Trustworthy interface compliancy: data model adaptation

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Abstract

In component-based software development approaches, components are considered as black boxes, communicating through required and provided interfaces which describe their visible behaviors. Each component interface is equipped with a suitable data model defining all the types occurring in the signature of interface operations. The provided interfaces are checked to be compatible with the corresponding required interfaces, by the way of adapters. We propose a method to develop and verify these adapters when the interface data models are different, using the formal method B. The use of B assembling and refinement mechanisms eases the verification of the interoperability between interfaces and the correctness of the component assembly.

Keywords: Component-based approach, correctness, interoperability, formal method, adapter.

1 Introduction

Component orientation is a new paradigm for the development of software-based systems. The basic idea is to assemble the software by combination of pre-fabricated parts called software components, instead of developing it from scratch. This procedure is similar to the construction methods applied in other engineering disciplines, such as electrical or mechanical engineering.

Software components are put together by connecting their interfaces. A provided interface of one component can be connected with a required interface of another component if it offers the services needed to implement the required interface. Hence, an appropriate description of the interfaces of a software component is crucial. In earlier papers [4,6,11], we have investigated how to formally specify interfaces of software components and how to demonstrate their interoperability, using the formal method B. Each component interface is equipped with a suitable data model defining all the types occurring in the signature of interface operations.

In this paper, we study how to connect components by the way of adapters when their interface data models are different. We propose a method in three steps to build a trustworthy adapter following a refinement process: we start with the required
interface and refine it until we can include the provided one. Each step expresses a level of interoperability, is supported by the prover and help us to establish the correctness of the adaptation.

The rest of the paper is organized as follow: in Section 2, we describe how we support component-based development using the formal method B. We then describe our method to connect components in case of mismatching interface data models in Section 3. The method is illustrated by the case study of an embedded system presented in Section 4. The paper finishes with the discussion of related work in section 5 and concluding remarks in section 6.

2 Using B for component-based development

We briefly describe the formal method B and explain how we use it in the context of component-based software. We formally express provided and required interfaces using B models in order to verify their compatibility.

2.1 The formal method B

B is a formal software development method based on set theory, which supports an incremental development process using refinement [1]. Starting out from a textual description, a development begins with the definition of an abstract model, which can be refined step by step until an implementation is reached. The refinement of models is a key feature for incrementally developing more and more detailed models, preserving correctness in each step.

The method B has been successfully applied in the development of several complex real-life applications, such as the METEOR project [2]. It is one of the few formal methods which has robust and commercially available support tools for the entire development life-cycle, from specification down to code generation [3]. It provides structuring primitives that allow one to compose models in various ways. Proofs of invariance and refinement are part of each development. The proof obligations are generated automatically by support tools such as AtelierB [16] or B4free [5]. Checking proof obligations with B support tools is an efficient and practical way to detect errors introduced during development.

2.2 Specifying component architectures

We define component-based systems using UML 2.0 composite structure diagrams [13]. They express the overall architecture of the system in terms of components and their required and provided interfaces. UML 2.0 Class diagrams serve to express interface data models with their different attributes and methods.

Component interfaces are then specified as B models, which increases confidence in the developed systems: the correctness of the specifications, as well as the correctness of the refinement process can be checked with support tools. In an integrated development process, the B models can be obtained by applying systematic derivation rules from UML to B [10,9].
2.3 Proving interoperability of component interfaces

The components must be connected in an appropriate way. To guarantee interoperability of components, we must consider each connection of a provided and a required interface contained in a software architecture and try to show that the interfaces are compatible. Using the method B, we prove that the B model of the provided interface is a correct B refinement of the required one. This means that the provided interface constitutes an implementation of the required interface, and we conclude that the two components can be connected as intended [4].

Often, to construct a working component architecture, adapters have to be defined, connecting the required interfaces to the provided ones. An adapter is a piece of glue code that realizes the required interface using the provided interface. At the signature level, it expresses the mapping between required and provided variables. In [11], we have studied an adapter specification and its verification by giving a B refinement of the adaptation that refines the B model of the required interface including the B model of the provided (previously incompatible) interface.

