A Fast Community Based Algorithm for Generating Web Crawler Seeds Set

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Abstract: In this paper, we present a new and fast algorithm for generating the seeds set for web crawlers. A typical crawler normally starts from a fixed set like DMOZ links, and then continues crawling from URLs that are found in these web pages. Crawlers are supposed to download more good pages in less iteration. Crawled pages are good if they have high PageRanks and from different communities. In this paper, we present a new algorithm with running time $O(n)$ for generating crawler's seeds set based on HITS algorithm. A crawler can download qualified web pages, from different communities, starting from seeds set generated using our algorithm in less iteration.

1. Introduction

Nowadays web has an imperative impact on our daily life providing required information. Based on [1], the size of web was estimated 11.5 billion pages at 2005. This size is now even larger and become larger as the time elapse. Web search engines like Google, Yahoo, MSN,… have important roles for facilitating information access. A web search engine consists of three main parts: A crawler that retrieves web pages, an indexer that builds indexes, and a searcher. A major question a crawler has to face is that which pages it has to retrieve so as to have the "most suitable" pages in the collection [3]. Crawlers normally retrieve a limited number of pages. In this regard, the question is how fast a crawler collects the "most suitable" pages. A unique solution to this question is not likely to exist. In what follows, we try to answer this question.

Different algorithms with different metrics have been suggested to lead a crawl towards high quality pages [4,5]. In [4] Cho, Garcia-Molina, and Page suggested using connectivity-based metrics to do so. To direct a crawl, they have used different ordering metrics: breadth-first, backlink count, PageRank, and random. They have revealed that performing a crawl in breadth-first order works nearly well if "most suitable" pages are defined to be pages with high PageRanks.

Najork and Wiener extend the result of Cho et al. They examined the average page quality over the time of pages downloaded during a web crawl of 328 million unique pages. They have showed that traversing the web graph in breadth-first search order is a good crawling strategy.

Based on Henzinger's work [3] better understanding of graph structure might lead to a more efficient way to crawl the web. We use this idea in this paper to develop our algorithm. First, we define the "most suitable" pages and then we show how a crawler can retrieve most suitable pages. We use three metrics to measure the quality of a page. The first metric is the community of a page. A collection of good crawls should contain pages from different communities. The second metric is its PageRank [2]. Pages with high PageRanks are the most important pages in web. The third metric is number of visited pages at iterations. A good crawler will visit more pages in less iteration.
In this paper, we present a new fast algorithm for extracting seeds set from a previously crawled pages. Using offered metrics, we show that by starting from extracted seeds suggested by our algorithm, a crawler will quickly collect most suitable pages from different communities.

We have studied different community extraction algorithms: PageRank, Trawling, HITS, and Network flow base community discovery. From our analysis, we decided to use HITS ranking without keyword search in our algorithm for community discovery and collecting seeds set. We have found that bipartite cores are useful for selecting seeds set. Bipartite cores contain Hub and Authority pages. Since we are interested in having Authority pages in our crawl, we would need to start crawling from Hub pages. Hubs are durable pages, so we can count on them for crawling.

The main idea in our method is to use HITS_Ranking on the whole graph for extracting the most important bipartite cores. We offer two bipartite core extraction algorithms. Using these algorithms, we extract bipartite cores and select some seeds from the hubs in the extracted cores. Finally, we remove the extracted bipartite core from the graph and repeat these steps till having desired number of seeds.

We have compared the results of the crawls starting from extracted seeds set produced by our algorithm, with crawls starting random nodes. Our experiments show that the crawl staring from seeds set identified by our algorithm finds the most suitable pages of web very faster than a random crawler did.

According to our knowledge, this is the first seeds extraction algorithm that is able to identify and extract seeds from different web communities. Low running time is crucial in working with large size web data. The running time of proposed algorithm is $O(n)$. Low running time with community base properties make this algorithm unique in comparison with previous algorithms.

The remainder of this paper proceeds as follows. In Section 2, we present our algorithm for discovering seed sets in a large web graph and compute the complexity of proposed algorithm. In section 3, we discuss the results of running and evaluating this algorithm on 18M and 39M node graphs. Section 4 contains conclusion and future works.

