Bounds and Algorithms for Multiple Frequency Offset Estimation in Cooperative Networks

Hani Mehrpouyan†, Member, IEEE, and Steven D. Blostein§, Senior Member, IEEE,
†Department of Signals and Systems, Chalmers University of Technology, Sweden,
§Department of Electrical and Computer Engineering, Queen’s University, Canada,
Emails: hani.mehr@ieee.org and steven.blostein@queensu.ca

Abstract—The distributed nature of cooperative networks may result in multiple carrier frequency offsets (CFOs), which make the channels time varying and overshadow the diversity gains promised by collaborative communications. This paper seeks to address multiple CFO estimation using training sequences in space-division multiple access (SDMA) cooperative networks. The system model and CFO estimation problem for cases of both decode-and-forward (DF) and amplify-and-forward (AF) relaying are formulated and new closed-form expressions for the Cramer-Rao lower bound (CRLB) for both protocols are derived. The CRLBs are then applied in a novel way to formulate training sequence design guidelines and determine the effect of network protocol and topology on CFO estimation. Next, two computationally efficient iterative estimators are proposed that determine the CFOs from multiple simultaneously relaying nodes. The proposed algorithms reduce multiple CFO estimation complexity without sacrificing bandwidth and training performance. Unlike existing multiple CFO estimators, the proposed estimators are also accurate for both large and small CFO values. Numerical results show that the new methods outperform existing algorithms and reach or approach the CRLB at mid-to-high signal-to-noise ratio (SNR). When applied to system compensation, simulation results show that the proposed estimators significantly reduce average-bit-error-rate (ABER).

Index Terms—Cooperative communications, synchronization, carrier frequency offset estimation, Cramer-Rao Lower Bound (CRLB), MUltiple SInal Characterization (MUSIC).

I. INTRODUCTION

COOPERATIVE multiplexing and diversity, which are achieved when multiple terminals collaborate through distributed transmissions, are shown to increase capacity and reliability in wireless networks [1]–[5]. However, the majority of the analysis in the area of cooperative communications is focused on improving capacity and reliability while assuming perfect frequency synchronization [1]–[5].

The presence of multiple carrier frequency offsets (CFOs) in distributed cooperative networks arises due to simultaneous transmissions from spatially separated nodes with different oscillators and Doppler shifts. The CFOs result in the rotation of the signal constellation causing signal to noise ratio (SNR) loss. The amount of SNR loss and channel estimation accuracy are highly dependent on CFO estimation precision at the receiver [6]. Thus, accurate CFO estimation is key to successful deployments of cooperative networks.

In [7]–[9] and references therein, space time coding techniques are proposed that provide full spatial diversity in the presence of CFOs. However, the schemes outlined in [7]–[9] require CFOs to be estimated and equalized at the destination and do not address CFO estimation.

Previously proposed multiple CFO estimation methods for frequency-flat multiple-input-multiple-output (MIMO) systems include [10]–[13]. In [10], a maximum-likelihood estimator (MLE) is presented that requires exhaustive search and performs poorly when the CFOs are close to one another. In [11], a correlation-based estimator (CBE) is proposed using orthogonal training sequences transmitted from different antennas. However, the CBE suffers from an error floor, requires the use of correlators at the receiver, and performs very poorly when normalized CFO values are larger than 0.05. In [12] and [13], iterative schemes are proposed to eliminate the CBE’s error floor. However, since CBE is used as the initial estimator, the estimators in [12] and [13] also perform poorly at large CFO values. While the assumption of small CFO values in [11]–[13] might hold for point-to-point MIMO systems, it is not justifiable for cooperative systems with distributed nodes and independent oscillators. In addition, the estimators in [10]–[13] cannot be directly applied to the case of amplify-and-forward (AF) relaying networks due to the different training signal model.

In [15] a maximum a posteriori (MAP) CFO estimator for single-relay frequency-flat 3-terminal decode-and-forward (DF) networks is presented. However, the approach in [15] is limited to the case of DF relaying and suffers from the same shortcomings as in [10]. While a multiple CFO estimator for DF relaying cooperative networks is proposed in [16], no specific performance analysis is provided. In [17], CFO estimation in two-way AF relaying networks is investigated. However, the system model consists of a single relay only and the effect of Doppler shift is ignored. In [18], CFO estimation in multi-relay orthogonal frequency division multiple access (OFDMA)-based cooperative networks is addressed. However, to simplify the CFO estimation problem, it is assumed in [18] that at any given time only a single relay transmits its signal to the receiver. Finally, CFO estimation in AF relaying single-relay orthogonal frequency division multiplexing (OFDM)-based cooperative networks has been analyzed in [19], where similar to [18], it is assumed that the received signal is affected by only a single CFO.

1This research has been supported in part by Defense R&D Canada through the Defense Research Program at the CRC Canada and in part by NSERC Discovery Grant 41731.

2This work is part of the first author’s Ph.D. dissertation, which was completed at Queen’s University.
The Cramer-Rao lower bound (CRLB) [20] has been used as a quantitative performance measure for CFO estimators and can be applied to determine the effects of network protocol and topology on CFO estimation accuracy in cooperative systems. The CRLB for CFO estimation in MIMO point-to-point systems is derived in [10]. In [15], the CRLB for 3-terminal DF cooperative networks is presented. However, the analysis in [15] is limited to single-relay DF networks and the results are based on an assumed Gaussian distribution for the CFO, which is not realistic, given that the sources of CFO do not undergo significant changes, as shown in [10]–[13], [21], [22]. To the best of the authors’ knowledge there are no CRLB results in the literature for joint estimation of multiple CFOs and channel gains in a multi-relay cooperative network.

The Multiple Signal Characterization (MUSIC) algorithm is a spectral estimation method that has been applied to the estimation of parameters of a received signal, including CFO and direction-of-arrival in point-to-point systems [23]. The application of the MUSIC algorithm to CFO estimation in multi-relay or multi-user networks is difficult, however, due to the following shortcomings: i) estimating closely-spaced CFO values, and ii) no method of assigning each CFO to its source. In the case of OFDMA-based systems, the MUSIC algorithm has been proposed as a suitable method of estimating each user’s CFO [24], [25]. However, to address the shortcomings of MUSIC, the algorithms in [24], [25] are based on the assumptions that in OFDMA systems, the users’ carrier frequencies are well spaced and each user has a specific set of subcarriers assigned to it. Both of these assumptions are not applicable to space-division multiple access (SDMA) networks, where multiple relays simultaneously transmit their signals over the same frequency band [4], [5], [9].