2.4 An example of architecture

We illustrate our method with the case study of an embedded system where different sensors send alarm events. These alarms can be canceled by a control console and are memorized by a centralized database. The software architecture of this system is shown Figure 1 using the syntax of composite structure diagrams. It uses three COTS components:

- The component Database provides database functionalities described by its provided interface Database_O as presented Figure 2 by UML diagrams and its associated B model (with only its signature). The B model of this interface with its data model and one of the operations is given Figure 4 (listing 1): (i) the types used in the interface, (ii) variables as far as necessary to express the effects of the operations, (iii) an invariant on these variables and (iv) an operation specification.
- The component SensorDriver software part of each sensor requires an interface Sensor_U to signal warning and error alarms to the system. These alarms need to be saved in the database. This component is used twice.
- The component ConsoleDriver, in charge to drive an alarm control console, requires an interface Console_U in order to query and cancel the alarms saved in the database.
The interface Alarms, described Figures 3 and 4 (listing 2), expresses the global requirement of the alarms shared between the sensors and the console. Listing 3 of Figure 4 presents the types used in Alarms.

To assemble these three COTS, three adapters have been introduced:
• The adapter `Alarms_DB` to map the provided interface `Database_O` that shares the global resources, to the interface `Alarms_U` (see Figures 1 and 5).

![Figure 5. Adapter Alarms_DB](image)

• Two adapters `Console_Alarms` and `Sensor_Alarms` provide the required interface of each driver component using the interface `Alarms_U`.

In the rest of this paper, we focus on the development and the correctness of the adapter `Alarms_DB` which must provide `Alarms_U` using `Database_O`. In terms of B models, we have to prove that `Alarms_DB` is a refinement of `Alarms_U` including `Database_O` [11] as shown Figure 5.

### 3 Trustworthy method to adapt interface data models

Let `I_U` be an interface required by a component `A` and `I_O` another interface provided by a component `B`. Our goal is to adapt the data model of `I_U` using the data model of `I_O`. In other words, the adapter that we are developing, must express the variables, their data types and the operations of `I_U` in terms of the variables, data types and operations of `I_O`.

`I_U` and `I_O` are defined by B models. We will refer to their variables `V_U` and `V_O`, and to their operations `OP_U` and `OP_O` respectively. We notice `D_U` (resp. `D_O`) the data types of the variables `V_U` (resp. `V_O`) as presented Figure 6.

![Figure 6. Process of the adapter development](image)

The adapter must be trustworthy and its proof becomes complex when data models of `I_U` and `I_O` are different. To ease this proof, we develop the adapter by incremental refinements guided by the transformation of variables of `I_U` into the variables of `I_O`.

#### 3.1 Process description

The adaptation process is guided by the interface `I_O` and consists of three refinement steps. Each step is proved by using the B refinement mechanism.
(1) **Variables adaptation**

This step provides a matching between the variables of $I_U$ and $I_O$:

- each variable of $V_U$ is transformed into a new variable of $V'_U$, “corresponding to” a variable of $V_O$, using the data types $D_U$;
- the body of each operation $OP_U$ is transformed with respect to these new variables into $OP'_U$.

(2) **Data types adaptation**

This step provides a matching between the data types of $I_U$ and $I_O$:

- each variable of $V'_U$ expressed on $D_U$ is transformed into a new variable of $V''_U$ expressed using the data types $D_O$. To do that, relations between $D_U$ and $D_O$ have to be defined;
- the body of each operation $OP'_U$ is transformed with respect to these new variables $V''_U$ into $OP''_U$.

(3) **Provided interface inclusion**

This step, which have been prepared by the two previous ones, consists in:

- associating each variable of $V''_U$ to $V_O$ variables,
- expressing each operation of $OP''_U$ in terms of the call the relevant operations of $OP_O$.

### 3.2 B as a guideline for the adaptation steps

When the required and the provided interfaces are defined on the same data types, the adaptation becomes a problem of transforming variables and calling the right operations. Similarly, when the interfaces are similar modulo their data types, the problem is reduced to find whether $D_U$ are subtypes of $D_O$, and then indeed calling the operations with the transformed variables. In that case, the role of the adapter is simply the role of a variable wrapper.

With the use of B, the adaptation process and therefore the adapter itself, is validated by the proof of the different refinement steps. A direct consequence is that the adaptation process is less guided by the developer’s intuition and more by mathematical and logical laws. That means that each step of the process might require several refinement steps in practice in order to provably guarantee that the transformation is correct. As a matter of fact, the B refinement mechanism encourages this practice.

Furthermore, in some transformation steps, functions are introduced as constants, which will need to made explicit in the implementation step. Hence our method is no silver bullet: great care has to be taken when these functions appear. The developer of the adapter will have to ensure that the translation functions exist. Their existence can be more easily stated if the refinement steps are limited to simple, intuitive and progressive transformations. For instance, instead of transforming enumerated values of a set directly to the set of natural numbers, it is wiser to first translate it to a set of numbers modulo the number of enumerated values and then translate it to the full set of natural numbers. The proof of the refinements become easier.
4 Case study

We now show the application of the previous development process to develop and prove an adapter that provides the interface data model of Alarms_U using the interface data model of Database_O. Each time we will refer to a listing in this section, we implicitly refer to figure 7. The specification of the operations (not shown in this figure) is of course modified according to the transformations realized at each step 1.

