POSITION ESTIMATION OF MOBILE ROBOTS CONSIDERING
CHARACTERISTIC TERRAIN PROPERTIES

Michael Brunner, Dirk Schulz
Department of Unmanned Systems, Fraunhofer-Institute FKIE, Wachtberg, Germany
{michael.brunner, dirk.schulz}@fkie.fraunhofer.de

Armin B. Cremers
Department of Computer Science, University of Bonn, Bonn, Germany
abc@cs.uni-bonn.de

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Abstract: Due to the varying terrain conditions in outdoor scenarios the kinematics of mobile robots is much more complex compared to indoor environments. In this paper we present an approach to predict future positions of mobile robots which considers the current terrain. Our approach uses Gaussian process regression (GPR) models to estimate future robot positions. An unscented Kalman filter (UKF) is used to project the uncertainties of the GPR estimates into the position space. The approach utilizes optimized terrain models for estimation. To decide which model to apply, a terrain classification is implemented using Gaussian process classification (GPC) models. The transitions between terrains are modeled by a 2-step Bayesian filter (BF). This allows us to assign different probabilities to distinct terrain sequences, while taking the properties of the classifier into account and coping with false classifications. Experiments showed the approach to produce better estimates than approaches considering only a single terrain model and to be competitive to other dynamic approaches.

1 INTRODUCTION

The kinematics of mobile robots in outdoor scenarios is much more complex than in indoor environments due to the varying terrain conditions. Therefore, truly reliable velocity controls for robots which are able to drive up to 4 m/s or even faster (e.g. Figure 1) are hard to design. The drivability is primarily determined by the terrain conditions. Thus, we developed a machine learning system which predicts the future positions of mobile robots using optimized terrain models.

In this paper we present a Gaussian processes (GPs) based method for estimating the positions of a mobile robot. Our approach considers the different terrain conditions to improve prediction quality. Gaussian process regression (GPR) models are utilized to estimate the translational and rotational velocities of the robot. These estimated velocities are transferred into the position space using an unscented Kalman filter (UKF). By projecting the uncertainty values of the GPR estimates onto the positions, the UKF enables us to also capitalize the GPR uncertainties. To distinguish the different terrains the robot is traversing, we classify the spectrums of vertical accelerations using Gaussian process classification (GPC). The transitions between terrains are modeled by a 2-step Bayesian filter (BF). This allows us to assign different probabilities to distinct terrain sequences, as we incorporate the properties of the classifier.

The remainder of this paper is organized as follows: Related work is presented in Section 2. In Section 3 we explain GPs. In Section 4 we describe our dynamic approach. Experiments are shown in Section 5. We conclude in Section 6.

2 RELATED WORK

Several works study Gaussian processes (GPs) and their application to machine learning problems. A detailed view is provided by Rasmussen and Williams (Rasmussen and Williams, 2005). Other works are Williams (Williams, 2002), and MacKay (MacKay, 1998).

There is a lot of research on prediction of positions or trajectories of mobile robots. Many different systems are proposed, like a stereo-vision approach (Agrawal and Konolige, 2006), probability
networks (Burgard et al., 1996) or an approach using a particle filter combined with a Monte-Carlo method (Thrun et al., 2000). In (Seyer et al., 2005) artificial neural networks (ANN) are employed to build a model predictive controller (MPC). The current prediction error is considered to improve the quality of the velocity estimations. Another least-square support vector machine (LS-SVM) based controller adjusts its model iteratively by removing the least important data point from the model when adding a new point (Li-Juan et al., 2007).

Similar to the work presented here, GPs are used by Girard et al. (Girard et al., 2003) to make predictions several time steps ahead. The uncertainty of the previous step is integrated in the regression to track the increasing uncertainty of the estimation. Hence, the uncertainty value of the GP is the accumulated uncertainty of the previous time series. In contrast, we are able to relate the Gaussian uncertainties by using an UKF. A similar approach has been suggested by (Ko et al., 2007b), and (Ko et al., 2007a). They estimated the trajectory of an autonomous blimp by combining GPR with an UKF or ordinary differential equations (ODE), respectively. Localization of wireless devices, like mobile telecommunication devices or mobile robots is solved by modeling the probability distribution of the signal strength with GPs integrated in a BF (Ferris et al., 2006).