Under the consideration of frequency-flat fading channels, this paper seeks to extend the results in [26] so as to derive more general expressions of the CRLB, provide a more comprehensive investigation of the performance of the proposed estimators, and gain insight on the effect of CFO estimation accuracy on the performance of cooperative networks. The contributions and organization of this paper can be summarized as follows:

- In Section II, a system model for CFO estimation in DF and AF relaying networks is outlined. Flat-fading channels are considered, which is motivated by pioneering work in the area of multiple CFO and channel gain estimation for MIMO and cooperative networks [10]–[13], [15], [16]. In addition, consideration of frequency-selective channels for multi-relay cooperative networks would require estimation of very large numbers of parameters and is beyond the scope of this paper.
- In Section III, new closed-form CRLB expressions for CFO estimation for AF and DF multi-relay cooperative systems are derived. In addition to serving as a benchmark for assessing the performance of CFO estimators, the CRLBs are used in a novel way to quantitatively determine the effect of network protocol and number of relays on CFO estimation accuracy.
- Section IV proposes an algorithm that uses linearly independent training sequences transmitted from each relay to address certain shortcomings of MUSIC and accurately estimate and assign each CFO to its corresponding relay. Unlike the algorithms in [10]–[13] the proposed estimators have accuracies that are maintained over the full range of possible CFO values. Moreover, it is shown that the proposed CFO estimators are also applicable to AF relaying networks. Finally, a complexity analysis for both estimators is presented.
- In Section V, numerical results are presented showing that the proposed estimators either reach or approach the CRLB at mid-to-high SNR. By combining the proposed CFO estimation technique with the CFO compensation method in [27], it is also shown that frequency synchronization and significant performance gains in cooperative networks may be achieved.

Notation: italic letters (x) are scalars, bold lower case letters (x) are vectors, bold upper case letters (X) are matrices, X_{k,m} represents the kth row and mth column element of X, I denotes the identity matrix, \( \odot \) stands for Schur (element-wise) product, and \((\cdot)^*, \,(\cdot)^T, \,(\cdot)^H, \) and Tr(\cdot) denote conjugate, transpose, conjugate transpose (hermitian), and trace, respectively.

II. SYSTEM MODEL

A half-duplex SDMA cooperative network consisting of a source and destination pair and a cluster of R relay nodes is considered, where the relays are assumed to be distributed throughout the network as shown in Fig. 1. Multiple CFO estimation using a training sequence (TS) is analyzed, where during the training interval, the CFOs and channel gains corresponding to R relay nodes are estimated. These estimates can be applied in the data transmission interval to improve system performance. Throughout this paper, the following set of assumptions and system design parameters are considered:

1. In Phase I the source broadcasts its TS to the relays and in Phase II the relays transmit R linearly independent and orthonormal TSs simultaneously to the destination, as in Fig. 1.
2. Without loss of generality, it is assumed that unit amplitude phase-shift keying (PSK) TSs are transmitted.
3) Quasi-static and flat-fading channels are considered, where the channel gains are assumed not to change over the length of a frame of symbols but to change from frame to frame.
4) CFOs are modeled as unknown non-random parameters.
5) Similar to most CFO and channel estimation methods, it is assumed that nodes within the network are synchronized in time [10]–[13]. In addition, it is noted in [10], [21] that timing offset estimation can be decoupled from CFO estimation.

Note that Assumptions 2, 3, and 4 are in line with previous CFO estimation analyses in [10]–[13], [21] and are also intuitively justifiable, since the main sources of CFO are oscillator mismatch and Doppler shift. In addition, oscillator properties, Doppler shifts, and channel gains are assumed not to change significantly during a transmission block consisting of TS and data.

A. Training Signal Model for DF Relaying Cooperative Networks

1) Training Signal Model at the Relays: For DF relaying, the signal at the relays is down-converted to baseband, matched-filtered, and decoded [1], [2], [9], [28]. Thus, the CFO from the source to the $k$th relay, $v_k[0]$, for $k = 1, 2, \ldots, R$, needs to be estimated at each relay, similar to that of a single-input-single-output (SISO) system. The baseband received training signal, $r_k(n)$ at the $k$th relay node at time $n$, for $n = 1, \ldots, L$ and $k = 1, \ldots, R$, is given by

$$r_k(n) = h_k e^{j2\pi\nu_k[0]} t_s(n) + v_k(n),$$

where:
- $L$ denotes the length of the TS,
- $t_s [\triangleq [t_s(1), \ldots, t_s(L)]^T]$ is the known TS broadcast from the source to the relay nodes,
- $\nu_k[0] \triangleq \Delta\nu_k[0]T$ is the normalized CFO from the source to the $k$th relay with T as the symbol duration,
- $h_k$ represents the unknown channel gain from the source to the $k$th relay, and
- $v_k(n)$ is the zero-mean additive white Gaussian noise (AWGN) at the $k$th relay with variance $\sigma_v^2$ and denoted by $\mathcal{C}\mathcal{N}(0, \sigma_v^2)$.

2) Training Signal Model at the Destination: The baseband received training signal model at the destination, $y$, for a DF cooperative network consisting of $R$ relay nodes is given by

$$y(n) = \sum_{k=1}^{R} g_k e^{j2\pi\nu_k[0]} t^r_k(n) + w(n), \quad n = 1, \ldots, L$$

where:
- $t^r_k [\triangleq [t^r_k(1), \ldots, t^r_k(L)]^T]$ is the distinct and known TS transmitted to the $k$th relay,
- $g_k$ denotes the unknown channel gain from the $k$th relay to the destination,
- $\nu_k[0] \triangleq \Delta\nu_k[0]T$ is the normalized CFO from the $k$th relay to the destination,

$\nu_k[0]$ is the CFO from the source to the $k$th relay, and $\nu_k[0]$ is the normalized CFO from the $k$th relay with T as the symbol duration. $h_k$ represents the unknown channel gain from the source to the $k$th relay, and $v_k(n)$ is the zero-mean additive white Gaussian noise (AWGN) at the $k$th relay with variance $\sigma_v^2$ and denoted by $\mathcal{C}\mathcal{N}(0, \sigma_v^2)$. $w(n)$ is the AWGN at the destination with $\mathcal{C}\mathcal{N}(0, \sigma_w^2)$.

According to (2), the CFOs $\nu_k[0] \triangleq [\nu_k[0], \ldots, \nu_k[0]]^T$, and channel gains, $g \triangleq [g_1, \ldots, g_R]^T$, need to be jointly estimated at the destination.

B. Training Signal Model for AF Relaying Cooperative Networks

1) Training Signal Model at the Relays: Since signals traveling through different channels experience different Doppler shifts and different oscillator offsets, the received signal at the destination is affected by multiple CFOs even if the relay does not convert the signal to baseband. Hence, to achieve frequency synchronization in an AF relaying network, we propose the baseband processing structure in Fig. 2 at each relay. In practice, AF relaying networks typically require signals at the relays to be converted to baseband [1], [4]. We remark that the proposed baseband processing structure of Fig. 2 does not increase hardware complexity at the relays and is significantly simpler than that of DF networks, which require relays to be equipped with a matched filter, decoder, and pulse shaping filter for retransmission.

