Perception and Steering Control in Paired Bat Flight

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Abstract: Animals within groups need to coordinate their reactions to perceived environmental features and to each other in order to safely move from one point to another. This paper extends our previously published work on the flight patterns of Myotis velifer that have been observed in a habitat near Johnson City, Texas. Each evening, these bats emerge from a cave in sequences of small groups that typically contain no more than three or four individuals, and they thus provide ideal subjects for studying leader-follower behaviors. By analyzing the flight paths of a group of M. velifer, the data show that the flight behavior of a follower bat is influenced by the flight behavior of a leader bat in a way that is not well explained by existing pursuit laws, such as classical pursuit, constant bearing and motion camouflage. Thus we propose an alternative steering law based on virtual loom, a concept we introduce to capture the geometrical configuration of the leader-follower pair. It is shown that this law may be integrated with our previously proposed vision-enabled steering laws to synthesize trajectories, the statistics of which fit with those of the bats in our data set. The results suggest that bats use perceived information of both the environment and their neighbors for navigation.

Keywords: Bio control; Vision-based control; Robotics; Numerical simulation; Group behaviors

1. INTRODUCTION

For a group of animals navigating through a cluttered environment, each individual must utilize sensory cues from both the environment and its neighbors in order to coordinate its motion with the neighbors and achieve effective navigation. A superb example of group navigation is bats emerging from their roost in groups shortly after sunset and flying through a wooded flight corridor to reach their forage ground. Kong et al. (2013) analyzed data recovered from a large collection of video records of a group of Myotis velifer emerging from a cave on the Bamberger Ranch Preserve near Johnson City, Texas, focusing on their sensorimotor behavior with respect to environmental features. In this paper, we continue to analyze the same data set by considering the interactions between pairs of bats with the aim of establishing a more unified view of bat navigation behavior.

Based on the species involved and the nature of the flight, paired-animal flight interactions have been mainly studied in the context of two situations: chasing and following. Chasing refers to the case in which a predator tries to catch a prey. Mizutani et al. (2003) and Ghose et al. (2006) show that bats and dragonflies use a motion camouflage flight strategy, which minimizes motion parallax cues that the prey can extract from its optical flow. Following is less aggressive than chasing and is generally conspecific. Chiu et al. (2010) shows that a follower bat displays such a behavior to conceal itself from the leader bat in order to increase its prey-capture performance. A classical pursuit strategy, in which the follower points its velocity vector towards the leader, is preferred in following.

Fig. 1. Flight path statistics for 39 M. velifer are depicted. The red curve is the mean trajectory, and the blue ellipses (centered on the mean trajectory) represent a dispersion of one standard deviation. Two obstacles, a vine and a pole, are denoted as circles. The triangles are visual features in a wooded area (mostly tree branches) and the dotted lines define the edges of the wooded area.

In Sebesta and Baillieul (2012) and Kong et al. (2013), we discussed the concept of time-to-transit and used it as the basis for a collection of vision-based steering
control laws. It was argued that time-to-transit was a biologically meaningful parameter that could probably be calculated in an animal’s visual cortex, and steering control laws based on time-to-transit relative to single pairs of environmental features were proposed. Our research assumed that the bats navigated through the flight corridor depicted in Fig. 1 by stitching together sequences of motion primitives in each of which visual feedback focused on either one or two environmental features. It was shown that even a very small set of such motion primitives was expressive enough to allow a simulated air vehicle to fly a bat-like trajectory. The keys to generating animal-like trajectories for a simulated flight vehicle were:

- designing a set of vision-based motion primitives that produce motion segments based on the geometry and movement of image points on the focal plane (retina) of the image sensor;
- sequentially updating a set of key feature points and selecting the appropriate motion primitives to guide the vehicle along each path segment;
- a protocol for switching between the key features of one segment and the next.

Comparing the simulated flight paths with the paths reconstructed from animal field data, we developed the hypothesis that the animal movements were guided by both direct reaction to environmental features and some form of cognitive processing that could involve spatial memory and path choices to minimize energy expenditures. Using our control primitives, we were able to develop a motion strategy that would closely approximate the mean flight path of the bats (the red curve in Fig. 1). The question remained as to why many animals deviated significantly from this mean path. In the present paper, we propose that large excursions toward the boundary of the woods could be the result of a trailing bat following a leader according to a certain leader-follower protocol. Using the concept of virtual loom, we formulate a new steering law that produces simulated flight paths consistent with those of pairs of bats observed in the field.