Several works employ information about the current terrain conditions to improve the navigation systems of mobile robots. One intuitive approach is to distinguish between traversable and non-traversable terrain (Dahlkamp et al., 2006), (Rasmussen, 2002). In contrast to the binary separation, Weiss et al. (Weiss et al., 2006) are using a SVM to classify the vertical accelerations and hence the terrain type. Using spectral density analysis (SDA) and principal component analysis (PCA) Brooks et al. (Brooks et al., 2005) concentrate on the vibrations a mobile robot experiences while driving. The preprocessed data records are categorized through a voting scheme of binary classifiers. Another way to analyse the driving conditions is to measure the slippage (Iagnemma and Ward, 2009), (Ward and Iagnemma, 2007).

Kapoor et al. (Kapoor et al., 2007) are using GPs with pyramid-match kernels to classify objects from visual data. Urtasun and Darrell (Urtasun and Darrell, 2007) chose a GP latent variable model to achieve a better classification by reducing the input dimension. Although many works concentrate on position estimation as well as terrain classification, none combined GPR and GPC to solve both problems at once for a velocity controller of high speed outdoor robots.

3 GAUSSIAN PROCESSES

GPs are applicable to regression as well as classification tasks. In contrast to other methods GPs do not have any parameters that have to be determined manually. However, the kernel function affects the properties of a GP essentially and must be chosen by hand. The parameters of GPs can be automatically optimized using the training data. Furthermore, GPs provide uncertainty values additionally to the estimates. These properties makes GPs attractive for regression and classification task like position estimation and terrain classification. However, a drawback of GPs is their running time which is quadratic in the number of training cases due to the inversion of the kernel matrix.

3.1 Regression

Computing the predictive distribution of GPs consists of three major steps. First, we determine the Gaussian distribution of the training data and the test data. To integrate the information of the training data into the later distribution, we compute the joint distribution. Finally, this joint distribution is transformed to the predictive equations of GPs by conditioning it completely on the training data.

Let \( X = [x_1, \ldots, x_n] \) be the matrix of the \( n \) training cases \( x_i \). The measured process outputs are collected in \( y = [y_1, \ldots, y_n] \). The noise of the random process is modeled with zero mean and variance \( \sigma_n^2 \). The kernel function is used to compute the similarities between two cases. Our choice is the squared exponential kernel given by

\[
k(x_i, x_j) = \exp\left(-\frac{1}{2}\|x_i - x_j\|^2\right),
\]
where $k$ is the kernel and $x_i, x_j$ are two inputs. A further quantity we need to provide is the prior distribution of the training data is the kernel matrix of the training data $K = K(X, X)$. It is given by $K_{ij} = k(x_i, x_j)$ using the kernel function. Now, we are able to specify the distribution of $y$:

$$y \sim \mathcal{N}(0, K + \sigma_y^2 I).$$

We are trying to learn the underlying function of $f$.

To get the distribution of the values of the underlying function $f = [f_1, \ldots, f_n]^\top$, we simply need to neglect the noise term from the distribution of the training data.

$$f \sim \mathcal{N}(0, K).$$

Secondly, we determine the distribution of the test data. Let $X_* = [x_{n+1}, \ldots, x_{n+m}]^\top$ be the set of $m$ test cases assembled in a matrix like the training data. $f_* = [f_{n+1}, \ldots, f_{n+m}]^\top$ are the function values of the test cases. The normal distribution of the test data is therefore given by

$$f_* \sim \mathcal{N}(0, K_*),$$

where $K_* = K(X_*, X_*)$ is the kernel matrix of the test cases, representing the similarities of this data points.

To combine training and test data distributions in a joint Gaussian distribution we further require the kernel matrix of both sets, denoted by $K = K(X, X_*)$. Consequently, the joint distribution of the training and test data is:

$$
\begin{bmatrix}
y \\
f_*
\end{bmatrix}
\sim \mathcal{N}
\left(0,
\begin{bmatrix} K + \sigma_y^2 I & K_* \\ K_*^\top & K_*
\end{bmatrix}
\right).
$$

This combination allows us to incorporate the knowledge contained in the training data into the distribution of the function values of the test cases $f_*$, the values of interest.