Fig. 2. The baseband processing structure at the relays in the case of AF relaying multi-relay networks ($f_{k}^r$ denotes the carrier frequency at the $k$th relay).

2) Training Signal Model at the Destination: For AF relaying, the signal model is given by

$$y(n) = \sum_{k=1}^{R} \zeta_k g_k h_k e^{j2\pi\nu_k[0]} t^r_k(n) t_s(n) + w(n), \quad n = 1, \ldots, L$$

where $\zeta_k$ is a scaling factor that is used to satisfy the $k$th relay’s power constraint, $\nu_k[0] \triangleq \nu_k[0] + \nu_k[0]$, $t^r_k(n)$ is used to modulate the received TS, $t_s(n)$ to ensure the $k$th relay has a specific TS.

Eq. (3) follows from the fact that the received signal, $r_k(n)$, is amplified and forwarded without being decoded. Note that in (3), $t_k^r = [t_k^r(1), \ldots, t_k^r(L)]^T$ does not change the statistical properties of the noise, $v_k$, assuming unit-amplitude PSK training symbols.

According to (3), $2R$ quantities containing CFOs are present in the signal model: 1) $\nu_{sum} [\triangleq [\nu_1[0], \ldots, \nu_R[0]]^T$, which result in rotation of the signal constellation and 2) $\nu_{rd} [\triangleq [\nu_1[0], \ldots, \nu_R[0]]^T$, which affect the noise at the relays. Since
components of $\nu^{[dl]}$ only phase-shift the noise in (3) and do not affect signal detection, the terms $\nu^{[sum]}$ are the only CFO-related quantities that influence system performance. From the above, we conclude that it suffices to estimate $\nu^{[sum]}$ at the destination.

Note that it has been shown in [29] that for effective signal detection at the destination in the case of AF relaying cooperative networks, only the overall channel gains from source-relay-destination links, $g_k h_k$, for $k = 1, \ldots, R$, need to be estimated at the destination, whereas the channel gains $h \triangleq [h_1, \ldots, h_R]^T$ and $g \triangleq [g_1, \ldots, g_R]^T$ do not need to be estimated separately.

III. CRAMER-RAO LOWER BOUND

In this section, the CRLBs for joint CFO and channel estimation in multi-relay networks are derived.

A. Amplify-and-Forward Cooperative Networks

The signal model in (3) can be rewritten as

$$y(n) = \sum_{k=1}^{R} \left( \zeta_k \alpha_k e^{j2\pi n \nu^{[sum]}_k} c_k(n) + \beta_k e^{j2\pi n \nu^{[out]}_k} \tilde{v}_k(n) \right) + w(n), \tag{4}$$

where $\alpha_k \triangleq g_k h_k$, $\beta_k \triangleq \zeta_k g_k c_k(n) \triangleq \tilde{v}_k(n)^{*} l_k^{[*]}(n)$, and $\tilde{v}_k(n) \triangleq \tilde{v}_k^{[*]}(n)/v_k(n)$. Note that due to the assumption of unit-amplitude PSK Ts, $\tilde{v}_k$ has the same statistical properties as $v_k$.

Based on the signal model in Section II B., the vector of parameters of interest, $\lambda^{[AF]}$, is given by

$$\lambda^{[AF]} \triangleq \left[ \begin{array}{c} \text{Re}\{\alpha\}^T, \text{Im}\{\alpha\}^T, (\nu^{[sum]}_{\text{out}})^T \end{array} \right]^T,$$

where $\alpha = [\alpha_1, \ldots, \alpha_R]^T$, and $\text{Re}\{\cdot\}$ and $\text{Im}\{\cdot\}$ denote real and imaginary parts, respectively.

Throughout this section AWGN at the relays and destination is considered, where $v_k = [v_k(1), \ldots, v_k(L)]^T$, for $k = 1, 2, \ldots, R$, and $w = [w(1), \ldots, w(L)]^T$ are distributed according to $CN(0, \sigma_v^2 I)$ and $CN(0, \sigma_w^2 I)$, respectively. Moreover, $v_k$, $v_m$, $\forall k \neq m$, and $w$, are assumed to be mutually independent.

Based on the above set of assumptions, the vector of received training signal, $y = [y(1), \ldots, y(L)]^T$, is distributed as $CN(\mu_y, \Sigma_y)$, where $\mu_y$ and $\Sigma_y$ are given by

$$\mu_y = \sum_{k=1}^{R} \alpha_k e^{j \nu^{[sum]}_k}, \quad \text{and}$$

$$\Sigma_y = \left[ \begin{array}{l} \left( \sum_{k=1}^{R} \beta_k e^{j 2 \pi n \nu^{[out]}_k} l_k^{[*]}(i) v_k(l) + w(l) \right) \\
\times \left( \sum_{m=1}^{R} \beta_m e^{j 2 \pi n \nu^{[out]}_m} l_m^{[*]}(i) w_m(i) + w(i) \right) \end{array} \right]^H \tag{7a}$$

$$= \sum_{k=1}^{R} \sum_{m=1}^{R} \beta_k \beta_m^* E \left[ e^{j 2 \pi n \nu^{[out]}_k l_k^{[*]}(i)} \left( e^{j 2 \pi n \nu^{[out]}_m l_m^{[*]}(i)} \right)^* \right]$$

$$\times E[v_k(l) v_m(i)] + E[w(l) w(i)] \tag{7b}$$

$$= \begin{cases} 0 & i \neq l \\
\sum_{k=1}^{R} |\beta_k|^2 \sigma_v^2 + \sigma_w^2 & i = l \end{cases} \tag{7c}$$

where $e^{[sum]}_k \triangleq \zeta_k \left[ c_k(1) e^{j 2 \pi n \nu^{[sum]}_k}, \ldots, c_k(L) e^{j 2 \pi n \nu^{[sum]}_k} \right]^T$. Note that (7b) follows from the fact that the noise at the destination and $k$th relay, $w$ and $v_k$, respectively, are mutually independent, $\forall k$, and (7c) follows the AWGN assumption, where $E[w(i) w(l)] = 0$ for $i \neq l$. Thus, $\Sigma_y$ is given by

$$\Sigma_y = \left( \sum_{k=1}^{R} |\beta_k|^2 \sigma_v^2 + \sigma_w^2 \right) I. \tag{8}$$