2. ALGORITHM for DISCOVERING SEED SETS in LARGE WEB GRAPH

In this section, we present our algorithm for discovering seeds sets from web graph. Firstly, we start with a discussion about the web structure. This will give some intuition about our algorithm to the reader. The connected web's macroscopic structure breaks into four pieces [6]: SCC, IN, OUT, TENDRILS. SCC consist all of whose pages can reach one another along directed link. IN consists of pages that can reach the SCC, but cannot be reached from it. OUT consists of pages that are accessible from SCC, but do not link back to it. Finally, the TENDRILS contain pages that cannot reach the SCC and cannot be reached from SCC.

From the structure and analysis presented in [6], the most important web pages are expected to be in SCC+OUT. From [2] we know that web pages with high PageRanks are the most valuable pages in the web. In addition, from [3, 7, 8] we understand that bipartite cores are one of the most valuable sources in the web usually called hubs and authorities. Beside, we know that the web contains thousands of different communities. In [7] Kleinberg used keywords and a ranking method for finding hubs and authorities pages which result contains pages in one or more communities. In [9] Flake et al suggested a method based on network flow algorithm for finding web communities. The relation between communities extracted from their algorithm and Kleinberg's community is that the result of the former is expected to be a subset of Flake et al algorithm [10]. See Figure 1 for a sample relationship between results of these two algorithms.

A crawler normally do not crawl the entire web. Instead, it continues to retrieve a limited number of pages. Crawlers are expected to collect "most suitable" pages of web rapidly. We defined "most suitable" pages of web as those pages with high PageRank. These pages are pages that HITS algorithm calls them Authority pages. The difference is that HITS algorithm finds the authorities pages relating to keywords but PageRank shows the importance of a page in the whole web. As well, we know that good hubs link to good authorities. If we are able to extract good hubs from a web graph and different communities, we will be able to download good authorities that have high PageRank of different communities.

We use HITS ranking without keywords search on previously crawled web pages and then prune the resulting sub graph. The procedure of using HITS ranking and the elimination will be repeated until enough seed points are reached. We show that selected hub nodes from the resulted sub graph of iterations can solve the crawl problem mentioned in this paper.
The results of a crawl lead to the most suitable pages. The seeds from these results are used to seed our algorithm, why would the other question that may arise is that if a crawler starts from these communities. Thus, a crawler will be able to download pages from different communities starting from these seeds. We have experimented our algorithm using web graph of UK 2002 containing 18M nodes and 298M edges, and UK 2005 containing 39M nodes and 936M edges [6, 7]. Our experiments prove that extracted bipartite cores have a reasonable distance from each other.

The other question that may arise is that if a crawler starts from seeds resulted from our algorithm, why would the results of crawl lead to the most suitable pages. The

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### Figure 2. HITS Ranking Algorithm

#### 2.1. Iterative HITS Ranking & Pruning

We assume that we have a web graph of crawled web pages. The goal is to extract seeds set from this graph so that a crawler can collect the most important pages of the web in less iteration. To do this we run HITS ranking algorithm on this graph. This is the second step of HITS algorithm. In the first step, it searches the keywords in an index-based search engine. For our purpose, we ignore this step and only run the ranking step on the whole graph. In this way, bipartite cores with high Hub and Authority rank will become visible in the graph. Then we select the most highly ranked bipartite core using two algorithms we suggest, namely: extracting seeds with fixed size, and extracting seeds with fixed density. Then, we remove this sub-graph from the graph, repeat ranking, seed extraction, and sub-graph removal steps up to a point that we have enough seeds set.

A question that may arise is that when repeating these steps, why we need to run HITS ranking again. Isn't one time ranking enough for whole steps? The answer is that, removing bipartite core in each step modifies the web graph structure we are working on. In fact, re-ranking changes the hub and authority ranks of bipartite cores. Removing high ranked bipartite core and re-ranking web graph drive appeared bipartite cores to be from different communities. Thus, a crawler will be able to download pages from different communities starting from these seeds.

We have experimented our algorithm using web graph of UK 2002 containing 18M nodes and 298M edges, and UK 2005 containing 39M nodes and 936M edges [6, 7]. Our experiments prove that extracted bipartite cores have a reasonable distance from each other.

### Figure 3. Extracting Bipartite Cores with Fixed Size

The answer is that, in iterations of algorithm, we select and extract high ranked bipartite cores from the web graph. Extracted bipartite cores have high hub or authority ranks. It is expected that pages with high hub rank link to pages with high PageRank. Our experiments prove the correctness of this hypothesis.