Since the process outputs $y$ are known, we can compute the distribution of $f_*$ by conditioning it on $y$, resulting in the defining predictive distribution of GP models:

$$f_*|X, y, X_* \sim \mathcal{N}(\mathbb{E}[f_*], \mathbb{V}[f_*])$$

with the mean and the variance given as

$$\mathbb{E}[f_*] = K_*^\top [K + \sigma_y^2 I]^{-1} y,$$

$$\mathbb{V}[f_*] = K_* - K_*^\top [K + \sigma_y^2 I]^{-1} K_*.$$

The final distribution is defined only in terms of the three different kernel matrices and the training targets $y$.

### 3.2 Classification

The basic principle of GPC for multi-class problems is similar to GPR. Yet GPC suffers from the problem that the class labels $p(y|f)$ are not Gaussian distributed. Hence, the distribution of the function values given the training data

$$p(f|X, y) = \frac{p(y|f)p(f|X)}{p(y|X)}$$

is also not Gaussian. $X$ and $f$ still denote the training data and its function values, whereas $y$ now represents the class labels of the training data. Yet to use GPs we have to have Gaussian distributed variables and must approximate $p(f|X, y)$, by the Laplace method for instance. Once the approximation is done, the further procedure is similar to GPR models, resulting in the predictive distribution of the GPC models $f_*|X, y, x_*$. Class probabilities are computed by drawing samples from this final distribution and applying the softmax function to squeeze the values into $[0, 1]$.

GPC have the same properties as GPR. The class probabilities can be seen as a confidence value and are perfectly suited to be combined with probabilistic filters.

### 4 DYNAMIC APPROACH

Simple controller consider only one type of terrain or use one averaged terrain model. In contrast, our approach considers the different effects on the kinematics of mobile robots caused by varying terrain conditions. Our algorithm splits naturally in two parts, the estimation of the robot’s position and the classification of the terrain. Figure 2 shows a graphical model of our dynamic approach.

#### 4.1 Position Estimation

The position estimation consists of two methods. We use GPs to do regression on the robot’s velocities and an UKF to transfer the results into the position space.
The values used were provided by an IMU installed on the robot. A series of preceding experiments were done to determine the composition of data types which in combination with the projection into the position space allowed the best position estimation. The data compositions compared in these experiments varied in two aspects, first the type of the data, and second the amount of past information.

The data combinations considered were: (1) the change in x-direction\(^1\) and y-direction, (2) the change in x-direction, y-direction and in the orientation, (3) the x-velocity and y-velocity, (4) the x-velocity, y-velocity and the change in the orientation, (5) the translational and rotational velocity, and (6) the translational and rotational velocity and the orientation change. The number of past values was altered from 1 to 4 values to determine the minimal amount of previous information necessary for the system to be robust, while at the same time does not cloud the data records and does not complicate the learning task. Leading to a total number of 24 different data compositions. While differing in the motion model and complexity, all approaches can be easily transformed into positions. However, some approaches suffer from a poor transformation function, making them rather useless.

The results showed that a single past value of the translational and rotational velocity works best for position estimation. Thus, the data records of the GPR reads as follows:

\[
[l_{t-1}, l_t, r_{t-1}, r_t, v_{t-1}, \omega_{t-1}]
\]

(10)

Since our Longcross robot has a differential drive, \(l_i\) and \(r_i\) denote the values of the speed commands to the robot for the left and right side of it’s drive. \(v_j\) and \(\omega_j\) represent the translational and rotational velocity, respectively. To learn a controller we need both the commands given to the robot and the implementation of these commands. The values of interest are the current velocities, \(v_i\) and \(\omega_i\).

We use GPR to solve this regression task which not only provides the estimates of translational and rotational velocities but also gives us uncertainty values. We transform the estimates into positions using an UKF. Additionally, the uncertainties are projected onto these positions and are propagated over time (Figure 3). Starting with a quite certain position the sizes of the error ellipses are increasing, due to the uncertainties of the velocity estimates and the increasing uncertainties of the previous positions they rely on.