The paper is organized as follows. Section 2 introduces the concept of virtual loom. Section 3 presents our analysis of M. velifer’s apparent leader-follower behavior and tests the data against existing pursuit laws. In Section 4, we first propose a virtual loom based steering law that produces the kinds of leader-follower behaviors that have been observed in bat pairs in the field. We then describe motions of simulated vehicles that use synthetic images of both stationary features and moving objects (a leader bat or another vehicle) to guide motion through the computer reconstructed flight corridor. A number of vehicle simulations were carried out with vehicles entering the flight corridor at random (Poisson) times and random (Gaussian) locations across the left hand boundary of the flight corridor. Comparisons with our bat flight data are made and show that the simulations have significant similarities.

2. VIRTUAL LOOM

We model flight kinematics following the model of Justh and Krishnaprasad (2006). The dynamics of the leader are given as:

\[
\begin{align*}
\dot{r}_l &= v_l x_l \\
\dot{x}_l &= v_l y_l w_l \\
y_l &= -v_l x_l w_l,
\end{align*}
\]

where \(v_l\) is the speed of the leader, \(r_l\) is the position of the leader, \(x_l\) is the unit tangent vector to the trajectory of the leader, \(y_l\) is the corresponding unit normal vector, and the plane curvature \(w_l\) is the steering control for the leader. Similarly, the dynamics of the follower are given as:

\[
\begin{align*}
\dot{r}_f &= v_f x_f \\
\dot{x}_f &= v_f y_f w_f \\
y_f &= -v_f x_f w_f.
\end{align*}
\]

In this paper, we assume that the leader and the follower have the same speed. This assumption is consistent with field data.

![Fig. 2.](image-url) Fig. 2. Frenet frame representations of the leader and the follower together with the follower’s side-looking eye. L and F are the center axis points of the eyes of the leader and the follower, respectively. \(|f|\) is the focal length distance from the lens to the focal plane (retina). \(L’\) is the image point corresponding to \(L\). \(\alpha\) is the angle between \(x_l\) and \(x_f\).

In terms of these kinematic models and the follower’s imaging system model that is depicted in Fig. 2, we recall the definitions of optical flow parameters from Sebesta and Baillien (2012) and Kong et al. (2013). Suppose the follower’s initial position is \(r_f(0) = (r_1(0), r_2(0))\) at time \(t = 0\) and it is flying in \(x_f\) direction with a constant speed \(v_f\). In such a case, if the leader is stationary, the follower will cross the line of transit at time \(\tau = r_x/v_f\). Here line of transit is the line that is perpendicular to the line of flight and passes through the origin of the leader frame, and \(r_x\)

\[1\text{As noted in Kong et al. (2013), the bat motions in our data set are approximately planar.}
is the distance between \( r_f(0) \) and this same line of transit. This quantity \( \tau \) is called the \textit{time-to-transit}. It has been widely studied in literature dealing with motion perception (see e.g. references in Sebesta and Baillieul (2012)), and it has been shown to be easily computed in an animal’s visual cortex. Indeed, if, at the initial time \( t = 0 \), \( d \) is the distance in the follower’s image plane (bat retina) between the leader’s image \( (L’ \) in Fig. 2) and the principal camera axis point \( F \) (Fig. 2), then \( \tau = d/d \cdot \). If the leader is not stationary, the definition still makes sense and is related to the relative velocities of the leader-follower pair. Of course if the leader and the follower are traveling in the same direction at the same speed, the image distance \( d \) does not change over time \( \dot{d} = 0 \), which reflects the fact that \( \tau \) must be infinite. Since we shall be interested largely in the case where the leader and the follower fly at essentially identical speeds, we find it more convenient to work with the reciprocal of \( \tau \), which is called the \textit{loom}. Since we shall be dealing in particular with situations in which the follower never reaches the point of transit, we define the \textit{virtual loom} as follows:

\textit{Definition 1.} For a leader-follower pair (Eqs. (1) and (2)), the \textit{virtual loom} \( \lambda(t) \) at time \( t \) is

\[
\lambda(t) = \frac{1 - x_f(t) \cdot x_f(t)t}{r(t) \cdot x_f(t)}. \tag{4}
\]

Notice that \( \lambda(t) \) has a unit that is inverse of time. For brevity, we use \( \lambda \) to represent \( \lambda(t) \).

From Fig. 2, we have the following relationship:

\[
d = \frac{f}{r_y - f} r_x, \tag{5}
\]

so the follower bat can estimate \( r_x \) by sensing \( d \).