4.1 Variables adaptation

The first step consists in adapting alarms and active_alarms of the interface data model of Alarms_U to the interface data model of Database_O. In this step, we do not introduce new data types. In the database, each entry in the table is characterized by an identifier Uid which has a corresponding Value and an Attribute. Guided by these three variables, we choose to associate the alarm identifiers (alarms_ids) with the Uid field, the type of an alarm (AlarmTypes) with the Value field and its activity status (AlarmStatus) with the Attribute field.

This matching between an alarm identifier and its attributes can be easily expressed by B functions. Hence we come up with a function for expressing the type of an alarm, and a second one for the status of an alarm as illustrated listing 4. The proof of this refinement consists of 18 formulas, whose 4 have been proved interactively.

4.2 Data types adaptation

The second step might possibly be the harder one: great care must be taken when casting the variables from one type to another one. This is because typecasting is a frequent source of bugs, as limit conditions are often overlooked. The proof process exhibits these conditions and obliges to check their validity. In our process, the typecasting functions are introduced as constants. It means that the validity of the adaptation relies on the existence of these functions, hence it is wiser to choose typecasting functions with well-understood mathematical properties. We broke down the “data types adaptation” step into three refinements, characterized as follows:

- Typecasting the non-functional variables (alarms_ids)
- Typecasting the domain (in the mathematical sense) of each functional variable (alarms_type and alarms_status)
- Typecasting the codomain of each functional variable (the already transformed alarms_type and alarms_status).

4.2.1 Typecasting the non-functional variables

The alarms_ids variable will be represented in the end by the Uid field of the database. We thus introduce a constant id_cast in order to typecast from AlarmsIds to the natural numbers, i.e. the type of the Uid field. We therefore represent the alarms_ids

1 Complete B models are published in []
4.2.2 Typecasting the domain of each functional variable

The `alarms_status` and `alarms_type` depend on `alarms_ids`. As `alarms_ids` has been transformed into `nat_ids`, we must transform `alarms_status` and `alarms_type` so that they depend rather on `nat_ids`. We thus replace them with their equivalent `nat_status` and `nat_type`. The result is presented in listing 6. The proof of this refinement consists of 14 formulas, whose 5 have been proved interactively.

4.2.3 Typecasting the codomain of each functional variable

At this step, the codomains of `nat_status` and `nat_type` do not appear in the data types of `Database_O`. We need to typecast these codomains, namely `AlarmStatus` and `AlarmTypes`, to the corresponding data types fields of the database, i.e. `Attribute`
and Value respectively. These fields contain natural numbers, hence the typecasting functions will map AlarmStatus and AlarmTypes to natural numbers. These functions are introduced as constants and named status_cast and type_cast.

We thus introduce the variables status_nn and type_nn which correspond to the nat_status and nat_type respectively. As the codomains of status_nn and type_nn are the natural numbers, the codomains of nat_status and nat_type have been transformed by the typecasting functions mentioned above. For consistent notations, we rename nat_ids into ids_nn.

We finally introduce a new variable uid_gen for producing a new unique index each time a new alarm will be added in the database. All these transformations are shown listing 7. The proof of this refinement consists of 20 formulas, whose 6 have been proved interactively.

4.3 Provided interface inclusion

In the last step, we establish the relationship between status_nn and type_nn and the fields of the database as illustrated listing 8. We also do the calls to the operations of the database with the transformed data model. The proof of this refinement consists of 19 formulas, whose 5 have been proved interactively.

The proof of this last step is most difficult to perform because it relies on the proofs made along the refinement and the proofs of the Database_O abstract model. Our approach brought a benefit here: while the formulas are bigger in size because of the size of the terms, they have a shape similar with the proof obligations of the provided interface. Hence the proofs can be done by following roughly the proof steps for the provided interface.

If we take into account all the B models involved in this case study (i.e. the interfaces of figure 4 and the refinements of figure 7), there were 108 formulas involved in the proof process, among which 30 formulas had to be proved interactively.

5 Related work

One of the first approaches of module reuse through interface adaptation is the approach of Purtilo and Atlee [14]: they use a dedicated language (called Nimble) for relating a required interface to a provided interface, where the adaptation is made by the developer. Our approach is similar up to the formalism used for representing the interfaces: instead of a dedicated language, we use UML and the B method. Our approach thus has the benefit of relying on standards. Furthermore we overcome the limited semantics of their approach because we use a formal tool for expressing and verifying our interface adaptation.

