SIMULTANEOUS MEASUREMENTS OF DROP SIZE AND VELOCITY IN LARGE-SCALE SPRINKLER FLOWS USING LASER-INDUCED FLUORESCENCE AND MIE SCATTERING

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This paper reports an experimental technique that is developed for instantaneous planar measurements of drop size and velocity for dilute sprays in general and sprinkler sprays in particular. This particle tracking technique relies on photographic measurements of fluorescence and Mie scattering from water drops to determine their size and velocity. Measurements were made in a plane that passes through the vertical axis of symmetry of a specially designed axis-symmetric sprinkler. Drop sizes down to 0.2 mm, within the 250 mm \times 350 mm viewing area, were measured from the digitized photographs. Drop velocities were determined from the same double-exposed photographs and the directional ambiguity was resolved by color differentiation of fluorescence vs. scattering. Dye selection and its concentration were determined by testing the fluorescence output of water tracer dyes. Collection optics and laser power was varied to optimize the color differentiation and maximize the resolution for drop size measurements.

INTRODUCTION

Water spray sprinklers are the most commonly used automatic fire protection systems in buildings ranging from small offices to large warehouses. For effective fire suppression, the sprinkler water must reach the burning surface. An optimum sprinkler system, for a given application, is one that provides the maximum fraction of water delivered by the sprinkler (or sprinklers in a large warehouse) to the burning surfaces and suppresses the fire in the shortest time after its initiation. The design of such a sprinkler system depends on the geometrical relationship between the sprinkler(s) and the fire source and its heat release rate, the geometry of the room and its ventilation conditions and the sprinkler spray characteristics. Given the complexity of the problem, the optimization, as well as the evaluation, of various sprinkler systems is most cost-effectively accomplished via computer models that can calculate the fire and sprinkler-induced flows for different geometries. Such models have been developed at BFRL (NIST) by McGrattan et al. (see [1] and references therein). For experimental validation of these models, instantaneous field measurements are needed for the drop-size distribution, drop velocity, sprinkler-induced flows, and the actual

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delivered density. This paper develops a technique to provide instantaneous and simultaneous measurements of drop-size distribution and drop velocities in a large plane (250 mm \times 350 mm) illuminated by a laser sheet. High-resolution laser-induced fluorescence and Mie scattering images of drops are recorded on color photographs are analyzed.

A number of standard techniques and instruments are available for measuring drop-size distributions in sprays such as Phase-Doppler Anemometer (PDA) [2] and Particle Measuring System (PMS) [3]. These techniques are suitable for measuring a single point or an array of points, but do not provide the instantaneous spatial drop distribution in the spray. Consequently, a large number of measurements must be taken at a point to determine the drop-size distributions and the spray must be considered time invariant. To overcome this difficulty, an axis-symmetric sprinkler was designed and instantaneous planar measurements were made along the vertical axis of the sprinkler spray. Different techniques of simultaneous planar measurement of drop size and velocity have recently appeared in the literature. Kadambi et al. [4] have identified the errors associated with particle size measurements from Particle Image Velocimetry (PIV) images. Herpfer and Jeng [5] have introduced streak PIV for planar measurements of drop sizes and velocities. Cao et al. [6] and Everest and Atreya [7] have used planar laser-induced fluorescence for measurements of drop size and Particle Tracking Velocimetry (PTV) for measuring drop velocities. In this paper, we present a Particle Tracking Velocimetry and Imaging (PTVI) technique, similar to that given in [6, 7], which relies on taking instantaneous double-exposed color photographs of the spray and using them to obtain both velocities and particle sizes. Since the double-exposed photographs are created by laser shots of two different wavelengths, the color differentiation helps in resolving the flow direction.

EXPERIMENTAL TECHNIQUE

Drop Sizing Considerations

Sizing and tracking a particle in a large field of view (FOV) requires simultaneously satisfying disparate requirements of low magnification and high spatial resolution. For proper sizing, the spatial resolution of the optical, film and digital components must result in a fully resolvable drop, indicating as large a magnification as possible. Meeting the spatial requirements for drop sizing results in limiting the FOV and a subsequent loss in the dynamic velocity resolution and the dynamic spatial resolution, as defined by Adrian [8]. Greater than optimal magnification required to meet the sizing requirements reduces the spatial and velocity spectra over which the velocity measurements can be made.