In addition, we define an equilibrium state for a pair as follows.

\textit{Definition 2.} A leader-follower pair (Eqs. (1) and (2)) is said to be in a state of \textit{equilibrium} if \( \lambda \) is zero.

\textit{Remark 1.} If, as shown in Fig. 2, \( \alpha \) is the angle between the headings of the two bats, then \( \cos \alpha = x_f \cdot x_f \). Further, define \textit{transiting} as the instant when the image of the leader on the follower’s retina \( L’ \) coincides with \( F \), the focal point of the follower’s retina, which corresponds to \( r_x = r \cdot x_f = 0 \). For two bats flying with the same constant speed \( v_f = v_l = v \), a state of \( \lambda \) equilibrium means that the relative velocity of the two bats is zero and \( L’ \) stays at the same position on the follower’s retina. In this case, the follower bat can estimate \( \alpha \) by sensing \( d \), the optical flow. A zero \( d \) corresponds to a zero \( \alpha \). On the other hand, a non-zero \( d \) implies that \( \alpha \) is not zero and a transiting is going to happen if no adjustment is made by the follower. Finally, it is worth pointing out that, although in this paper we focus on vision-based control, bats can also use other sensory modalities, such as echolocation (Shaw et al. (1991)), to estimate time-to-transit \( \tau \) or virtual loom \( \lambda \).

\textit{Remark 2.} Parallel (or near parallel) flight alignment (with \( \alpha \approx 0 \)) has been observed in the mating activity of dragonflies (Wagner (1986)), competitive prey capturing in bats (Chiu et al. (2010)) and tandem flight of swallows (unpublished results from the Hedrick Lab at UNC Chapel Hill). Benefits of such a flight pattern include aerodynamic efficiency (the follower can utilize the vortex of the leader’s wingtip to save energy, known as ‘vortex surfing’), stealth (the follower can conceal itself from the leader to increase its prey capturing probability) and echolocation efficiency (the follower bat can turn off its sonar or adopt a low duty cycle).

3. FLIGHT BEHAVIOR OF MYOTIS VELIFER: DATA ANALYSIS

Data collection and analysis are described as follows.

3.1 Experiment Procedure

Raw flight data on \( M. \) velifer were collected shortly after sunset on 30 May, 2011. The bat colony resides in an artificial cave located approximately 50 meters from the point of observation. Upon exiting the roost, individuals immediately begin to disperse over the landscape by following the margin of a forest fragment toward an open flight corridor over a paved ranch road. We collected thermal infrared video of bats with three thermal cameras (FLIR ThermoVision SC8000, FLIR Systems, Inc.) placed along the flight corridor. We chose this location because there was an abundance of natural obstacles in the flight corridor and because it was sufficiently far from the roost that the bats presumably had accreted into flight groups but were not sufficiently far from the roost to have split from each other to forage separately. Our camera system operated at 131.5 Hz with 1024×1024 resolution and used 25 mm lenses.

The cameras were placed in a line perpendicular to the flight direction of the bats. Camera viewing angles were selected so as to optimize reconstruction accuracy at points of direct interaction between bats and a natural obstacle (a hanging vine), and to maximize flight track duration. On average, each bat was recorded for approximately 300 frames. This was accomplished by localizing the vine at a central focal point in each of the three camera views. The 3D geometry of the scene was calibrated by waving an object of known dimension through the shared view volume of the three cameras, in this case a 1.56 m PVC “wand”, and direct linear transformation (DLT) coefficients were calculated from pairs of wand points. A technician gathered 2D coordinates of each bat in each of the three views using custom annotation software developed by our research group. Flight trajectories were then reconstructed in 3D as described in Towne et al. (2012). For hand-annotated positions, some human-generated noise was introduced to the flight trajectories. This uncertainty was smoothed as described in Kong et al. (2013).

3.2 Poisson Emergence

Previous studies of bat emergence times have been largely focused on how factors, such as sunset time, weather, and the existence of predators, affect the onset of the emergence and the mean emergence time (Welbergen (2006); Kunz and Anthony (1996)). To our knowledge, there has been no study to model the fine details of emergence rates.