To determine the CRLB, the $3R \times 3R$ Fisher’s Information Matrix (FIM) needs to be determined. For parameter estimation from a complex Gaussian observation sequence, the FIM entries are given by [20]

$$\text{FIM}(\lambda)_{k,m} = 2 \text{Re} \left\{ \frac{\partial \mu_y}{\partial \lambda_k} \frac{\partial \mu_y}{\partial \lambda_m} \right\} + \text{Tr} \left( \Sigma_y^{-1} \frac{\partial \Sigma_y}{\partial \lambda_k} \Sigma_y^{-1} \frac{\partial \Sigma_y}{\partial \lambda_m} \right), \tag{9}$$

where $\lambda = \lambda^{[AF]}$ is defined in (5). The corresponding components of the CRLB are computed as

$$\frac{\partial \mu_y}{\partial \lambda_k} = j \alpha_k D_k \nu^{[sum]}_k, \quad \frac{\partial \mu_y}{\partial \lambda_m} = -j \frac{\partial \mu_y}{\partial \text{Im}\{\alpha\}} = e^{[sum]}_k, \tag{10}$$

where $D_k \triangleq \text{diag}(2\pi, 4\pi, \cdots, 2L \pi)^1$, Note that (11a) and (11b) follow (8) due to the fact that $\frac{\partial \mu_y}{\partial \text{Re}\{\alpha\}} = 0$.

After substituting the derivatives in (10), (11a), and (11b) into (9) and after carrying out straightforward algebraic manipulations for $k, m = 1, \ldots, R$, we arrive at

$$\text{FIM}_{k,m} = \frac{2}{\sigma_n^2} \text{Re} \left\{ \left( e^{[sum]}_k \right)^H e^{[sum]}_m \right\} + 2L \text{Re} \left\{ \alpha_k \frac{\partial \mu_y}{\partial \lambda_k} \alpha_m \frac{\partial \mu_y}{\partial \lambda_m} \right\} \frac{\sigma_v^2 \sigma_w^2 \zeta_k^2 \zeta_m^2}{\sigma_n^2}, \tag{12}$$

$$\text{FIM}_R, k = m = \frac{2}{\sigma_n^2} \text{Re} \left\{ \left( e^{[sum]}_k \right)^H e^{[sum]}_m \right\} + 2L \text{Re} \left\{ \alpha_k \frac{\partial \mu_y}{\partial \lambda_k} \alpha_m \frac{\partial \mu_y}{\partial \lambda_m} \right\} \frac{\sigma_v^2 \sigma_w^2 \zeta_k^2 \zeta_m^2}{\sigma_n^2}, \tag{13}$$

$$\text{FIM}_{k,2R+m} = \frac{2}{\sigma_n^2} \text{Im} \left\{ \left( e^{[sum]}_k \right)^H e^{[sum]}_m \right\} + 2L \text{Im} \left\{ \alpha_k \frac{\partial \mu_y}{\partial \lambda_k} \alpha_m \frac{\partial \mu_y}{\partial \lambda_m} \right\} \frac{\sigma_v^2 \sigma_w^2 \zeta_k^2 \zeta_m^2}{\sigma_n^2}, \tag{14}$$

$$\text{FIM}_{R+k,2R+m} = \frac{2}{\sigma_n^2} \text{Re} \left\{ \left( e^{[sum]}_k \right)^H e^{[sum]}_m \right\} + 2L \text{Re} \left\{ \alpha_k \frac{\partial \mu_y}{\partial \lambda_k} \alpha_m \frac{\partial \mu_y}{\partial \lambda_m} \right\} \frac{\sigma_v^2 \sigma_w^2 \zeta_k^2 \zeta_m^2}{\sigma_n^2}, \tag{15}$$

$$\text{FIM}_{R+k,2R+m} = \frac{2}{\sigma_n^2} \text{Re} \left\{ \alpha_k \left( e^{[sum]}_k \right)^H e^{[sum]}_m \right\} \tag{16}$$
of interest, can be rewritten in compact form as shown in (18) at the bottom of this page. In (18),

- \[\mathbf{D}_\alpha|_{R \times R} \triangleq \text{diag}(\alpha_1, \ldots, \alpha_R),\]
- \[\mathbf{E}_{\nu|\text{sum}}|_{L \times R} \triangleq \begin{bmatrix} \mathbf{e}_1^{[\text{sum}]}, & \cdots, & \mathbf{e}_R^{[\text{sum}]} \end{bmatrix},\]
- \[\mathbf{\rho} =\begin{bmatrix} \sqrt{\sigma_1^2} \alpha_1^2 \sigma_2^2, \cdots, \sqrt{\sigma_R^2} \alpha_R^2 \sigma_2^2 \end{bmatrix}^T.\]

Next, using partitioned matrix inverse in a similar manner to that in [10], [30], a closed-form expression for the CRLB for CFO estimation in the case of AF relaying cooperative networks can be derived as shown in (19) at the bottom of this page. In (19),

- \[\mathbf{[Y]}|_{R \times R} \triangleq \mathbf{D}_H^T \mathbf{H}_{\nu|\text{sum}} \mathbf{D}_\alpha \mathbf{E}_{\nu|\text{sum}} \mathbf{D}_\alpha,\]
- \[\mathbf{[\Pi]}|_{R \times R} \triangleq \mathbf{H}_{\nu|\text{sum}}^T \mathbf{D}_\alpha \mathbf{E}_{\nu|\text{sum}} \mathbf{D}_\alpha,\]
- \[\mathbf{F}_{2R \times 2R} \text{ is the first } 2R \text{ rows and } 2R \text{ columns of the FIM in (18).}\]

In order to derive the CRLB for the estimation of the combined real and imaginary parts of channel gains, \(\alpha\), the set of parameters of interest, \(\lambda^{[\text{AF}]}\), is modified as

\[
\lambda^{[\text{AF}]} \triangleq \begin{bmatrix} \mathbf{I} & \mathbf{J} & 0 & 0 \\ 0 & 0 & \mathbf{I} \end{bmatrix} \lambda^{[\text{AF}]},
\]

where \(\lambda^{[\text{AF}]} = [\alpha^T, (\nu^{[\text{sum}]}]^T)\). The CRLB for the estimation of \(\lambda^{[\text{AF}]}\) is given by (20)

\[
\text{CRLB} \left( \lambda^{[\text{AF}]} \right) = \text{JCRILB} \left( \lambda^{[\text{AF}]} \right) \mathbf{J}^H.
\]

Using (18) and (21) the CRLB for the estimation of channel gains is given in (22) at the bottom of this page. In (22), \(\mathbf{J} \triangleq \begin{bmatrix} \mathbf{I} & \mathbf{J} \end{bmatrix}\) and \(\Phi\) is defined in (19).
determined. On the other hand, if linearly dependent training and data
estimation can easily be achieved. According to [31], the FIM is not singular and the CRLB for both channel and CFO estimation is not
singular, indicates that an unbiased estimator does not exist that can jointly estimate $\nu_{[\text{sum}]}$. This motivates the choice of orthogonal TSs for transmission and the baseband processing structure in Fig. 2.