Given only the first translational and rotational velocity, the regression does not rely on any further IMU values. It takes previous estimates as inputs for the next predictions. Assuming the first velocities to be zero (i.e. the robot is standing) makes our approach completely independent of the IMU device. However, IMU data is required for training.

For each type of terrain we trained two\(^2\) GPR models with data recorded only on that terrain. This has several advantages: Firstly, the effects of the robot commands on a specific terrain can be learned more accurately, since they are not contaminated by effects on other terrain types. Secondly, in combination more effects can be learned. And thirdly, due to the allocation of the training data to several GPR models the size and complexity of each model is smaller compared to what a single model covering all terrain types would require. The classification described in the next paragraph enables us to select the appropriate terrain models for regression.

### 4.2 Terrain Classification

The terrain classification is implemented with a GPC model, and a 2-step BF is used to model the transitions between terrains and to smooth the classification results.

As for the position estimation task preceding experiments were conducted to determine the best suited data records for the classification task. In contrast, here are mainly two possible data types, the vertical velocities and accelerations.

\(^1\)All directions are relative to the robot. The x-directions points always in the front direction of the robot, and the y-direction orthogonal laterally.

\(^2\)GPs are not able to handle multi-dimensional outputs. Hence, we need one GPR model for each velocity, translational and rotational.
By taking a look at the raw IMU data it is evident that the different terrains are hardly distinguishable and that it may need to be preprocessed. To be sure, we classified vertical velocity and acceleration records of varying sizes. Since the single values carry no information about the terrain, we took vectors of 25, 30, 35, and 40 values. The results showed the raw data to be improper for the classification task at hand.

The information about the terrain types is enclosed in the vibrations a mobile robot experiences while driving. We used the fast Fourier transform (FFT) to extract the frequency information. Given that the FFT works best with window sizes being a power of 2, we chose 16, 32, 64, and 128 as input lengths. Due to the symmetric structure of the FFT output, it is sufficient to use only the first half of the result. This reduces the complexity of the problem and allows us to consider larger window sizes as for the raw data. Using Fourier transformed vertical velocities and accelerations improved the classification results, as was expected. We found the vector of 128 velocities and accelerations improved the classification the raw data. Using Fourier transformed vertical velocities allowed us to consider larger window sizes as for the raw data. The results showed the raw data to be improper for the classification task at hand. Hence, the input to the GPC model is given by

$$\text{[fftaz0, ..., fftaz63]}, \quad (11)$$

where $\text{fftaz}_i$ denotes the $i$th value of the FFT result.

If the robot’s speed is too slow the terrain characteristics are not longer present in the vibrations, and therefore a good classification is impossible. Thus, we omit data for which the robot’s translational velocity is below some threshold $\tau$.

Due to the native characters of the terrains, the driving conditions vary within a terrain type. This makes it hard to achieve a perfect classification. To deal with false predictions and to account for the properties of the classifier, we used a 2-step BF to model the transitions between terrains. The quality values GPC models provide, come in terms of class probabilities which are well suited to be included into a probabilistic filter like the BF. The defining equation of our 2-step BF is slightly modified to accommodate the classification and the dependency on two previous beliefs.

$$b(x_{t|t-1}) \propto \sum_{x_{t-1|t-1}} \sum_{x_{t-2|t-2}} p(x_{t|t-1}|x_{t-1|t-1}, x_{t-2|t-2}) \cdot b(x_{t-1|t-1}) \cdot b(x_{t-2|t-2}) \quad (12)$$

The notation $x_{t|t-1}$ denotes the value of the state $x$ at time $t$ given all observations up to time $t-1$. $b(\cdot)$ is the belief, and $p(x_{t|t-1}|x_{t-1|t-1}, x_{t-2|t-2})$ represents the transition probabilities, i.e. the dependency on the previous states. At this point the belief of the current state $x_t$ depends only on the observations up to $z_{t-1}$. We include the current observation $z_t$ via the result of the classifier $c_t$.

$$b(x_{t|t}) \propto \frac{p(x_{t|t-1}|c_t, z_t) p(c_t|z_t)}{p(x_{t|t-1}|z_t)} \cdot b(x_{t|t-1}), \quad (13)$$

where $p(c_t|z_t)$ is the classification result. The output of our BF is the belief of state $x_t$ given all observations including $z_t$. It considers the classification and two previous states.