We define the first time a bat appears in the video as its emergence time. By this, we get an ordered time sequence, \( S := \{t_i, i = 1, \ldots, N\} \), where \( t_i \) is the emergence time of
the ith bat and $N = 254$ is the total number of recorded bats. Notice that Fig. 1 only shows a fraction of the trajectories. Please refer to Kong et al. (2013) for details regarding the whole data set. The Kolmogorov-Smirnov test is used to determine whether the sequence (or a subset of it) fits a Poisson model. Fig. 3 shows the sampled rate parameter $\bar{\theta}(t)$ of the subset $\{t_i \in [t, t+T]\}$ with $t \in [0, 450]$ and $T = 120$ seconds. The time axis corresponds to the whole duration of the recording period with 0 corresponding to the time the recording started.

3.3 Effects of Leader on Follower

We classify the 254 collected trajectories into six groups based on their positions with respect to the obstacles (the vine and the pole). The 39 trajectories that are shown in Fig. 1 and will be analyzed in this subsection correspond to the group of bats passing the vine from the left and passing the pole from the right. See Kong et al. (2013) for the information regarding the classification and other groups.

For the group of 39 trajectories shown in Fig. 1, we further select data segments of paired bats for analysis based on the following criteria: the paired bats need to be present simultaneously in the video for longer than 20 frames and the spatial separation between the paired bats must be shorter than 10 meters$^3$. We say that the bat emerging earlier is the leader and the one emerging later is the follower. The trajectories of one such pair are shown in Fig. 4.

There is a correlation of $R = 0.8894$ (Pearson correlation coefficient) between the mean $y$ coordinate of bats emerging within a fixed time window and the number of bats in the window. The result is shown in Fig. 5. As shown in Fig. 4, a higher $y$ coordinate implies a smaller distance to the woods. Further, the larger the number of bats emerging within a fixed time window, the shorter the average interval between the successive emergence of two

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$^2$ Another truncated sequence $S_2 := \{t_i \in [300, 450]\}$ was also tested. But it did not pass the test due to the lack of enough data points for statistical significance.

$^3$ A bat can perceive items within 10 meters with a good resolution via its eyes (Wimsatt (1970)). Given that the average speed of the observed bats is 10.17 m/s, this threshold corresponds to approximately one second difference between the two bats’ emergence times.
Fig. 6. Flight path statistics of \( G_1 \) and \( G_2 \) are depicted. The red (green) curve is the mean trajectory of \( G_1 \) (\( G_2 \)). The blue (black) ellipses (centered on the mean trajectory) represent a dispersion of one standard deviation of \( G_1 \) (\( G_2 \)).

Table 1. Number of Bats in Each Class

<table>
<thead>
<tr>
<th>( C_1 )</th>
<th>( C_2 )</th>
<th>( C_3 )</th>
<th>( C_4 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>14</td>
<td>4</td>
<td>14</td>
</tr>
</tbody>
</table>

The correlation means that a bat (a follower) behaves differently if there is another bat (a leader) in front of it. In order to further illustrate the behavior difference, we classify the 39 trajectories shown in Fig. 1 into four classes. They are

- \( C_1 \): the bat is a single bat, which is neither a leader nor a follower;
- \( C_2 \): the bat is a single-role leader bat, which is a leader but not a follower;
- \( C_3 \): the bat is a dual-role bat, which is both a leader and a follower;
- \( C_4 \): the bat is a single-role follower bat, which is follower but not a leader.

The numbers of bats in different classes are shown in Table 3. We then combine the four classes into two groups: the leader group \( G_1 = \{C_1, C_2\} \) and the follower group \( G_2 = \{C_3, C_4\} \). The statistics of the two groups are shown in Fig. 6. It is quite obvious that the follower group curves more toward the wooded area than the leader group.

To conclude, as the number of bats emerging within an interval becomes larger or equivalently the initial distance (the emergence interval) between the leader-follower pair becomes smaller, the follower bat tends to stay closer to the wooded area and take a longer route than the leader bat. One possible interpretation of the observed effects is that the trailing bat is trying to align itself with the leader while staying a safe distance away from the obstacles, e.g. the pole. For the specific environment as shown in Fig. 6, a side effect of such a behavior is a larger excursion towards the woods for the follower bat.

Remark 3. The analysis in this subsection is based on 39 bat trajectories, which were collected in a single day during an 8 minute time interval. Recently we have collected a much larger data set of the same species at the same location. The recording was 45 minutes long for each day and lasted 8 days. We plan to perform the same analysis on the new data set to test and validate these observations.