Kadambi et al. [4] identified the effects that must be considered in properly resolving the drop size. In their experiments, scattering from solid particles suspended in a liquid was measured. They identified effects of spatial resolution, light-sheet intensity distribution, and depth of field (DOF) on particle size measurements. It was observed that the particle image should be greater than 3 pixels in diameter to accurately determine its size. In quantifying the light-sheet intensity distribution effect and the DOF effect, they used a 200- μ m particle, a DOF of 200 μ m, and a beamsheet thickness of 1600 µm. By moving the focused particle through the light sheet, they observed a decrease in the measured diameter of approximately 9% and a roughly 50% decrease in scattered light intensity at the edges of the light sheet relative to the center. In another experiment, they traversed the imaging camera while holding the particle and laser sheet fixed to determine the effect of DOF. It was observed that the particle diameter increased by approximately 9%, while the intensity level again decreased by roughly 50%. Thus, when a particle is not centered in the light sheet and the focal plane, DOF and beam-sheet intensity effects approximately cancel each other out resulting in a constant particle diameter. Their reported particle diameters had a standard deviation of 7%.

While Kadambi et al. [4] and Adrian's [8, 9] results were very helpful, scattering measurements did not yield a reliable drop size in the present work perhaps due to a greater disparity in the index of refraction between air and water. Thus, planar fluorescence imaging along with scattering was used to make drop size and velocity measurements in a large FOV with low-density sprinkler spray. The fluorescence emission signal F for drops is given by the equation:

$$F \sim \phi I_0 \vee V (m/(m+1)/f\#)^2 f(c) f(R).$$
 (1)

Here, F is proportional to the fluorescence yield ϕ , incident intensity of light on the drop I_0 , frequency of emitted light v, and the volume of the illuminated drop V. F is nonlinearly related to the magnification m, f-number (f#), the dye concentration c, and the film response function R. The scattering signal for large water drops in a low-density spray is given by:

$$S \sim I_0 \vee A (m/(m+1)/f\#)^2 \phi(\tau) f(R).$$
 (2)

The signal S is linearly related to I_0 - the incident intensity, v- the frequency of scattered light, and A- the area of the illuminated drop. It is nonlinearly related to the magnification m, f-number, the angle of incidence of a light ray on the drop τ , and the film response function R. For both cases, the signal quality is improved by using higher magnifications and smaller f-numbers. However, to meet the FOV requirements the magnification is fixed at 0.1, and only f-number can be reduced.

The response function R of the film is dependent on the spectral and exposure response characteristics of the film emulsions. Characteristic sensitivity curves for Kodak Pro film were used to define the film spectral response function. These curves indicate that the film is 30 times more sensitive for 588-nm (fluorescence) and 532-nm (scattering) than for 355-nm UV scattered light. The increased energy in the shorter UV wavelength improves the signal but lower 355-nm laser power offsets that gain. As a result, 355-nm scattering was observed only in a few images.

Tests were conducted to identify the effect of fluorescent dye concentration, resolution of the imaging system, effect of variation in laser sheet intensity and effect of laser sheet power. The results of these tests are used to quantify the ability of the measuring system to accurately characterize the spray velocities and particle size while maximizing FOV.

Experimental Setup

Figure 1 schematically shows the experimental layout for the drop velocity and size distribution measurements.

Water exits through an 8-mm diameter nozzle at 5 gallons/min and impinges on a conical strike plate creating the sprinkler spray. A fluorescent tracer dye is injected into the water far upstream of the nozzle. A dual-pulse Nd:YAG laser pro-



Fig. 1 Experimental arrangement for spray measurements.

