisfy the queueing property.

## A. Comparing NFV\_C with NFV\_AC

1) Impact of  $P_c$ : Fig. 7 shows the impact of  $P_c$  on the average packet delay of NFV packets. We found that the analytical results match the simulation results, irrespective of the architecture: NFV\_C or NFV\_AC. This means our model and analysis can correctly emulate real conditions. Also, we observed that packet delay increases with an increase in  $P_c$ ; the more packets sent to the controller, the heavier the load on the controller, resulting in a longer packet delays. Comparing NFV\_C with NFV\_AC, the packet delay for NFV\_AC is much shorter than that for NFV\_C, largely for three reasons. First, each NFV packet in NFV\_C has to enter the controller, and then goes to the VNF, and finally returns to the switch via the controller. This is a longer route for NFV packets in NFV\_C, compared to that in NFV\_AC. Second, more packets enter the controller in NFV\_C than in NFV\_AC. We can see that the arrival rate of packets entering the controller is  $(2P_{nfv} + P_c - P_c P_{nfv})\lambda_0$ , which is much larger than  $(1 + P_{nfv})P_c\lambda_0$  in NFV\_AC. The heavier the load the controller has, the longer the delay packets experience in the controller. Third, more packets sent to the controller from the switch represent more packets sent back to the switch. Although there is feedback from the VNF module to the switch for NFV\_AC, the arrival rate in switch for NFV\_C is also larger than that for NFV\_AC. We can easily see this from Eqs. (1) and (8) for our baseline parameters. The arrival rate in switch for NFV\_C is  $(1 + P_c + P_{nfv} - P_c P_{nfv})\lambda_0$ , which is larger than that for NFC\_AC,  $(1 + P_c + P_t P_{nfv})\lambda_0$  because we have considered the default value of  $P_t$  as 0.5, and to observe the impact of  $P_c$  we changed the value from 0.01 to 0.3. For our baseline configuration there is a delay reduction of 68.83% for NFV\_AC over NFV\_C. The service rate of the controller plays an important role when comparing the two



Fig. 7. Average packet delay of NFV packets vs.  $P_c$ .

different models. A large portion of the delay for NFV\_C is introduced by the controller. If we consider a larger service rate for the controller, then the difference between the two models will decrease.

2) Impact of Service rate at VNF,  $\mu_f$ : Fig. 8 shows the impact of service rate at VNF,  $\mu_f$ , on the average packet delay of NFV packets. For both cases, the analytical results match the simulation results very closely. We found that NFV\_AC performs better than NFV\_C because of the three reasons described above. The delay gap between NFV\_C and NFV\_AC is constant because  $\mu_f$  only affects the packet delay in the VNF module. However, the packet arrival rates for NFV C and NFV AC are the same, meaning that the packet delays in VNF are also the same for both, irrespective of the value of  $\mu_f$ . This can be proved from Eqs. (4) and (11) because they have the same formula. The gap is caused by the packet delay differences in the controller, switch, and the service chaining model, but it is not affected by  $\mu_f$ . It can also be seen from Fig. 8 that, with the increase of the service rate at VNF, there is little variation for either of the models. From this we can get an idea of how network vendors should design a VNF module. Usually fewer packets will enter into VNF module compare to a switch and controller.

3) Impact of  $P_{nfv}$ : Fig. 9 shows the impact of  $P_{nfv}$  on the average packet delay of NFV packets. We found that the analytical result matches the simulation results, verifying the correctness of our analysis. we also observed that the average packet delay increases with an increase in  $P_{nfv}$ . As described above,  $\mu_f$  will not affect the gap between NFV\_C and NFV\_AC. However,  $P_{nfv}$  actually affects this gap because a larger  $P_{nfv}$  means more packets sent to the controller, especially for NFV\_C. That causes that the packet delay for NFV\_AC.

4) Impact of  $\lambda_0$ : Fig. 10 shows the impact of  $_0$  on the average packet delay of NFV packets. We found that the



Fig. 8. Average packet delay of NFV packets vs.  $\mu_f$ .



Fig. 9. Average packet delay of NFV packets vs.  $P_{nfv}$ .

analytical result matches the simulation results, confirming the accuracy about our work. We could also see that the average packet delay increases with an increase of  $\lambda_0$ , and with an increase in the arrival rate at a switch, the load at both switch and controller will also increase. In the case of NFV\_C the load at the controller will much higher than for NFV\_AC. Our calculations show that for low arrival rates there is delay reduction of 54.02% for NFV\_AC compared to NFV\_C. For higher arrival rates NFV\_AC performs even better. On average there is delay deduction of 72.6% for NFV\_AC over NFV\_C. Arrival rates at a switch should be one of key concerns in the design of the network equipment. For better performance, in all our experiments the service rate of the switch was almost double of the arrival rate. As there are feedbacks from the controller and VNF module, total arrival rate becomes very



Fig. 10. Average packet delay of NFV packets vs.  $\lambda_0$ .

high. To hold the queuing property, service rate must be higher than total arrival rate.