As already mentioned, the terrain classification is used to determine on which terrain the robot is currently driving and hence which terrain model should be used to estimate the next position. Since the robot commands required for the position estimation are given at a rate of approximately 3 Hz, whereas the terrain classification relies only on IMU data provided at 100 Hz, we implemented both parts to work independently of each other. However, it takes about a second to acquire enough data for classification, thus we reuse the last terrain model until a new classification will be performed and the current model will be updated.

### Algorithm 1 Dynamic Approach

**Input:** initialized and trained GPR and GPC models

while sensor data $q_t$ available do

1: $p_{a, t} = \text{UKF.process}(v_{a, t}, a_{a, t})$
2: $p_{g, t} = \text{GPC.predict}(v_{g, t})$
3: $b_p = \text{BF.process}(p_{a, t}, p_{g, t})$

4: if $p_{a, t}$ available and speed $> \tau$ then
5: $s_{s, t} = \text{FFT}(p_{a, t})$
6: $t_p = \text{GPC.classify}(s_{s, t})$
7: $\text{model} = \text{selectModel}(b_{p, t})$

8: end if
9: if $\text{model}(\text{FFT}(p_{a, t}))$ then
10: $\text{pos} = \text{UKF.predict}(v_{a, t}, a_{a, t})$
11: $\text{publish}(\text{pos})$

12: end while

The algorithm requires trained GP models. If sensor data $q_t$ is available, the algorithm predicts the velocity values using the current terrain model. If sufficient vibration data $p_{a, t}$ is available for classification (omitting low speed data), a new classification of the terrain will be performed and the current model will be updated.

### 5 EXPERIMENTAL RESULTS

The Longcross (Figure 1) is an experimental platform weighing about 340 kg with a payload capacity of at least 150 kg. The compartment consists of carbon-fibre and is environmentally shielded. Our version is equipped with a SICK LMS 200 2D laser scanner, a Velodyne Lidar HDL-64E S2 3D laser scanner, and


an Oxford Technical Solutions Ltd RT3000 combined GPS receiver and inertial unit. The software runs on a dedicated notebook with an Intel Core 2 Extreme Quad processor and 8 GB memory.

5.1 Simple Approaches

We evaluated our approach on a test drive covering three different terrains, starting on field, continuing with grass, and ending on asphalt. The test sequence consists of 190 positions (about a 1 minute) almost evenly partitioned on the three terrains. We compared our dynamic approach to a field model, an asphalt model, a grass model and an averaged model. The first three models were trained only on the specific terrain. The averaged model was trained on all three terrains equally. All models used a total of 1500 training cases. The dynamic approach utilizes the three terrain specific models.

We used the mean squared error (MSE) and the standardized MSE to evaluate the quality of the regression. The SMSE is the MSE divided by the variance of the test points, thus it does not depend on the overall scaling of the values. The MSE is not applicable to measure the quality of a trajectory because errors at the beginning are propagated through the entire trajectory influencing all proceeding positions. So we introduced the mean segment distance error (MSDE). First, we split the original trajectory and the prediction in segments of fixed size. Each pair of segments is normalized to the same starting position and orientation. The distance of the resulting end positions is computed subsequently. The mean of all these distances constitutes the MSDE. We found a segment size of 10 to be a reasonable size.

The estimation results of the translational (upper row) and the rotational velocities (lower row) of the field model, the averaged model and of our dynamic approach are shown in Figure 4. The field model is the best of the simple models. The averaged model would be the model of choice if one wants to consider different terrain conditions but does not want to employ a dynamic approach.

The estimation of the translational velocities by the averaged model shows little or no reaction to any of the outliers. Averaging the effects of commands over several terrains involves diminishing ef-
Table 1: Prediction quality. The translational velocity unit is \( m/s \), the rotational velocity unit is \( \text{rad}/s \), and the MSDE unit is \( m \).