vides two laser beams that are formed into light sheets by a single f6.35-mm diverging cylindrical lens. The leading beam sheet, formed by the third harmonic (355 nm) occurs 1 millisecond prior to the lagging beam sheet, which results from the second harmonic (532 nm) of the second Nd:YAG laser. Fluorescence and Mie scattered light from the two laser pulses is captured by a 35-mm color film camera using a 50-mm f1.2 lens with 800 ASA Fujicolor film. Since the framing rate of the film camera is too low to obtain images on separate frames, the photographs were double exposed. Time discrimination was obtained by the fluorescent dye that created different color drop images for the two laser pulses firing at two different wavelengths. To control the scattering signal at 532 nm, Quantaray R2 red filter or Schotts OG530 was used to allow only the fluorescence signal and some portion of the scattered signal to reach the film. Images of water drops in a region 250 mm \times 350 mm and 300 mm downstream of the strike plate were taken at a magnification of 0.1 to characterize the drop size and velocity. The negatives were digitized with a 4000-dpi Polaroid film scanner that resulted in a digital resolution of 71 µm in the drop plane/pixel (based on scattering from two fibers at a known distance apart). The optical spatial resolution of the imaging system was also measured by using a standard USAF resolution chart. Images were obtained at a magnification of 0.1 for various f-numbers. The best resolution obtained was for an f-number of 2.8 at 3.17 lp/mm, i.e., a 158-µm-thick line could be resolved in the drop plane. This corresponds to roughly 2 pixels in the image. Assuming that 3×3 pixels are needed to measure the drop size with reasonable accuracy, we obtain the minimum measurable drop diameter of about 0.2 mm.

The digitized images were processed using the TSI Insight and SCION Image software for determining the drop velocities and drop size, respectively. These images had sufficient spatial resolution for sizing 0.2-mm-diameter drops, as well as, color differentiation for resolving the directional ambiguity in velocity measurements. For a laser pulse separation of 1 ms, velocities in the range of 0.2 m/s (for small drops) to 10 m/s (for large drops) could be measured.

Determination of Fluorescent Dye Concentrations

Proper choice of the fluorescent dye and its concentration must be made to obtain the best signal. Two types of water tracing dyes with high fluorescence yield, red rhodamine WT and yellow/green fluorescein, can be injected into the water stream 1.5 m upstream of the nozzle exit (to ensure mixing) as shown in Fig. 1. Different concentrations of these dyes were tested by passing a beam through a long glass tube filled with the mixture. The emissions were imaged onto videotape by a Cohu CCD array camera with an f2.8 lens and Schott OG550, and analyzed using a Data Translation frame-grabber board and Image-Pro software. The relative emission



Fig. 2 Relative fluorescence emissions from the tracer dyes for 532-nm and 355-nm excitation.

curves of the rhodamine and fluorescent dyes are given in Fig. 2. Emissions from the excitation due to the UV, 355-nm, laser and the visible, 532-nm, laser are indicated. The laser power was intentionally low at 5 mJ/shot to simulate the laser fluence that exists in the experiment.

A number of striking observations can be made from Fig. 2. At low concentrations, the rhodamine dye is much better at fluorescing than the fluorescein dye for both excitation wavelengths. The 355-nm excitation is more effective than excitation at 532 nm for low fluorescein dye concentrations. The rhodamine dye reaches a maximum fluorescence signal at approximately 0.005 g/l, and this maximum is reached earlier at 532 nm. The fluorescein dye reaches a maximum near a concentration of 0.05 g/l, and again the stronger excitation wavelength, 355 nm, reaches the maximum first. Absorption was also qualitatively measured and observations indicated that the rhodamine dye is the more effective dye for absorbing both excitation wavelengths. 532-nm excitation was more effectively absorbed than 355-nm excitation. Beyond 0.1 g/l, both dyes have a high absorption that reduces the emissions. In a different set of dye concentration experiments, the Schotts OG530 filter replaced the OG550 filter in front of the CCD camera, allowing some 532-nm scattering to be imaged. 532-nm scattering from air bubbles in the water column was observed to have a signal that is equal to 75% of the net fluorescence signal at a concentration of 0.0066 g/l. Since the scattering of a water drop in air is expected to be 10 times greater than an air bubble in water, clearly the scattering will be dominant in the sprinkler flow when the fluorescein dye is used. When the rho-damine dye is used, test results indicate that scattering and fluorescence will be of the same order of magnitude with the OG530 filter.