IV. PROPOSED CFO ESTIMATORS

In this section we propose two estimators based on multiple signal characterization (MUSIC), namely, iterative-MUSIC (I-MUSIC) and iterative correlation-based-MUSIC (I-C-MUSIC) and highlight their novelty.

A. I-MUSIC for DF Networks

For notational clarity, $\nu_{[\text{ind}]}$ is denoted by $\nu$ throughout this subsection. Let us partition the TS, $t_k^r$, of length $L$ symbols into $M$ blocks of length $N$ symbols ($M = L/N$). Under the assumptions of constant channels gains over the length of each block and narrow band transmitted signals, the temporal covariance matrix of the received signal, $y$, in (2) is given by

$$Q_y = E[y(m)y^H(m)] = \Gamma(\nu)S\Gamma^H(\nu) + \sigma_w I,$$

where

- $\nu = [\nu_1, \cdots, \nu_2]$, with $\nu_1 = y(m+1), \cdots, y(m+N)$
- $S = E[s(m)s^H(m)]$, and
- $s(m) = [s_1(m), \cdots, s_K(m)]^T$, with $k$th element given by $s_k(m) = \{g_k^T(r)\}_{r=1}^{M}$.

Let $\nu_1 \geq \nu_2, \cdots, \geq \nu_N$ denote eigenvalues of $Q_y$. If the CFO values are distinct, rank $[\Gamma(\nu)S\Gamma^H(\nu)] = R$ and it follows that $\nu_k > \sigma_w$ for $k = 1, \cdots, R$ and $\nu_k = \sigma_w$ for $k = R+1, \cdots, N$. Denote the unit-eigenvectors corresponding to $\nu_{R+1}, \cdots, \nu_N$ as $[\Psi^N]_{N \times (N-R)} \triangleq [\psi_{R+1}, \cdots, \psi_N]$, where $\Psi^N$. Using steps in [26, the MUSIC estimate of $\nu_k$, $\hat{\nu}_k$, for $k = 1, \cdots, R$, is given by

$$\hat{\nu}_k = \arg\max_{\nu_k \in [-\epsilon, \Delta \nu_k]} \left(1 - \psi^H(\nu_k)\Psi^N \Psi^N \psi^H(\nu_k)\right)^{-1},$$

where $|\epsilon, \Delta \nu_k$ represent the range and step size of the 1-dimensional maximization for the $k$th relay, respectively. In (27) the matrix multiplication $\psi^H(\nu_k)\Psi^N \Psi^N \psi^H(\nu_k)$ needs to be calculated only once, since $\Psi^N$ is not a function of $\nu_k$. The temporal covariance matrix $Q_y$ can be estimated by time averaging over $M_F$ blocks of training and data symbols

$$\hat{Q}_y = \frac{1}{M_F} \sum_{m=1}^{M_F} y(m)y^H(m),$$

where $M_F = L_F/N$ and $L_F$ is the number of symbols in a frame. Though accurate, the above MUSIC-based CFO estimator, similar to MLE, cannot distinguish among close-spaced CFO values [26, 32] and does not associate estimated CFOs to corresponding relays, which is necessary for equalization and detection at the destination. These shortcomings are addressed by utilizing the linearly independence of the TSs transmitted from each relay.

1) Initialization of I-MUSIC: Let $q$ denote the number of distinct CFOs present in $y$, where $q$ can be estimated using the algorithms in [33–35]. The following two possible scenarios are considered:

Scenario 1) $q=R$: Given that $y$ is distributed as $CN(\mu_y, \sigma_w^2 I)$, the negative log likelihood function (LLF) of the CFO vector and the channel gains is proportional to

$$\delta(\nu, g) = ||y - E_\nu g||^2,$$

where for a given $\nu$, the minimizer of (29) and the ML estimates of the channel gains, $\hat{g}$, are given by

$$\hat{g} = (E_\nu^H E_\nu)^{-1} E_\nu^H y,$$

where $E_\nu \triangleq [\psi_1, \cdots, \psi_R]^T$ and $E_\nu \triangleq E_{\nu_{\text{ind}}}$. To estimate the CFOs, the MUSIC algorithm is used, where in (27) the search is performed for $R$ maxima. Next, using (30) and the first $M-1$ blocks of the received training signal, $y^{[c]} \triangleq [y(1), \cdots, y((m-1)N)]^T$, the channel gain corresponding to each CFO is determined. Given that linearly independent TSs are transmitted from each relay node, the $M$th block of received training signals, $y^{[\text{in-c}]} \triangleq [y((m-1)N+1), \cdots, y(mN)]^T$ and the LLF in (29) are used to assign the pairs $\nu$ and $\hat{g}$ to specific relays by carrying out the minimization

$$\nu^{[A]}, \hat{g}^{[A]} = \arg\min_{\nu, \hat{g}} \delta(\nu, g),$$

where

- $y(m) \triangleq [y(m+1), \cdots, y(m+N)]^T$
where \( \hat{\nu}^{[A]} \) and \( \hat{g}^{[A]} \) denote the sets of estimated CFOs and channel gains corresponding to each relay node, respectively. Note that in this case (31) needs to be carried out \( RL \) times.

**Scenario 2) \( q \leq R \):** The set of \( q \) estimated CFOs in combination with the orthonormal TSs are used to estimate and assign the CFOs and channel gains to each path. See the algorithm in Table I.

### Table I

**Initialization Steps for I-MUSIC and I-C-MUSIC**

<table>
<thead>
<tr>
<th>Step</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td><strong>Initialization</strong>&lt;br&gt;Using the method in [33]–[35], determine ( q ). Using (27), determine the set of ( q ) distinct CFOs, ( \hat{\nu}^{[o]} ).</td>
</tr>
<tr>
<td>2</td>
<td><strong>CFO and Channel Gain Assignment</strong>&lt;br&gt;For ( o = 1, 2, \ldots, (\frac{R}{q}) ):&lt;br&gt;• Construct ( \hat{\nu}^{[o]} = \hat{\nu}^{[o]} \cup (\hat{\nu}^{[R-q]})^{[o]} ), where ( \hat{\nu}^{[R-q]} ) is a set of frequencies selected from ( \hat{\nu}^{[o]} ).&lt;br&gt;• Using (30), determine ( \hat{g}^{[o]} ) corresponding to ( \hat{\nu}^{[o]} ).&lt;br&gt;• Using (31), determine ( \hat{\nu}^{[A]} ) and ( \hat{g}^{[A]} ) that result in the smallest LLF value, ( \delta(\hat{\nu}^{[A]}), (\hat{g}^{[A]}) ) as ( \hat{\nu}^{[A]} ) and ( \hat{g}^{[A]} ), the set of estimated CFO and channel gains corresponding to each relay node, respectively.</td>
</tr>
</tbody>
</table>