<table>
<thead>
<tr>
<th>Model</th>
<th>MSE</th>
<th>SMSE</th>
<th>MSDE</th>
</tr>
</thead>
<tbody>
<tr>
<td>Field</td>
<td>0.02522</td>
<td>0.10588</td>
<td>0.42923</td>
</tr>
<tr>
<td>Asphalt</td>
<td>0.07032</td>
<td>0.29517</td>
<td>0.56363</td>
</tr>
<tr>
<td>Grass</td>
<td>0.05161</td>
<td>0.21662</td>
<td>0.51907</td>
</tr>
<tr>
<td>Averaged</td>
<td>0.06203</td>
<td>0.26038</td>
<td>0.45478</td>
</tr>
<tr>
<td>Dynamic</td>
<td>0.01181</td>
<td>0.04956</td>
<td>0.31407</td>
</tr>
</tbody>
</table>

The effects of certain command-terrain combinations, hence causing inaccurate estimates. The field model performs best of the simple approaches, mainly because it recognizes the slowdown around the 70th test case. However, the other two outliers are not identified. The estimates of the remaining test cases are similar to the averaged model, yet the field model is slightly superior. Our dynamic approach outperforms both previous models. In contrast, it recognizes all outliers, as the right terrain model is applied most of the times. Additionally, the estimates of each test point are pretty accurate.

The estimates of the rotational velocities give a similar picture. The averaged model is somewhat off at the beginning, underestimating the true values. The field model is much more accurate. The error bars seem to be larger than in the upper row but it is due to the scale of the data. However, our approach again provides the best estimation, reacting even to minor changes in the velocity values.

The velocities are translated into positions using an UKF. The resulting trajectories of all models tested are shown in Figure 5. The previous tendencies are reflected in the quality of the trajectories. The averaged model’s trajectory is rather inaccurate, followed by the trajectory of the field model which is outperformed by our dynamic approach. At the beginning the predicted tracks are close, the differences start during the first turn and increase by the time. Even though the distinction between the velocity estimates are relatively small, the impact on the trajectories are formidable. Especially the rotation values are crucial to the trajectory quality.

We analyzed the quality of the GPR estimations of the velocities with the MSE and the SMSE. Due to the reasons mentioned above, the trajectories are evaluated by the MSDE. The results are presented in Table 1.

Table 2 lists the classification quality in terms of correct classifications and applied models. Also, the classification rates are broken down into the classes giving more insight.

5.2 Dynamic Approaches

In the previous section we compared our dynamic approach to single terrain models, which by definition cannot be optimal when the robot drives on several different terrains. Therefore, we constructed another dynamic approach similar to the one presented. By doing so, we combined a support vector machine (SVM) to perform the regression of the velocities, and a k-nearest neighbor (k-NN) method for classification. We chose to combine a SVM and k-NN because of their low runtimes. The conducted experi-
Figure 7: Comparison of the two dynamic approaches. Estimation of the translational velocities (left column), and of the rotational velocities (right column) with error bars.

ments showed the overall runtime of the GP approach to be a serious issue.

We omitted the UKF from the system because the SVM does not provide any uncertainty values. These values are essential to the UKF in order to work properly. However, we kept the 2-step BF, even though the k-NN method usually returns simple class labels rather than class probabilities. We counted the votes for each class and divided them by the total number of neighbors $k$ to provide class probabilities anyway. We used the LibSVM library (Chang and Lin, 2001) with a radial basis function (RBF) as SVM kernel and found the OpenCV k-NN implementation with $k = 8$ neighbors to work best for vibrations.

To train the terrain models of the SVM we used the same training data as we did for the GP models. The training set of the classifiers are also unchanged.

Since this approach is able utilize several terrain models for prediction, it should be more competitive than the single terrain model approaches. To distinguish the two dynamic approaches, we will refer to the GP based system as GP-Approach and to the SVM and k-NN system as SVM-Approach.