For imaging drops, the rhodamine dye was used at a concentration of 3.3 mg/l. If used at higher concentrations, Fig. 2 indicates that the signal would not increase due to absorption of the laser beam. If used at lower concentrations, the UV fluores-cence signal becomes too weak. As shown below, scattering appears to dominate the drop signal except when it is fully in the laser sheet, where the scattering vs. fluorescence signal depends on the scattering angle.

Identification of Minimum Signal Levels

The effect of varying f-number (f#) of the photographic system was investigated by imaging a 2.8 mm \pm 5%-diameter drop that was centered in the 355-nm laser light sheet and centered in the depth of field of the camera. A long-pass 550nm filter was used to collect fluorescence at 588 nm that results from 355-nm excitation. Images were taken at a magnification (m) of 0.09 for f#s of 1.2, 2.8, 4.0, and 5.6. The laser intensity was 2.2 times higher than in the spray experiments. As discussed below, the 355-nm beam sheet FWHM was 3.5 mm. The depth of field (δz), calculated according to [9]: $\delta z = 4(1 + m^{-1})2 f \#^2 \lambda$, shows that at f# of 1.2, the depth of field is only 0.5 mm — much less than the drop size. The depth of field becomes 3 mm for f# greater than 2.8. This indicates that at low f#s some intensity is lost. The measured drop diameters were 2.7 mm \pm 10%.

The change in the relative maximum intensity with f# is shown in Fig. 3 for f#s of 1.2, 2.8, 4.0, and 5.6. From Eq. (1) the signal is proportional to volume/f#². Thus, the intensity is plotted against 1/f#², which should result in a linearly increasing function, but it is clearly not linear across the entire range. The two highest f#s were used to define a line through the origin (background intensity level of 34 has been subtracted). This line defines the expected intensity level for the 2.8-mm drop. At f# of 1.2, the intensity is significantly lower than the expected signal level, but is still larger than others.

For imaging, the volume is proportional to $\delta z \times (drop \ diameter)^2$. Thus, for the same drop, volume can be replaced with the minimum of the drop diameter or δz . Since, δz is also proportional to $f^{\#^2}$, it would appear that for drops larger than



Fig. 3 Fluorescence response from a 2.8-mm drop at 355 nm excitation. Line indicates the expected signal when intensity varies inversely with f#2. Low f#s fall below the expected intensity due to depth of field effects.

the depth of field, the intensity should not depend on $f^{\#}$. However, there is some increase as indicated in Fig. 3 by the dotted line; the reason is that the portion out of the depth of field still makes some contribution to the signal.

The minimum discernable diameter due to the intensity of the fluorescence can be identified from the graph. From the drop images it was determined that the noise in the background signal level is 10% of 34, indicating that intensity levels below 7 will have a signal-to-noise ratio (SNR) less than 2. For f# of 2.8, particles with a diameter less than 104 µm will give a fluorescence signal below the desired SNR of two. Similarly for f# of 4, 213 µm defines the lower limit for detectability. In both cases, the limiting fluorescence diameter is greater than the pixel dimension as required. Equation (1) can be used to estimate the lower identifiable limits in the spray experiments where the beam sheet intensity was 2.2 times less and the magnification was 0.1. The lower limit under those conditions for f# of 2.8 is 189 µm and 387 µm for f# of 4.

The f-number experiment was repeated for scattering of the 532-nm beam. The experimental parameters were the same as above except fluorescence and scattering from the drop was measured. The drop size was estimated as 3.3 mm \pm 13%, slightly larger than the expected 2.8-mm diameter. Scattering was observed from a small portion of the drop on the side on which the laser beam was incident. The size of this region changed with $f^{\#}$, but the maximum scattering intensity was insensitive to the increase in $f^{\#}$, due to saturation of the film.

To determine if 355-nm excitation and 532-nm excitation would result in the same drop size, a series of images were taken with long-pass filters used to cutoff the short wavelengths. With no filter or the 532-nm filter, the scattering from 532nm light exists. 550 nm adequately blocks the scattering and indicates a round drop (eccentricity = 1.04), 3.0 mm \pm 10% in diameter for 532-nm excitation and a slightly smaller drop (eccentricity = 1.05), 2.7 mm \pm 10% in diameter for 355-nm excitation. The maximum fluorescence intensity for 355-nm excitation is the same for all filters, indicating that the filters do not impede any of the fluorescent signals. The maximum fluorescent signal for 532-nm excitation is 16% larger than the corresponding 355-nm excited drop. The scattering from the drops at 532-nm excitation is very useful in identifying the location of drops, but not so in identifying the size.