#### 2.2. HITS Ranking

Ranking is the second step of HITS algorithm [7]. In our algorithm, the HITS-Ranking procedure is given a directed graph $G$ as an input and HITSIterationCount. The procedure defines two $h$ and $a$ vectors for Hub and Authority rank of nodes. Their initial value is set to $I$. Then algorithm updates $h$ and $a$ vectors of all nodes in the input graph. Afterwards, the updated vectors are normalized to $I$. The Algorithm repeats vector updates and normalization steps until it reaches the required number of iterations. Two vectors $h$ and $a$ are returned as the results of HITS-Ranking procedure. Figure 2 shows HITS-Ranking algorithm.

#### 2.3. Extracting Seeds with Fixed Size

The Extract-Bipartite-Cores-with-Fixed-Size procedure, as its name indicates, extracts one bipartite sub-graph with highest hub and authority ranks with predetermined size given as an input. The Algorithm is given a directed graph $G$, BipartiteCoreSize, NewMemberCount and $h$, and $a$ vectors. BipartiteCoreSize specifies the desired size of bipartite core we like to be extracted. NewMemberCount indicates that in each iteration of the algorithm how many hub or authority nodes should be added to the hub or authority sets. $h$ and $a$ vectors are hub and authority ranks of nodes in the input graph $G$.

In the initial steps, the Algorithm sets HubSet to empty and adds the node with highest authority rank to AuthoritySet. While sum of AuthoritySet size and HubSet size is less than BipartiteCoreSize it continues to find

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<table>
<thead>
<tr>
<th>Procedure</th>
<th>HITS-Ranking</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input:</strong> graph: $G=(V,E)$, integer:HITSIterationCount</td>
<td></td>
</tr>
<tr>
<td>1)</td>
<td>For all $v$ in $V$ do</td>
</tr>
<tr>
<td>2)</td>
<td>Set $a(v) = 1$;</td>
</tr>
<tr>
<td>3)</td>
<td>Set $h(v) = 1$;</td>
</tr>
<tr>
<td>4)</td>
<td>End For</td>
</tr>
<tr>
<td>5)</td>
<td>For $i=1$ to HITSIterationCount do</td>
</tr>
<tr>
<td>6)</td>
<td>For all $v$ in $V$ do</td>
</tr>
<tr>
<td>7)</td>
<td>$a(v) = \sum_{(w,v)\in E} h(w)$;</td>
</tr>
<tr>
<td>8)</td>
<td>End For</td>
</tr>
<tr>
<td>9)</td>
<td>For all $v$ in $V$ do</td>
</tr>
<tr>
<td>10)</td>
<td>$h(v) = \sum_{(v,w)\in E} a(w)$;</td>
</tr>
<tr>
<td>11)</td>
<td>End For</td>
</tr>
<tr>
<td>12)</td>
<td>Normalize $h$ vector to 1;</td>
</tr>
<tr>
<td>13)</td>
<td>Normalize $a$ vector to 1;</td>
</tr>
<tr>
<td>14)</td>
<td>End For</td>
</tr>
<tr>
<td>output: $h, a$</td>
<td></td>
</tr>
<tr>
<td>End Procedure</td>
<td></td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Procedure</th>
<th>Extract-Bipartite-Cores-with-Fixed-Size</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input:</strong> graph: $G=(V,E)$, integer: BipartiteCoreSize, NewMemberCount;</td>
<td></td>
</tr>
<tr>
<td>vector: $h, a$;</td>
<td></td>
</tr>
<tr>
<td>1)</td>
<td>HubSet = $\emptyset$;</td>
</tr>
<tr>
<td>2)</td>
<td>AuthoritySet= Add $v$ with highest $a(v)$ to AuthoritySet;</td>
</tr>
<tr>
<td>3)</td>
<td>While $</td>
</tr>
<tr>
<td>4)</td>
<td>AuthoritySet= AuthoritySet $\cup$ (Find Top NewMemberCount $h(v)$ where $v,w\in E$ and $w$ in AuthoritySet and $v$ not in HubSet);</td>
</tr>
<tr>
<td>5)</td>
<td>HubSet = HubSet $\cup$ (Find Top NewMemberCount $a(v)$ where $v,w\in E$ and $v$ in AuthoritySet and $w$ not in HubSet);</td>
</tr>
<tr>
<td>6)</td>
<td>End While</td>
</tr>
<tr>
<td>output: HubSet, AuthoritySet</td>
<td></td>
</tr>
<tr>
<td>End Procedure</td>
<td></td>
</tr>
</tbody>
</table>
new hubs and authorities regarding the NewMemberCount and adds them to the related set. We use this procedure when we like to extract bipartite sub-graph with fixed size. Figure 3 shows the steps of Extract-Bipartite-Cores-with-Fixed-Size procedure. In Figure 4 we show the steps of bipartite sub-graph creation with NewMemberCount equal to 1. An interesting result we have found in our experiments is that at very first steps, all the hubs have links to all authorities. This leaded us to suggest an extraction algorithm with density factor that is described in the following subsection.