**2) Iterative Step for I-MUSIC:** Since the unit amplitude PSK TSs are known, the effect of data modulation corresponding to the \( i \)th node can be eliminated according to

\[
\tilde{y}_i(n) = y(n) \left( \frac{t_i}{r}(n) \right)^* = \sum_{k=1, k \neq i}^{R} g_k e^{j2\pi n \nu^{[i]}_k (n)} \tilde{t}_i(n) + w(n) \left( \frac{t_i^r}{r}(n) \right)^* + \tilde{w}_i(n),
\]

where \( \tilde{t}_i(n) = \frac{t_i}{r} \left( \frac{t_i}{r}(n) \right)^* \) and \( \tilde{w}_i(n) = w(n) \left( \frac{t_i^r}{r}(n) \right)^* \). Note that \( \tilde{w}_i(n) \) has the same statistical properties as \( w(n) \), since multiplication by \( \left( \frac{t_i}{r}(n) \right)^* \) only results in a phase shift of the noise.

The initial estimates of \( \nu^{[i]} \) and \( g \), \( \left( \hat{\nu}^{[i]} \right)^{[1]} \) and \( \left( \hat{g}^{[i]} \right)^{[1]} \), respectively, are used to reduce the interference term in (32) according to

\[
f_i(n) = \tilde{y}_i(n) - \sum_{k=1, k \neq i}^{R} \hat{g}_k e^{j2\pi n \nu^{[i]}_k (n)} \tilde{t}_i(n), \quad (33)
\]

where \( f_i = \{ f_i(1), \ldots, f_i(L) \} \) is applied in the next iteration to estimate the CFO corresponding to the \( i \)th node using (27). This approach also transforms the joint CFO estimation problem into multiple single-parameter estimation problems. In addition, for closely-spaced CFO values the MLE in (30) does not perform well since the term \( E_y H E_{\nu} \) in (30) becomes nearly singular. To address this shortcoming, at each iteration the \( i \)th relay’s channel gain is estimated via

\[
\hat{g}_i = \frac{1}{L} \sum_{n=1}^{L} \frac{f_i(n)}{e^{j2\pi n \nu^{[i]}_k (n)}}, \quad (34)
\]

which is based on the expectation conditional maximization (ECM) algorithm [36]. The iteration stops when the absolute difference between the LLF of two iterations is smaller than a threshold value \( \chi \)

\[
||y - E_{\nu^{[i]}}(\hat{g}^{[i]}_k)||^2 - ||y - E_{\nu^{[i]}}(\hat{g}^{[i]}_k)||^2 \leq \chi, \quad (35)
\]

where \( (\hat{\nu}^{[i]}) \) and \( \hat{g}^{[i]} \) denote CFO and channel gain estimates corresponding to the \( i \)th iteration.

### B. I-C-MUSIC for DF Networks

By transforming the problem from \( R \)-dimensional to one-dimensional estimation, a variety of CFO estimation methods suitable for different scenarios may be applied to improve upon the proposed algorithm [6], [37]. Here we apply the estimator in [37], which consists of estimating the \( i \)th node’s CFO as

\[
2\pi \nu^{[i]}_k = \sum_{n=1}^{L-1} \omega(n) \text{angle} \left\{ f_i(n), f_i(n+1) \right\}, \quad (36)
\]

where \( \omega(n) \) is a window designed to reduce the estimator’s variance (see [37] for details). Similar steps as outlined in Section IV A may be used to determine the CFO values, where (36) is used instead of (27) in the iterative step (see [26] for details).

### C. CFO Estimation in AF Networks

To apply the MUSIC algorithm for CFO estimation: 1) the length of each block, \( N \), needs to be larger than the number of relays, 2) the additive noise needs to be zero-mean, and 3) the additive noise needs to be white [23]. By simply choosing \( N \) to be larger than \( R \) the first condition can be satisfied. According to the signal model in Eq. (3) and based on the assumption of zero-mean AWGN at the relays, the mean of the additive noise at the destination can be shown to be

\[
E \left[ \sum_{k=1}^{R} \beta_k e^{j2\pi n \nu^{[i]}_k} t^n_k \nu_k(n) \right] + E[w(n)] = 0, \quad (37)
\]

which satisfies the second condition. Finally, in (8), it is shown that the overall noise at the destination is white, satisfying the third condition. Thus, the proposed I-MUSIC and I-C-MUSIC algorithms can also be applied to AF relaying cooperative networks.
D. Complexity of I-MUSIC and I-C-MUSIC

Throughout this section it is assumed that the step size in (27) for all relays are the same, i.e., \( \Delta \nu = \Delta \nu_1 = \cdots = \Delta \nu_R \), and computational complexity is defined as the number of additions and multiplications. Accordingly, the computational complexity of the initialization step for I-MUSIC and I-C-MUSIC, denoted by \( C_I \), is calculated as shown in (38) at the bottom of this page.

In (38), \( \vartheta = \frac{2^R}{N} \), where \( \epsilon \) is defined in (27).

Using (38), the computational complexity of I-MUSIC and I-C-MUSIC can be determined as

\[
C_{\text{I-MUSIC}} = C_I + \kappa R \left[ N^2 (N - R) + \vartheta (2N^2 + 1) \right] + 2MN + 1, \quad \text{and} \quad \kappa = \frac{1}{\vartheta} \quad \text{(39)}
\]

\[
C_{\text{I-C-MUSIC}} = C_I + \kappa R \left[ 2MN - 2 + 2MN + 1 \right], \quad \kappa = \frac{1}{\vartheta} \quad \text{(40)}
\]

where \( \kappa \) represents the number of iterations. (39) and (40) demonstrate that the computational complexity of I-MUSIC is considerably higher than that of I-C-MUSIC for the same \( \kappa \). A numerical comparison of number of iterations versus performance is provided in Section V.

The computational complexity of the MLE based on [10, Eq.(22)] and implemented using the iterative alternating projection method [38] is calculated as

\[
C_{\text{MLE}} = \kappa_{\text{MLE}} R \theta \left[ R^3 + 2R^2 L + (R + 1)L^2 + L \right] + R^3 + 2R^2 L + RL^2, \quad \text{(41)}
\]

where \( \kappa_{\text{MLE}} \) represents the number of iterations required by the alternating projection method, which is between 3-4 [38]. Table II represents a quantitative comparison between the computational complexity of I-MUSIC, I-C-MUSIC, and MLE in [10]. As shown in Table II, compared to MLE in [10], I-MUSIC and I-C-MUSIC are on average 30 and 1800 times less computationally intensive, respectively. In addition, the algorithm in [13] requires correlating the received signal with each TS, which can be computationally intensive and due to its poor performance when the CFOs are far apart may not be applicable to the case of cooperative networks. Therefore, a quantitative comparison between the computational complexity of the algorithm in [13] and I-MUSIC and I-C-MUSIC is beyond the scope of this paper.