Effect of Beam-Sheet Intensity and Drop-Size Variation

The laser-beam incident intensity, drop volume illuminated, and incidence angle of light ray on the drop are important for determining the amount of signal collected from the drop. The incident intensity is a function of the location of the drop in the light sheet, both vertically and in the depth of the sheet. The beam-sheet thickness for 355-nm excitation and various powers of 532-nm excitation are shown in Fig. 4, normalized by the full width at half maximum of 4.4 mm for the 532-nm beam at 220 mJ/pulse. For high laser power, the visible excitation beam-sheet thick-



Fig. 4 Relative sheet thicknesses for the 355-nm laser beam at high laser fluence and 3 different laser fluences of the 532-nm beam.



Fig. 5 The 2.8-mm drop begins behind the laser sheet and is moved forward in 1mm increments. The 532-nm laser sheet has a FWHM of 4.4 mm and 355-nm laser sheet has a FWHM of 82% of that. Laser power for 532 nm is 220 mJ/pulse and for 355-nm excitation is 130 mJ/pulse. Fluorescence at 588 nm from 355-nm excitation is observed from the upper drop in each frame, while scattering and fluorescence is observed from the lower drop. No filters were used to take these images. When the drop is centered in the beam sheets, the drop size as measured by fluorescence from 355-nm excitation is 2.7 mm, while the drop size as measured from 355nm excitation and scattering is 3.3 nm. When centered in the 355-nm laser sheet, some scattering from 355 nm was detected by the film.

ness is larger than the 355-nm sheet. Thus, visible scattering is seen more often than fluorescence.

The result of the wider 532-nm beam sheet is indicated in Fig. 5 where a 2.8mm drop is traversed in 1-mm increments from behind through the light sheets. These drops were ejected from a 22-gauge hypodermic needle at a rate of 6 drops/s and images were taken 4 ms apart with a resolution of 71 (m/pixel at a downstream location of 120 mm \pm 48 mm. The drops are accelerated by gravity and the highest velocity is around 1.8 m/s.

Fluorescence at 588 nm from 355-nm excitation is observed in the upper drop in each frame, while scattering and fluorescence from 532-nm beam is observed in the lower drop. Filters were not used to take these images. The scattering of the 532-nm laser beam by the forward edge of the drop is the first and last signals observed in the sequence. The largest source of this light is reflected light although signals from the rear and top of the drop indicate the effect of internal reflection. Fluorescence from 532 nm appears before the fluorescence from 355 nm due to both a wider beam and the increased response of the dye to 532-nm excitation. The 532nm drop measurement indicated elongated drops with an average eccentricity of 1.14, while the 355-nm measurements were more round with an eccentricity of 1.07.

An important aspect of defining the beam sheet thickness is the size of the particle that is to be measured. If the sheet is very thin relative to the particle, the probability of measuring the true diameter is small. The measured mean drop diameter is related to the beam-sheet thickness by the following formula:

$$D_{\rm m} = ((2/3)^{1/2} D_{\rm a}^2 + D_{\rm a} b) / (D_{\rm a} + b)$$
(3)

where $D_{\rm m}$ is the measured mean drop diameter, $D_{\rm a}$ is the actual drop diameter, and b is the beam sheet thickness. If the beam sheet is infinitesimal, the measured diameter is 81.6% of the actual diameter. This means that if all the drops were uniformly of the same diameter, the images would show a variety of sizes with a mean diameter that is 81.6% of the actual diameter. If the beam sheet is equal to the drop diameter, the measured particle will be 90.8% of the actual particle, while if 10 times the diameter of the drop, the measured drop will be 98.3% of the true diameter. When a variety of drop sizes are to be measured instantaneously, it is important that the measured diameter be as nearly equal to the true diameter as possible. This would indicate that a wider beam sheet is better than a thin one. In the spray experiments, the 532-nm beam-sheet thickness was maintained at the FWHM of 4.4 mm.