2.4. Extracting Seeds with Fixed Cover Density

The Extract-Bipartite-Cores-with-Fixed-CoverDensity procedure, as its name indicates, extracts one bipartite sub-graph with highest hub and authority ranks in a way that the sub-graph has the desired cover-density function. A directed graph $G$, CoverDensity, and $h$ and $a$ vectors are given to the algorithm.

We define Cover-Density as follows:

$$100 \times \frac{|E(HubSet, AuthoritySet)|}{|HubSet||AuthoritySet|} \quad (1)$$

This measure shows how many nodes in the authority set are covered by nodes in hub set. If the bipartite sub-graph is a complete bipartite sub-graph, this measure will be equal to 100. Therefore, if we intend to extract complete bipartite sub-graph we set CoverDensity to 100. $h$ and $a$ vectors are hub and authority ranks of nodes in the input graph $G$.

In initial steps, the Algorithm sets HubSet to empty set and adds the node with highest authority rank to AuthoritySet. In addition, it sets CoverDensityCur to 100.

While CoverDensityCur is bigger than or equal to input CoverDensity, procedure continues to find new hubs and authorities. This algorithm adds only one new node to the sets at each iteration of the algorithm. Remember that in Extract-Bipartite-Cores-with-Fixed-Size we could adjust the count of new members. Here, we do not have such a variable. This is because of the fact that we like to have a precise cover density here. In other words, if we increase the number of new nodes to more than 1, this might cause the reduction of the accuracy of desired cover density.

We use this procedure when we like to extract bipartite sub-graph with desired density between hubs and authorities. Figure 5 shows the details of the Extract-Bipartite-Cores-with-Fixed-CoverDensity procedure.

2.5. Putting It All Together

Up to now, we have presented algorithms for HITS-Ranking and bipartite core extraction based on hub and authority ranks. Our goal is to extract a set of desired number of seeds to crawl and download pages from different web communities with high PageRank in less iteration. We use the proposed algorithms to achieve this goal. We assume that we have a web graph of crawled web pages. Then we run HITS-Ranking algorithm on the whole graph and use one of the bipartite core extraction algorithms we have presented. Then we select arbitrarily one of the nodes in the extracted hub set and add it to our seeds set. Finally, we remove the extracted core from the input graph and repeat these steps until we find ideal number of seeds.

We can use one of these two bipartite-core extraction algorithms that we have proposed: Extract-Bipartite-Cores-with-Fixed-Size, Extract-Bipartite-Cores-with-Fixed-CoverDensity. If we wish bipartite cores to have a fixed size we use the first algorithm and if we are looking for bipartite cores having desired cover density, then we use the second algorithm. For example, if we like bipartite cores to be complete we must use the first algorithm. We have experimented both of these algorithms. As we cannot guess suitable size of a web community, we use the second method. The second method can calculate density of links between hubs and authorities. If we have a complete bipartite core then we are sure that the all the authority pages are from the same community. By decreasing the Cover-Density measure, we decrease the degree of relationship between authority pages. Because the second method is more reliable than the first one, in this paper we only present experimental results achieved from using Extract-Bipartite-Cores-with-
The AuthoritySet is output: 

```
End Procedure
```

```

3) CoverDensityCur = 100;
```

```
5) AuthoritySet = AuthoritySet ∪ (Find Top NewMemberCount h(v) where v,w ∈ E and w in AuthoritySet and v not in HubSet);
```

```
6) HubSet = HubSet ∪ (Find Top NewMemberCount a(v) where v,w ∈ E and v in AuthoritySet and w not in HubSet);
```

```
7) CoverDensityCur = 100 * |E(HubSet, AuthoritySet)| / |HubSet ∪ AuthoritySet|;
```

```
8) End While
```

```
output: HubSet, AuthoritySet
```

Figure 5. Extracting Bipartite Cores with Fixed Density

Fixed-CoverDensity. Figure 6 shows the seed extraction algorithm we have used in our experiments in this paper.