## B. The impact of $P_t$ on NFV\_AC

In this section, we will observe the impact of  $P_t$  on NFV aside the controller model. We use three values for  $P_t = \{0.1, 0.5, 0.9\}$  for both analytical and simulation purpose. Other parameters are same as baselines values listed in Table III

1) Impact of  $P_c$ : Fig. 11 shows the impact of  $P_c$  and  $P_t$  on the average packet delay of NFV packets when NFV is aside the controller. We found that the analytical results coordinate the simulation results. This implies that our model and analysis can successfully emulate practical conditions. We also observed that packet delay increases with the increase in  $P_c$ . More packets sent to the controller result in a heavier load on the controller, resulting in greater packet delays. For NFV\_AC, we have a total of 4 queues. If we observe the arrival rate of these four queues from Eqs. (8), (10), (12) and (14), we see  $P_t$  has an impact only on the arrival rate of the switch. For a high value of  $P_t$ , the load on the switch will be very high. An increase in the rate for high  $P_t$  is much faster than the increase rate for low  $P_t$ . In the case of a low  $P_t$ , the load at switch is not very high. For a low value of  $P_c$  there is a delay increase of 61.79%, comparing low feedback  $P_t = 0.1$ with high feedback  $P_t = 0.9$ . In case of a high value of  $P_c$ this delay is very high (82.95%). If we consider high feedback from VNF to the switch, then the service rate of the switch must be very high. We observed another issue here, that the arrival rate of the switch must be comparatively lower then the service rate of the switch. In our model we considered an arrival rate of the switch of 55000 pkts/sec but a service rate of the switch of 100000 pkts/sec. Main reason behind this is - As we are considering high feedback ( $P_t = 0.9$ ), then the total arrival rate at the switch (new packet, feedback



Fig. 11. Average packet delay of NFV packets vs.  $P_{sc}$  (Varying  $P_t$ ).

from VNF and feedback from controller) becomes very high. If we consider a low service rate for the switch then M/M/1 property of the switch can become violated. While designing the switch network vendors should calculate the upper-limit of the arrival rate at the switch and check wether it holds the M/M/1 property or not.

2) Impact of Service rate at VNF,  $\mu_f$ : Fig. 12 shows the impact of the service rate at NFV,  $\mu_f$  and  $P_t$  on the average packet delay of NFV packets when NFV is aside the controller. For all cases, the analytical results match the simulation results very closely. The delay gaps between different  $P_t$  lines are constant because  $\mu_f$  only affects the packet delay differences in the switch, as for high  $P_t$  large number of packet will be forwarded to switch from VNF. Other than that, all other parameters will remain same. We also observed that the average packet delay of the NFV packets decreases with the increase of service rate at NFV.

3) Impact of  $P_{nfv}$ : Fig. 13 shows the impact of  $P_{nfv}$  and  $P_t$  on the average packet delay of NFV packets when NFV is aside the controller. We found that the analytical results again matched the simulation results, verifying the correctness of our analysis. We also observed that the average packet delay increases with the increase of  $P_{nfv}$ , regardless of  $P_t$ . For high values of  $P_t$ , the increase in rate is much higher, because for high  $P_t$  many packet will be returned to the switch from VNF, which will cause traffic in the switch and increase the total delay. If both  $P_{nfv}$  and  $P_t$  is high, it means a large portion of the packets will need service from VNF and from there a large portion will be returned to the switch. Since both are very high, this will cause a considerable delay.

4) Impact of  $\lambda_0$ : Fig. 14 shows the impact of  $\lambda_0$  and  $P_t$  on the average packet delay of NFV packets when the NFV is aside the controller. We again found that the analytical result match the simulation results, verifying the correctness of



Fig. 12. Average packet delay of NFV packets vs.  $\mu_f$  (Varying  $P_t$ ).



Fig. 13. Average packet delay of NFV packets vs.  $P_{nfv}$  (Varying  $P_t$ ).

our analysis. Furthermore, we also observed that the average packet delay increases with an increase of  $\lambda_0$  regardless of  $P_t$ . For high values of both  $\lambda_0$  and  $P_t$  the total load at the switch is very high as there are many new packets and large number of packets are send from the VNF module, which causes a large overall delay. If we consider a large number of feedbacks then we should not allow large numbers of new packets. For low loads there is a delay increase of 35.42%, comparing low feedback  $P_t = 0.1$  with high feedback  $P_t = 0.9$ . In the case of high load this number is very high (66.64%).

### V. CONCLUSION AND FUTURE WORKS

In this paper, we have presented models for two SDN architectures combined with NFV. The analysis for packet delay of NFV packets is derived using an M/M/1 model. Extensive



Fig. 14. Average packet delay of NFV packets vs.  $\lambda_0$  (Varying  $P_t$ ).

simulations were conducted to verify our analysis. Results show that analytical results very closely match simulation results, supporting the correctness of our model and analysis. The packet delay for NFV\_AC is significantly less than that for NFV\_C. We recorded a significant delay reduction of 68.83% for NFV\_AC compared to NFV\_C, for three reasons: a shorter route, a smaller controller load, and a smaller switch load.

The service rate at VNF,  $\mu_f$ , does not affect the delay gap between NFV\_AC and NFV\_C because packet delays in VNF are the same for both. On the other hand, the probability exists that NFV packets,  $P_{nfv}$ , will have some effect. A large  $P_{nfv}$ will cause a larger gap in packet delay between NFV\_AC and NFV\_C because switch and controller become more congested for NFV\_C.

If there is a feedback from the VNF to switch for NFV\_AC, then with a high value of  $P_t$ , the delay of NFV packets will increase compare to low value of  $P_t$ . As for high  $P_t$  arrival rate at switch will increase, which will cause an overall delay. While designing a switch, network vendors should concentrate on the upper limit of the arrival rate of the switch. If total arrival rate becomes very high it may violate the M/M/1 property of the switch.

Although NFV\_AC is obviously better than NFV\_C in our model, our model assumes VNF has the same capacity to serve packets. In a real environment, NFV\_C has more flexibility to select a lightly-loaded instance to serve NFV packets to reduce packet delay in VNF. This scenario will be further investigated in the future. Besides, Poisson is not realistic compared to more sophisticated arrival models, such as MMPP. But given the combined complexity of the system model, using MMPP would not give us computational affordability. As this is the first work on the modeling of both SDN and NFV, we would leave this as a future work.

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