3.4 Are Bats Pursuing One Another?

Fig. 7. Analysis results for the pair shown in Fig. 4: the baseline direction \( r/|r| \) (blue) and the angle between the baseline direction \( r/|r| \) and the follower’s heading \( x_f \) (black). Both are represented as angles. For instance, the blue curve is computed by \( \tan^{-1}(p_2/p_1) \) with \( p_1 \) and \( p_2 \) being the first and second component of \( r/|r| \).

In this subsection, we analyze paired bats’ behavior by checking the data against existing pursuit laws: classical pursuit, constant bearing, and motion camouflage (Wei et al. (2009)). In classical pursuit, the follower aligns its direction of motion \( x_f \) with the baseline direction \( r/|r| \), where the baseline \( r \) is defined as \( r_l - r_f \) in Section 2; in constant bearing, the follower keeps the angle between its heading \( x_f \) and the baseline direction \( r/|r| \) constant; in motion camouflage, the follower keeps the baseline direction \( r/|r| \) constant.

Fig. 7 illustrates that none of these pursuit laws explains the behavior observed in Fig. 4. The baseline direction \( r/|r| \) (blue curve) does not stay constant, which violates motion camouflage pursuit; the angle between the baseline direction \( r/|r| \) and the follower’s heading \( x_f \) (black curve) is neither zero nor constant, which violates classical and constant bearing pursuits. The result implies that the follower bats are not pursuing the leader bats (by pursuing we mean that there is a moment when the follower intercepts the leader). The reasons may be as stated in Remark 2. Nevertheless an alternative interpretation is needed to explain the observed behavior. In the next section, we will propose a steering law and a navigation strategy the follower bat might use.

4. INTEGRATED NAVIGATION STRATEGY

In Kong et al. (2013), we proposed an integrated strategy to explain the navigation behavior of \( M. velifer \) in a data set of 254 individuals (the same data set from which we are selecting the bat pairs studied here). We hypothesized that these bats used landmarks recalled from their spatial memory to select features from the
environment and then generated control strategies based on these remembered features. Synthesized trajectories generated by using sequences of feature-based control primitives approximately fit the mean behavior of the bats. However, as noted in Section 3, bats following leaders behave differently from those that do not. The interaction between the bats is a factor that the previous work of Kong et al. (2013) did not consider. In this section, we first propose a steering law that a follower bat may use to follow a leader. We then discuss a strategy that takes the leader-follower behavior into consideration and show that now the statistics, both the mean and the variance, of the synthesized trajectories fit with those of the data on bat pairs.

4.1 λ-Based Steering Law

The planar steering law we study next is based on minimizing the virtual loom in a follower’s perception of the leader’s motion.

**Theorem 1.** Consider leader-follower pair (Eqs. (1) and (2)) with the following assumptions:

1. the control of the leader $u_l$ is zero (the leader flies in a straight line);
2. $r_x$ is positive (the leader is in front of the follower).

Then for $k > 0$, the follower with control

$$u_f = k x_l \cdot y_f = -k \sin \alpha$$

will asymptotically align itself with the leader, i.e., $\alpha \to 0$ (and $\lambda \to 0$).

**Proof.** We take the unnormalized virtual loom as a Lyapunov function $V := 1 - x_l \cdot x_f$. This is 0 if $x_l \cdot x_f = 1$ ($\alpha = 0$) and positive otherwise. Its derivative along trajectories is

$$\dot{V} = -\dot{x}_l \cdot x_f - x_l \cdot \dot{x}_f = -u_f(x_l \cdot y_f) = -k(x_l \cdot y_f)^2$$

which is zero when $x_l \cdot y_f = 0$ or equivalently $x_l \cdot x_f = 1$ ($\alpha = 0$).

Theorem 1 implies that if the leader is flying in a straight line, then the follower can utilize the virtual loom to achieve parallel flight with the leader. See Remark 1 for the explanation of how bats might estimate the virtual loom.

4.2 Is Pure Following Strategy Sufficient?

Fig. 8 shows the actual trajectories of a leader-follower pair and a synthesized follower trajectory (purple) by using control law (6) with the assumption that the follower only reacts to the leader without utilizing either its spatial memory or cues from the environment. The purple synthesized trajectory fits with the actual follower bat’s trajectory (green) well for the segment that has $x$ coordinates smaller than 9 meters. This implies that the follower bat synchronizes its motion with the leader inside the open space between the pole and the wooded area. However, after passing 9 meters, the discrepancy between the synthesized and actual trajectories becomes larger. The synthesized trajectory has the danger of colliding with the obstacles or losing track of the leader due to occlusion. Here, we need to consider a navigation strategy that integrates a rapid refocus of attention on the looming tree obstacles.