V. Numerical Results and Discussions

Throughout this section the propagation loss is modeled as [6], \( \beta = (d/d_0)^{-m} \), where \( d \) is the distance between the transmitter and receiver, \( d_0 \) is the reference distance, and \( m \) is the path loss exponent. The following results are based on \( d_0 = 1 \text{ km} \) and \( m = 2.7 \), which corresponds to urban area cellular networks. \( \epsilon = 0.5 \) in (27). Without loss of generality, only CFO estimation performance for the first node is presented. The estimators’ performances are investigated for both far-apart and closely-spaced CFO values.

1) DF cooperative networks: Fig. 4 compares the performance of I-MUSIC and I-C-MUSIC for the estimation of \( \nu^{[\text{rd}]} \) in DF relaying networks against the CRLB in Eq. (24), the MLE in [10], and the estimator in [13]. In (35), the threshold is set to \( \chi = 0.001 \), which corresponds to approximately 6–20 iterations. Similar to [10] and [13], the channel gains, \( h \) are drawn from independent and identically distributed (i.i.d) zero-mean complex Gaussian processes with unit variance. For our particular channels \( h = [0.2790 - 0.9603i, 0.8837 + 0.4681i]^T \). Two sets of CFO values are selected, \( \nu^{[\text{rd}]} = \{0.1, 0.2\} \) and \( \nu^{[\text{rd}]} = \{0.2, 0.205\} \), which in Fig. 4 are represented by solid lines and dotted lines, respectively.

For the case of \( \nu^{[\text{ld}]} = \{0.1, 0.2\} \), simulation results reveal that I-MUSIC is close to but does not reach the CRLB. This is due to the inherent shortcoming of the MUSIC algorithm [32]. However, I-C-MUSIC reaches the CRLB at mid-to-high SNR but exhibits poorer performance at low SNR. Fig. 4 also shows that both algorithms outperform the MLE and the estimator in [13] at mid-to-high SNR. The MLE, on the other hand, requires that only one node transmits its training sequence at a time. Therefore, for a fair comparison, in the case of MLE a training sequence length of \( L/R \) is used, resulting in higher mean-square error (MSE). As expected, the estimator in [13] fails since the initial CFO estimates are extremely poor whenever the CFOs are larger than 0.05 (the results in [13] are based on normalized CFO values.

\[
C_I = \begin{cases} 
N^2 (N - R) + \vartheta (2N^2 + 1) + M_F N^2 + 1 + R! (R + 2)N + R^3 + R^2 MN + M^2 N^2 & q = R \\
N^2 (N - R) + \vartheta (2N^2 + 1) + M_F N^2 + 1 + (R^q) [(R + 2)N + R^3 + R^2 MN + M^2 N^2] & q < R 
\end{cases} \quad \text{(38)}
\]
of 0.01 and 0.015). For the case of closely-spaced CFO values ($\nu^{\text{rd}} = \{0.2, 0.205\}$), Fig. 4 illustrates that I-MUSIC and I-C-MUSIC approach the CRLB but do not reach it.

In the case of AF relaying, I-C-MUSIC reaches the CRLB while I-MUSIC is very close to the CRLB and demonstrates better performance at low SNR values. Also, for the case of closely-spaced CFO values, the performance gap between I-MUSIC and I-C-MUSIC and the CRLB is larger for the case of AF compared to that of DF. This can be explained by the fact that the noise introduced by the relay nodes, which is amplified and forwarded to the destination, cannot be removed by the iterative algorithm.

In the case of AF relaying, I-C-MUSIC reaches the CRLB while I-MUSIC is very close to the CRLB and demonstrates better performance at low SNR values. Also, for the case of closely-spaced CFO values, the performance gap between I-MUSIC and I-C-MUSIC and the CRLB is larger for the case of AF compared to that of DF. This can be explained by the fact that the noise introduced by the relay nodes, which is amplified and forwarded to the destination, cannot be removed by the iterative algorithm.

Fig. 5 compares the number of iterations for I-MUSIC, I-C-MUSIC, and the estimator in [13]. Note that both I-MUSIC and I-C-MUSIC algorithms require very few iterations to reach or approach the CRLB. As illustrated in Fig. 5 as the CFO values get close, I-MUSIC and I-C-MUSIC both require more iterations to approach the CRLB, due to the rough initial estimates. However, even for closely-spaced CFO values, both algorithms require considerably fewer iterations and overhead compared to [13] at all SNR values.

In the case of AF relaying, I-C-MUSIC reaches the CRLB while I-MUSIC is very close to the CRLB and demonstrates better performance at low SNR values. Also, for the case of closely-spaced CFO values, the performance gap between I-MUSIC and I-C-MUSIC and the CRLB is larger for the case of AF compared to that of DF. This can be explained by the fact that the noise introduced by the relay nodes, which is amplified and forwarded to the destination, cannot be removed by the iterative algorithm.

Fig. 7 compares the number of iterations for I-MUSIC and I-C-MUSIC for AF cooperative networks, where it is illustrated that both algorithms require fewer iterations to reach the CRLB when the CFOs are not very close. I-C-MUSIC requires fewer iterations to reach or approach the CRLB at low-to-mid SNR compared to I-MUSIC, while this advantage is reversed as the SNR increases. In Fig. 7, when the CFO values are close to one another (dashed + marked and • marked plots) at low SNR, the average number of iterations required by I-MUSIC and I-C-MUSIC is small, since the initial CFO and channel estimates are quite poor and further iterations do not result in better estimates. However, at high-SNR due to the shortcoming of the MUSIC algorithm in distinguishing between closely-spaced CFO values, the MSE of the initial CFO and channel estimates moves further away from the CRLB as the SNR increases and more iterations are required to reach the CRLB. Finally, in the case of AF, both algorithms require considerably more iterations to approach the CRLB for closely-spaced CFO values compared to the case of DF. These results demonstrate that in addition to requiring higher SNRs between the nodes, AF networks also require more time and overhead to achieve frequency synchronization.

Fig. 8 plots the MSE for the estimation of the overall channel gains from source-relay-destination links, $\alpha$, for both I-MUSIC
and I-C-MUSIC in the case of AF relaying cooperative networks versus the CRLB in (22). At mid-to-high SNR, both estimators reach the CRLB for channel estimation. Since similar results are obtained for the estimation of channel gains from relay-destination links, $g$, in the case of DF relaying, they are not presented here.