Another reason for a thicker beam sheet is related to the size of the sampling region. Given a number of drops randomly distributed in a volume such that the mean distance between drop is denoted by s, then there is a lower limit of the smallest volume that can be sampled and still return the correct number density,

which is s^3 . Sampling with a beam sheet dimension less than the mean distance between drops may result in underestimating the total number of drops and over-sampling the large drops. In the sprinkler experiment, the laser beam was expanded in only one direction, leaving the sheet thickness equal to the initial beam diameter of 5 mm. The calculated water flow rate from the measured drop diameters and the mean axial velocity of the drops matched with the rotameter flow rate to within the measurement error.

MEASUREMENTS IN SPRINKLER SPRAYS

Images of fluorescence and Mie scattering from spray drops are shown in Figs. 6 and 7. The images are 84 mm by 118 mm sections of the overall imaged area of 250 mm cm by 350 mm. The camera *f*-number is 2.8 and the magnification is 0.1. 355-nm excitation consistently gives a much redder drop than 532-nm excitation, due to the 532-nm scattered light from the visible radiation. The 355-nm beam precedes the visible by 1 ms, which was verified using an oscilloscope triggered by a photodiode. The 532-nm laser power in Fig. 6 is 10 mJ/pulse while the power in Fig. 7 is 200 mJ/pulse. The 355-nm power and dye concentration are held constant.

At low 532-nm laser power, there are clear particle pairs throughout the image. The drops illuminated by the green laser are only slightly more yellow than the red



Fig. 6 Low 532-nm laser power, 10 mJ/shot. UV laser power is 120 mJ/shot, imaged area is 84 mm by 118 mm.



Fig. 7 High visible laser power, 200 mJ/shot. UV laser power is 120 mJ/shot, imaged area is 84 mm by 118 mm.

drops, making distinction in colors difficult. Only due to the direction of gravity can the drop sequence be known and the velocity determined. The velocity of the large drops can be easily measured, but almost no small drops are visible. Increasing the 532-nm laser power to 200 mJ/pulse improves the color differentiation between the two drops. More particle pairs are indicated but unpaired green drops appear as a result of the higher intensity of scattering. The drop size at low 532-nm power was the same for both laser beams, while at higher laser powers all 355-nm drops are smaller than the corresponding 532-nm drops. Drops illuminated by 532 nm tend to have three types of images. In the first type, drops are solid or faint green with no fluorescence, indicating that they are at the edges of the beam or caused by secondary scattering of the laser sheet. The second type has a halo of green scattering completely or partially surrounding a fluorescent core. These are most likely small drops inside the light sheet. Finally, large drops have bright green scattering on the incident side of the laser beam while the rest of the drop image is dominated by a yellowish fluorescence that delineates the drop perimeter.

Figure 8 is an enlargement of the highest visible laser power image, Fig. 7. In this image, two drops appear to coalesce as they are falling. The initial UV beam indicates two fluorescence centers that are disconnected while the second visible laser indicates two bright centers with a single surrounding drop that is oblong. A green



Fig. 8 Enlargement of a small region of Fig. 7. The upper reddest drop is caused by UV excitation. Its size is 1.47 mm in diameter or 21 pixels. The bright yellow drops are caused by visible radiation. A green corona appears due to the scattering at the front of the drop.

corona is observed on one side while red fluorescence dominates the rear edge of the drop. The uppermost UV illuminated drop measures 1.47 mm or 21 pixels across, while the corresponding visible drop is approximately 75% larger. The velocity of the drops is easily measured from drop center to drop center. The radial component is 3.3 m/s outward and the axial component is 5.74 m/s downward, resulting in a speed of 6.6 m/s.

Size and Velocity Distributions

Using the technique developed in this paper, images of water sprays from an 8-mm nozzle and three combinations of flow rate and nozzle angle were analyzed. The images were taken with a Quantaray red filter to remove any scattering, therefore velocity was indicated by the direction of gravity. $f^{\#}$ of 1.2 was used and the magnification was 0.1. As discussed earlier, the minimum fluorescence signal depends on $f^{\#}$ of the lens and the magnification. Based on Eq. (1) and Fig. 3, the minimum detectable fluorescence results from a drop of approximately 35 μ m. The image resolution was dominated by the film resolution resulting in an expected minimum measurable diameter of 158 μ m. Based on Kadambi's [4] criterion of 3 pixels



Fig. 9 Drop trajectories for a nozzle with an orifice diameter of 8 mm. Drop trajectories are indicated by the three lines. The spray cone angle plays an important role in the droplet spread pattern.