4.3 Integrated Strategy: Spatial Memory Fused with Reactions to Environment and Other Bats

The integrated strategy proposed in Kong et al. (2013) is now extended so as to incorporate the leader-follower behavior. The navigation strategy is synthesized from three vision-based control primitives: a distance maintenance law $u_d[O_1, O_2]$, a circling control law $u_c[O_1]$ and a leader-follower control law $u_f[O_1]$, where $O_1$ and $O_2$ are visually perceived features used in a particular control law and can be either static (for $u_d$ and $u_c$) or moving (for $u_f$). The primitives $u_d$ and $u_c$ can be found in Kong et al. (2013), while the primitive $u_f$ is Eq. (6).

Fig. 9 shows the statistics of 100 synthesized trajectories. The red curve is the mean trajectory, and the blue ellipses (centered on the mean trajectory) represent a dispersion of one standard deviation. Labeled features are the ones that are assumed being memorized by the bats.

![Fig. 8. Actual bat trajectories (red: leader bat, green: follower bat) and synthesized follower trajectories (purple: based on control law (6), blue: based on the integrated strategy).](image)

![Fig. 9. Flight path statistics of 100 synthesized trajectories. The red curve is the mean trajectory, and the blue ellipses (centered on the mean trajectory) represent a dispersion of one standard deviation. Labeled features are the ones that are assumed being memorized by the bats.](image)
feature ‘a’ as shown in Fig. 9.) The intersubjective distance between a pair of vehicles determines whether there exists a leader for the trailing vehicle to follow. If there exists a leader, the follower vehicle relies on the leader and the control $u_f$ for navigation. It switches to environment-cue-directed control $u_d$ or $u_c$ when it is on a collision course. On the other hand, if there does not exist a leader, the follower vehicle relies on its spatial memory and cues from the environment for navigation and the controls they can use are $u_d$ and $u_c$. For Fig. 9, each trajectory is generated by a sequence of controlled motion segments as follows:

- If there does not exist a leader, the trajectory is generated by $u_c[\text{pole}] \rightarrow u_d[b,c] \rightarrow u_d[c,d] \rightarrow u_d[\ldots]$ for the reaming features;
- If there exits a leader, the trajectory is generated by $u_f[\text{leader}] \rightarrow u_d[b,c] \rightarrow u_d[c,d] \rightarrow u_d[\ldots]$ for the reaming features.

For Fig. 8, the follower trajectory (blue) is generated by the second strategy since it has a leader (red). We prescribe the switching between the primitives based on the nearest feature(s) in the follower’s body $x_f$ direction. For instance, the switching from $u_f[\text{leader}]$ to $u_d[b,c]$ is triggered if feature $b$ is closer to the follower than the leader in the $x_f$ direction. Similarly, the switching from $u_d[b,c]$ to $u_d[c,d]$ is triggered if feature $d$ is closer to the follower than feature $b$ in the $x_f$ direction.

A comparison between Fig. 9 and Fig. 1 shows that the synthesized trajectories accurately capture both the mean and the variance of the actual bat trajectories with the only difference being that the ellipses in Fig. 1 are slightly fatter. One possible explanation of the difference is that the sensors are assumed to be noiseless for the synthesized trajectories while this is not the case for actual bats. Similarity can also be observed between the actual follower’s trajectory (green) and the synthesized trajectory based on the integrated strategy (blue) in Fig. 8. Such resemblances support our integrated strategy hypothesis.

By following another bat, in the context of navigation, a follower bat can save energy by adopting a low duty cycle echolocation or even turning off its sonar completely (Chiu et al. (2010)). It can also be used by an inexperienced individual to follow an experienced one. In such a case, the leader (e.g. a female bat) is more familiar with the environment than the follower (e.g. a juvenile).

5. CONCLUSION

In this paper, we analyze a set of $M. v. elifer$ trajectories collected from field observation and show that, for pairs of bats, the flight behavior of the follower is significantly affected by that of the leader. This can not be explained by existing pursuit control laws. We propose a concept called virtual loom $\lambda$ and show that this is useful in characterizing the geometrical configuration of a bat pair. We then introduce a steering law based on $\lambda$ and show that synthesized trajectories generated by following an integrated strategy that combines spatial memory, environment-cue-based control and leader-follower-cue-based control and stitches together a sequence of vision-based motion primitives, exhibit behaviors that are similar to the observed bat behavior.

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