The Extract-Seed algorithm receives a directed graph G and SeedCount as input. At the initial step, the algorithm sets SeedSet to empty. While the size of SeedSet is less than SeedCount, the algorithm keeps running. In the first line of while section, algorithm calls HITS-Ranking procedure with G as the input graph and 60 as HITSIterationCount. Kleinberg’s work shows that HITSIterationCount equal to 20 is enough for convergence of hub and authority ranks in a small subgraph [7]. We have found experimentally that a number more than 50 is enough for convergence of hub and authority ranks with the dataset we use. HITS-Ranking algorithm returns two vectors, h and a, containing result of hub and authority ranks of all nodes in graph G. In the next line algorithm calls Extracting-Bipartite-Cores-with-Fixed-CoverDensity with G as input graph, 100 as cover density value, and h and a as hub and authority vectors. This function finds complete bipartite cores in the input graph and returns complete bipartite nodes in HubSet and AuthoritySet. In the next line, a node randomly is selected from hub set and it is added to the SeedSet. Now algorithm removes the hub and authority nodes and their edges from the graph G. The removal step helps us to find seeds from different communities.

### 2.6. Complexity of Proposed Seeds Extraction Algorithm

The running time of Seeds-Extraction Algorithm, Figure 6, is $O(n)$, where $n$ is number of nodes in the input graph. The while loop of lines 2-12 is executed at most $|SeedCount|$ times. The work of line 4 is done in $O(n)$. Because, the complexity of HITS-Ranking, Figure 2, is equal to $\Theta(K^2 n L n)$ where $K$ is $|\text{HITSIterationCount}|$, $L$ is the average number of neighborhoods of a node and $n$ is number of nodes in the input graph. This complexity is multiplied by 2 because there are two steps for this kind of computation, one for hub vector and the other for authority vector. In addition, the normalization steps can be done in $\Theta(3n)$. So, the complexity of HITS-Ranking is $O(n)$.

The running time of Extracting-Bipartite-Cores-with-Fixed-CoverDensity in line 4 is $O(n)$. The while loop of lines 4-8, in figure 5, is executed at most $|HubSet + AuthoritySet|$ times which can be viewed as a constant number $k$. Finding and adding a distinct hub node with highest rank to hub set, in line 5, takes $O(k n)$. Finding and adding a distinct authority node with highest rank to authority set, in line 6, takes $O(k n)$. So, the running time of Extracting-Bipartite-Cores-with-Fixed-CoverDensity is at most $O(n)$.

The removal steps of lines 6-11, in figure 6, takes $O(n)$ for removing identified hubs and authorities. Therefore, the total running time of Seed-Extraction Algorithm is $O(|SeedCount| n)$ which is equal to $O(n)$.

### 3. EXPERIMENTAL RESULTS

In this section, we apply our proposed algorithm, to find seeds set from previously crawled pages. Then, we start a crawl using extracted seed on the same graph to evaluate the result. To show that how applying the algorithm on old data can provide good seeds for a new crawl, we start the crawl on a newer graph using seeds set extracted from a previous crawl.

#### 3.1. Data Sets

The laboratory for Web Algorithmics at university of Milan provides different web graph data sets [11]. In our experiments, we have used UK-2002 and UK-2005 web graph data sets provided by this laboratory. These data sets are compressed using WebGraph library. WebGraph is a framework for studying the web graph [12]. It provides simple ways to manage very large graphs, exploiting modern compression techniques. With WebGraph, we can access and analyze a very large web graph on a PC.
Table 1. UK 2002 and 2005 Data Sets information before pruning

<table>
<thead>
<tr>
<th>Data Set</th>
<th>Nodes</th>
<th>Edges</th>
<th>Diameter Estimate</th>
</tr>
</thead>
<tbody>
<tr>
<td>UK-2002</td>
<td>18,520,486</td>
<td>298,113,762</td>
<td>14.9</td>
</tr>
<tr>
<td>UK-2005</td>
<td>39,459,935</td>
<td>936,364,282</td>
<td>15.7</td>
</tr>
</tbody>
</table>

Table 2. UK 2002 and 2005 Data Sets information after pruning

<table>
<thead>
<tr>
<th>Data Set</th>
<th>Nodes</th>
<th>Edges</th>
</tr>
</thead>
<tbody>
<tr>
<td>UK-2002</td>
<td>18,520,486</td>
<td>22,720,534</td>
</tr>
<tr>
<td>UK-2005</td>
<td>39,459,935</td>
<td>183,874,700</td>
</tr>
</tbody>
</table>
3.1.1. UK-2002

This data set has been obtained from a 2002 crawl of the .uk domain performed by UbiCrawler in 2002 [13]. The graph contains 18,520,486 nodes and 298,113,762 links.