Fig. 10 Drop velocities for a nozzle with an orifice of 8 mm. Velocities are similar at 5 m/s for each of the flows.



Fig. 11 Drop-size distribution for a nozzle of 8-mm orifice diameter. Distribution includes all drops identified in the field.



Fig. 12 Cumulative number distribution for a nozzle with an orifice diameter of 8 mm. A diameter of 0.5 represents the midpoint in the size distribution since half of the particles is larger and half is smaller.



Fig. 13 Cumulative volume fraction for a nozzle of 8-mm orifice diameter. At a drop diameter corresponding to a faction of volume of 0.5, one half of the volume is carried by drops of a larger diameter and the other half is carried by drops of a smaller diameter.

per particle, the actual minimum measurable diameter is $210 \mu m$. Although drops of smaller diameters can be detected, their diameters cannot be accurately determined.

Particle trajectories are indicated by the instantaneous drop locations in Fig. 9 for the three cone angles. The sprays originated at the 0,0 point and were directed downward and outward at an angle determined by the cone angle of the nozzle. Measurements are made with 5 gpm and a cone angle of 90, 4 gpm and 120 and 3 gpm and 140. The corresponding velocities of particle pairs are shown in Fig. 10. Very few images are required to determine the flow trajectories, velocities, and statistics of the spray distribution. For example, in this case two images were used.

Figures 11, 12, and 13 describe the spray statistics. In each of these images, the drop sizes below 150 μ m have been binned together at 100 μ m. The lowest resolvable drop size is 200 μ m, which is the second bin in the graphs. Figure 11 is the drop-size distribution function. The peaks have been normalized to indicate the spread. The 5 gpm and 4 gpm drop distributions are similar, while 3 gpm indicates larger diameter drops that account for a higher percentage of flow. It should be noted again that although the drops cannot be accurately sized, they are observable and therefore the large size bin into which there are placed indicates the possible error in size estimation.

Figure 12 is the cumulative number distribution, where 0.5 represents half of the total particles in the flow. The statistics indicate that over half of the observed particles in the flow are below the accurately measurable limit of the imaging systems. However, the cumulative volume fraction in Fig. 13 indicates that these particles carry about 0.2% of the water flow rate. The cumulative number distribution also indicates that the lower flow rates have a higher fraction of larger drops, which is indicated in the cumulative volume fraction graph for 3 gpm.

CONCLUSIONS

In measuring large fields of view, delectability of drop diameters down to 35 μ m is possible but size measurement is limited by fluorescence intensity and collection optics parameters. Fluorescence curves indicate that the proper concentrations of dye for maximum fluorescence imaging are around 0.0033 g/l for rhodamine. In order to detect small drops, low *f*# is desired; however there is limit to *f*# beyond which the ability to accurately measure size is impeded. Accurate measurements of drop sizes greater than 210 μ m were obtained in this work in a field of view of 250 mm × 350 mm by using fluorescence. These measurements are limited only by the film resolution and the standard digital resolution requirement of three pixels per particle. Scattering images did not prove to adequately represent the particle size. The effect of variation of intensity across the beam sheet, depth of focus, and volumetric response of the fluorescence signal combine to give varying drop sizes. These sizes varied by 8% and were observed to give an estimated drop size 7% lower than physical measurements.

Using the technique developed, particle tracking velocimetry and imaging (PTVI), size measurements of water drops in large-scale sprinkler flows were conducted. Spray patterns, drop velocities and drop sizes were measured to provide data on instantaneous and time-averaged water delivery density for three separate spray conditions. Spray number distributions indicate that many of the drops are below the measurable size, but volume measurements indicate that 99.8% of the flow is carried by drops of measurable size.

ACKNOWLEDGEMENTS

Financial support from NIST is gratefully acknowledged under the GRANT # 60NANB8D0080.

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