B. Cooperative Network Performance

During the data transmission interval BPSK modulation is used with a frame length, $L_F$, of 512 symbols and a synchronization overhead of 12%. In the case of DF relaying an orthogonal space-time block code (OSTBC) with a code rate of $\frac{3}{4}$, $[39]$, is used for the transmission of the signals from $R = 4$ relays. In the case of AF relaying, since application of OSTBC is not straightforward $[40]$, the algorithm in $[4]$ is used to investigate the performance of the cooperative networks. Quasi-static fading channels are considered, where new channel gains are generated from frame to frame (channel coefficients are complex Gaussian random variables with mean zero and unit variance). For DF relaying it is assumed that only relays that correctly decode the received signal are selected for retransmitting the signal. Finally, relays are uniformly distributed throughout the network such that $d^{[r]} \leq 1$ km and $d^{[d]} = (1 - d^{[r]})$ km.

For the DF relaying scenario, the time varying channel matrix $G_{L_F \times R} \triangleq \begin{bmatrix} \alpha_1 e_1^{[r]} & \cdots & \alpha_2 e_2^{[r]} \end{bmatrix}$, where $e^{[r]} \triangleq [e^{j2\pi \nu^{[r]}_1}, \ldots, e^{j2\pi \nu^{[r]}_{L_F}}]^T$ in combination with the decoder in $[39]$ may be used to mitigate CFOs for decoding the received signal at the destination. In this paper, the computationally simpler method in $[27]$ as referenced in Section V.B is used instead. Unfortunately, lack of space precludes providing the details of the CFO compensation method, which is available in $[27]$ and references therein. On the other hand, for AF relaying to mitigate the effect of CFOs the time varying channel matrix $F_{L_F \times R} \triangleq \begin{bmatrix} \alpha_1 e^{[r]}_{\text{sum}} & \cdots & \alpha_2 e^{[r]}_{\text{sum}} \end{bmatrix}$ where $e^{[r]}_{\text{sum}} \triangleq [e^{j2\pi \nu^{[r]}_1}, \ldots, e^{j2\pi \nu^{[r]}_{L_F}}]^T$ in combination with successive interference cancelation (SIC) as described in $[4]$ is used.

Figs. 9 and 10 illustrate the average-bit-error-rate (ABER) of DF and AF relaying SISO multi-relay cooperative networks, respectively. Here, I-MUSIC is used to acquire the completely unknown CFOs and channel gains. This result is compared to an unsynchronized system with normalized CFOs uniformly distributed in the range $[-0.5, 0.5]$ per node for $R = 4$ relays, $L_F = 512$. Figs. 9 and 10 also demonstrate that compared to DF, the performance of AF relaying networks is more significantly
imparted by CFOs. This outcome is anticipated, since CFO estimation in the case of DF relaying can be performed more accurately as predicted by the CRLB analysis in Fig. 3. Unlike DF relaying, the ABER of an AF relaying network synchronized via I-MUSIC does not reach that of a perfectly synchronized system at high SNR due to this difference in estimation performance.

Fig. 10. ABER plots for perfectly synchronized, estimated/imperfectly synchronized via I-MUSIC, and unsynchronized systems with normalized CFO in the range \([-0.5, 0.5]\) per node for \(R = 4\) relays, \(L_F = 612\).

VI. CONCLUSION

In this paper we have addressed the topic of CFO estimation in multi-relay cooperative networks. The system model for DF and AF relaying networks in the presence of multiple CFOs has been presented and new CRLB expressions are derived, in closed-form. Two novel multiple CFO estimators are outlined. Numerical analyses demonstrate that the proposed estimators’ performances reach or approach the CRLB at mid-to-high SNR and outperform the existing algorithms. The performances of DF and AF relaying cooperative networks in the presence of multiple CFOs has been investigated showing that the application of the proposed estimators result in significant performance gains. In addition, the results in Section V reveal that up to an SNR of 12 and 15dB for DF and AF relaying, respectively, there is a large performance gap between the ABER of idealized cooperative systems that assume perfect frequency synchronization and actual cooperative systems that require the CFOs to be estimated and compensated for at the receiver. Thus, it is important to consider the effect of imperfect CFO estimation when assessing the performance of cooperation methods, e.g., distributed beamforming and distributed space-time coding.

REFERENCES


Hani Mehrpouyan received his B.Sc. honours degree in Computer Engineering from Simon Fraser University, Canada in 2004. From 2005-2010 he was a Ph.D. candidate at the Department of ECE at Queens University, Canada. He has received more than 10 scholarships and awards due to leadership, academic, research, and teaching excellence. Some of these awards are, IEEE Globecom Early Bird Student Award, NSERC PGS-D, NSERC CGS-M Alexander Graham Bell, B.C. Wireless Innovation, and more. Hani has also been involved with industry leaders such as Ericsson AB, Qamcom AB, and Research in Motion (RIM). Since September of 2010 he has been working as a Post-Doctoral Researcher in the Department of Signals and Systems at Chalmers University of Technology in Sweden. His current research interests lie in the area of signal processing and wireless communications, including synchronization, channel estimation, and performance optimization for cooperative networks.

Steven D. Blostein (SM ’83, M ’88, SM ’96) received his B.S. degree in Electrical Engineering from Cornell University, Ithaca, NY, in 1983, and the M.S. and Ph.D. degrees in Electrical and Computer Engineering from the University of Illinois, Urbana-Champaign, in 1985 and 1988, respectively. He has been on the faculty in the Department of Electrical and Computer Engineering Queen’s University since 1988 and currently holds the position of Professor. From 2004-2009 he was Department Head. From 1999-2003, he was the leader of the Multi-Rate Wireless Data Access Major Project sponsored by the Canadian Institute for Telecommunications Research. He has also been a consultant to industry and government in the areas of image compression, target tracking, radar imaging and wireless communications. He spent sabbatical leaves at Lockheed Martin Electronic Systems and at Communications Research Centre in Ottawa. His current interests lie in the application of signal processing to problems in wireless communications systems, including synchronization, network MIMO and physical layer optimization for multimedia transmission. He has been a member of the Samsung 4G Wireless Forum as well as an invited distinguished speaker. He served as Chair of IEEE Kingston Section (1994), Chair of the Biennial Symposium on Communications (2000,2006,2008), Associate Editor for IEEE Transactions on Image Processing (1996-2000), and Publications Chair for IEEE ICASSP 2004. For a number of years has been serving on Technical Program Committees for IEEE Communications Society conferences that include ICC, Globecom and WCNC. He has also been serving as an Editor of IEEE Transactions on Wireless Communications since 2007. He is a registered Professional Engineer in Ontario and a Senior Member of IEEE.