3.1.2. UK-2005

This data set has been obtained from a 2005 crawl of the .uk domain performed by UbiCrawler in 2005. The crawl was very shallow, and aimed at gathering a large number of hosts, but a small number of pages from each host. This graph contains 39,459,935 nodes and 936,364,282 links.

3.2. Data Set Characteristics

3.2.1. Degree Distribution

We had investigated the degree distribution of UK-2002 and UK-2005. Figure 7 and 8 show In-degree and Out-degree distribution for UK-2002 in log-log form. Figure 9 and 10 show In-degree and Out-degree distribution for UK-2005 in log-log form. The results show that the In-degree and Out-degree distribution are power laws in these two datasets.

3.2.2. Diameter

Diameter of a web graph is defined as the length of shortest path from \(u\) to \(v\), averaged over all ordered pairs \((u,v)\) [14]. Of course, we omit the infinite distance between pairs that there is not a path between them. This is called average connected distance in [6]. We had estimated this measure on UK-2002 and UK-2005 data sets through experiments. Table 1 shows the estimated diameter of these data sets together with the number of nodes and edges. We use the resulted diameter to evaluate the distances between extracted bipartite cores resulting from our method.

3.3. Date Preparation

3.3.1. Pruning

Most of the links between pages in a site are for navigational purposes. These links may distort the result of presented algorithm. The result of the HITS-Ranking algorithm on this un-pruned graph will result in hub and authority pages to be found in a site. To eliminate this effect we remove all links between pages in the same site. We assume pages with the same host-name are in the same site. Table 2 shows the number of nodes and edges after pruning in the UK data sets.

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3.4. Results of Extracted Seeds using Proposed Algorithm

We run our algorithm for seeds extraction, Extract-Seeds, on UK-2002 and UK-2005. This algorithm, as Figure 6 shows, sets CoverDensity to 100 for seeds extraction. It searches and extracts complete bipartite cores and then, at each step, selects the seeds from hub nodes in the bipartite sub-graph (see figure 4). Figure 11 shows the size of extracted hubs and authorities in different iteration from UK-2002. It is clear that these cores are complete-bipartite. To reduce the impact of outlier hub sizes in the graphical presentation, we have used a log-log diagram. Figure 12 depicts the size of the extracted hubs and authorities in different iterations for UK-2005. Normally the hub sizes are bigger than the authority sizes. We obtained bipartite cores with very large hub size in UK-2002. So, we have limited the number of hubs to 999 in UK-2002 data set.

3.5. Quality Analysis

3.5.1. Metrics for Analysis

We used some different metrics to evaluate the quality of extracted seeds. The first metric is the distance between extracted seeds. As we have mentioned earlier, a crawler tends to extract web pages from different communities. Using HITS-Ranking and Iterative pruning we can conclude that extracted seeds are from different communities. To prove the intuition, we measure the distances between extracted cores. We have defined core-distances as the nearest directed path between one of the nodes from source core to one of the nodes in the destination core.

The second metric, is the PageRank of pages that will be crawled starting from these seeds. Previously, we have defined the most suitable pages in the web to be the pages with high PageRanks. Therefore, if the average PageRank of crawled pages, at each step of crawl, is bigger than a random crawl, especially at the beginning, then we can conclude that a crawl that starts from those seeds identified by our algorithm will result in better pages.

The third metric is the number of crawled pages at each step of crawling. We focus on a crawler whose goal is to download good pages in small iteration. Thus, if the number of crawled pages starting from extracted seeds by our method at each step is bigger than the number of crawled pages starting a random set, then we can conclude that, our method leads a crawl toward visiting more pages in less iteration too.

For the first metric, we measure the distance between the cores. For the other two metrics, we need to crawl the graph starting from seeds extracted with our method and compare it with a crawl staring from randomly selected seeds.