The top row of Figure 7 shows the estimations of the translational and rotational velocities by the GP-Approach from the previous section. The prediction results of the SVM-Approach are illustrated below. Both dynamic approaches fit the original translational velocities fairly accurately and recognize all outliers. The estimation differences between the two systems are somewhat more apparent when we concentrate on the rotational velocities. The SVM-Approach underestimates the first part and overestimates the velocities towards the end. Its predictions are more agitated in contrast to the averaging characteristic of the GP estimations.

The observations are reflected in the error values of Table 3. Even though the errors of the dynamic approaches are very small - they are the smallest of all tested models - the values of the SVM-Approach are more than $\frac{1}{3}$ higher. As we will see later, this is

<table>
<thead>
<tr>
<th>Model</th>
<th>MSE</th>
<th>SMSE</th>
<th>MSDE10</th>
</tr>
</thead>
<tbody>
<tr>
<td>GP</td>
<td>$v$</td>
<td>0.01181</td>
<td>0.04956</td>
</tr>
<tr>
<td>Approach</td>
<td>$\omega$</td>
<td>0.00279</td>
<td>0.19917</td>
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<td>$v$</td>
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<td>0.08073</td>
</tr>
<tr>
<td>Approach</td>
<td>$\omega$</td>
<td>0.00464</td>
<td>0.33089</td>
</tr>
</tbody>
</table>

Table 3: Prediction quality of the two dynamic approaches. The translational velocity unit is $m/s$, the rotational velocity unit is $rad/s$, and the MSDE unit is $m$. 
partly due to the lower k-NN classification quality.

The SVM’s underestimation of the rotational velocity corresponds to the assumption of a less sharper turn. The green trajectory in Figure 8 shows exactly this behavior. Furthermore, the higher estimated rotational velocities at the end of the trajectory result in tighter turns. Regardless of the rather different predictive trajectories, the trajectory qualities in Table 3 are almost the same.

With respect to the classification task the GP classifier performs much better than the k-NN classifier. The sequence of classifications and applied models are compared in Figure 9. While the GP-Approach keeps the current terrain until enough evidence is present that the terrain may have changed, the SVM-Approach tends to change the terrain class more quickly. This makes the system to apply the wrong terrain model more often.

Table 4 and 5 point out that the k-NN classifier struggles to distinguish grass and field records. Leading to a performance more than 25% worse than the GP classification. Evaluating the quality of the applied models, we can see a slight improvement by about 5%, still staying way behind our approach.

As stated earlier the classification quality is crucial to the performance of the overall system, since false classifications lead to the application of wrong terrain models, resulting in worse velocity estimations. However, the SVM-Approach, incorporating SVM regression and k-NN classification, is significantly faster than our GP-Approach.

### 6 CONCLUSION

In this paper we introduced a dynamic approach to estimate positions of a mobile robot. Since the terrain conditions are crucial to the robot’s implementation of velocity commands, we consider the terrain for the prediction of future positions. We used GPs for the regression of translational and rotational velocities. An UKF transfers the velocity estimates into positions and propagates the uncertainties of the positions over time. The vibration affecting the robot are classified by a GPC model in order to separate different terrains. A 2-step BF is used to compensate for classification errors and to model the terrain transitions.

The prediction problem considered in this paper has several difficult properties: first, with respect to the classification task, the visual ground truth is not always accurate. Due to natural terrain types, which in themselves can be vastly different, vibrations induced by separate terrains may sometimes look alike or even show characteristics of another terrain. In a consequence, making it tricky to evaluate the classifier’s performance. Second, finding a reasonable diversity of terrains is quite challenging, which aggra-
vates the task of determining the transition probabilities from real data.

Nevertheless, our approach proved to be more effective than simple approaches utilizing a single model for all terrains. Furthermore, our GP-Approach is competitive with other dynamic approaches using different machine learning techniques. The dynamic systems, our GP-Approach and the slightly structurally altered SVM-Approach, are both better than all simple models, proving the basic idea of our approach to be well suited to solve such prediction problems.

Future work will be to reduce the run time. Due to the use of GPs the entire systems suffers of a long run time. Several sparse algorithms for GPs exist which would help to improve this issue. Moreover, expanding the current system by additional terrains as sand or gravel would be desirable. Extending the classification records by the translational velocity could improve classification results, since it allows to learn the effects of different speeds on the vibrations.

References