3.5.2. Result of Bipartite Core Distances

We have measured the distance between all bipartite cores that were extracted from UK datasets and they had a reasonable distance in comparison with diameter of the related graph. Figure 13, shows the graphical representation of distances between 54 cores extracted from UK-2002. The number on the top of each node indicates the iteration number in which the core has been extracted. Because the distance graph between nodes may have not a Euclidian representation, distances in this figure is not exactly match with real distances. The other important information is that bipartite cores in close iterations have a distance equal or bigger than average distance. In addition, the cores that are close to each other (there is a short directed path between them) are identified in far iteration. As an example, the core extracted from iteration 32 has a distance one to the core extracted from iteration 47. In the sample, the minimum distance between nodes is 1 and maximum distance is 13. The average distance is 7.15. As the diameter of UK-2002 data set is 14.9, core distances are fine.

3.5.3. Result of Average PageRank and Visit Count

In this section, we evaluate the second and third metrics defined for evaluation. For UK-2002 we have executed the Extract-Seed algorithm with SeedCount=10. Therefore, the algorithm extracts one seed from each core.
in iteration. Then, we have started a crawling on UK-2002 data set implementing BFS strategy and measured the average PageRank of visited pages in each crawl depth, and the number of pages visited in each crawl depth. Then, we have compared the results with results gained from a crawl starting from random seeds for the same graph.

Figure 14 shows the comparison of average PageRank of crawl starting from seeds extracted with our method and a crawl starting from random seeds. Except the first depth (iteration) of crawl, in the other steps, up to step 4, the average PageRank of pages crawled with our method appear to be better. Specially, in the second and third iterations, the difference is superior. In the later iterations average PagRank of visited pages are close.

Figure 15 shows the comparison of log-number of pages visited in each depth of crawl on UK-2002. For better graphical representation, we have computed log-count of visited pages. Apparently, the results of our method is always better than crawl starting random seeds and a crawl with seeds extracted with our method downloads more pages in less iteration. Figure 16 and 17 show the experiments on UK-2005. The same results appear here too.

3.5.4. Good Seeds for a New Crawl

Using proposed algorithm we have discovered seeds from UK 2002 and UK 2005. Then we have evaluated the goodness of these seeds using three evaluation criteria. These evaluations are goods, but a real crawler has not access to seeds of web graph which it is going to crawl. We should show that the result is always good if we start the crawl using seeds extracted from an old crawled graph.

In this section, we show the result of crawling on UK 2005 using seeds extracted by proposed algorithm and we compare it by randomly crawled seeds to simulate the real environment. Before algorithm's execution, we have checked the validity of seeds found from UK-2002 in UK-2005 data set. If a seed does not exist in newer graph, then we remove that seed from our seeds set. Our experiments show that only 11 present of seeds exist in the new data set. In fact, we have extracted 100 seeds from UK 2002 to be sure that we have 11 valid seeds in UK 2005.

Figure 18 shows the comparison of average PageRank of crawl starting from seeds extracted with our method and a crawl starting from random seeds. The result of our method is better until iteration 3. Figure 19, shows the comparison of log-number of pages visited in each depth of the crawl. In this case, the result of our method is better than the random case between 4 and 15 steps. In fact our method download pages with high page rank till iteration 3 and after that it crawls more pages than the random case till iteration 15. After that the result is nearly the same. Therefore, we can conclude that, a crawler can download qualified web pages in less iteration; starting seed sets generated using our algorithm in less iteration.

4. CONCLUSION and FUTURE WORKS

Crawlers like to download more good pages in little iteration. In this paper, we have presented a new fast algorithm with running time $O(n)$ for extracting seeds set from previously crawled web pages. In our experiments we have showed that if a crawler starts crawling from seeds set identified by our method, then it will crawl more pages with higher PageRank in less iteration and from different communities than starting a random seeds set. In addition, we have measured the distance between selected seeds to be sure that our seeds set contains nodes from different communities. According to our knowledge, this is the first seeds extraction algorithm that is able to identify and extracts seeds from different communities.

Our experiments were on graphs containing at most 39M nodes and 183M edges. This method can be experienced on larger graph in order to investigate the quality of result on them too.
Another aspect where improvement may be possible is the implementation of the seeds that are not found in a new crawl. In our experiments, we have simply ignored nodes were present in an older graph but not in the newer graph. This aspect may be possible to be improved by finding similar nodes in the newer graph.

5. REFERENCES

[1] Gulli, A., and Signorini, A. The Indexable Web is More than 11.5 billion pages. WWW (Special interest and tracks and posters), (May. 2003), 902-903.