Dynamic component adaptation [12,7] goes further than our approach by proposing methods for adapting at run-time components by finding suitable adapter components based on the interfaces of the components to adapt. Unfortunately these methods have strong requirements (knowing inheritance relationships, runtime mapping of interface relationships,...) and rely primarily on types and/or object-oriented peculiarities, hence they are limited to subtype-like adaptations. This is not possible with our approach because trustworthiness would require also
proving these strong requirements at run-time. Our method allows nevertheless a broader range of possible adaptations (not limited to subtypes of a provided interface).

The refinement steps of our approach for building an adapter can also be viewed as steps for building morphisms between interfaces. Such methods, for instance the methods presented by Smith [15], are based on signature algebras and theory category. Our approach is rather practical because we chose the B method for expressing the interfaces. The B method is indeed easier for software engineers to understand because it is based on set theory. Our results nonetheless resemble much with interface morphisms, thus these methods could provide means for automating our approach better.

6 Conclusion

The component-based paradigm has received considerable attention in the software development field in industry and academia like in other engineering domains. In this approach, components are considered as black-boxes described by their visible behavior and their required and provided interfaces. To construct a working system out of existing components, adapters are introduced. An adapter is a piece of glue code that realizes the required interface using the provided interfaces. It expresses the mapping between required and provided variables and how required operations are implemented in terms of the provided ones. We have presented a method in three steps to adapt complex data models, each step expressing a level of interoperability and establishing the correctness of the adaptation.

Using the formal method B and its refinement and assembling mechanisms to model the component interfaces and the adapters, we pay special attention to the question of guaranteeing the interoperability between the different components. The B prover guarantees that the adapter is a correct implementation of the required functionalities in terms of the existing components. With this approach, the verification of the interoperability between the connected components is achieved at the signature, the semantic and the protocol levels.

We are currently working on a method for adding dependability features to component-based software systems. The method is applicable if the dependability features add new behavior to the system, but do not change its basic functionality [8]. The idea is to start with a software architecture whose central component is an application component that implements the behavior of the system in the normal case. The application component is connected to other components, possibly through adapters. It is then possible to enhance the system by adding dependability features in such a way that the central application component remains untouched. Adding dependability features necessitates to evolve the overall system architecture by replacing or newly introducing hardware or software components. The adapters contained in the initial software architecture have to be modified, whereas the other software components need not to be changed. Thus, the dependability of a component-based system can be enhanced in an incremental way.
References


A Source code of B models and refinements

MODEL Database_0

SETS
Indices = \{Uid, Value, Attribute\}

VARIABLES
table

INARIANT
\text{table} \in \text{Indices} \rightarrow (N \rightarrow N) \land
\text{dom}(\text{table}(\text{Uid})) = \text{dom}(\text{table}(\text{Value})) \land
\text{dom}(\text{table}(\text{Uid})) = \text{dom}(\text{table}(\text{Attribute})) \land
\text{table}(\text{Uid}) \in (N \rightarrow N)

INITIALISATION
\text{table} := \{ \text{Uid} \mapsto \emptyset, \text{Value} \mapsto \emptyset, \text{Attribute} \mapsto \emptyset \}

OPERATIONS

\text{add_row}(\text{uid}, \text{value}, \text{attr}) =
\text{PRE}
\text{uid} \in \mathbb{N} \land
\text{value} \in \mathbb{N} \land
\text{attr} \in \mathbb{N} \land
\forall ii .(\{ ii \in \text{dom}(\text{table}(\text{Uid})) \Rightarrow (\text{uid} \neq \text{table}(\text{Uid})(ii)))
\text{THEN}
\text{ANY indice}
\text{WHERE indice} \in \mathbb{N}_1 - \text{dom}(\text{table}(\text{Uid}))
\text{THEN}
\text{table} := \text{table} \downarrow\{ \text{Uid} \mapsto (\text{table}(\text{Uid}) \downarrow \{ \text{indice} \mapsto \text{uid} \}),
\text{Value} \mapsto (\text{table}(\text{Value}) \downarrow \{ \text{indice} \mapsto \text{value} \}),
\text{Attribute} \mapsto (\text{table}(\text{Attribute}) \downarrow \{ \text{indice} \mapsto \text{attr} \})\}
\text{END}

\text{remove_row}(\text{uid})(\text{uid}) =
\text{PRE}
\text{uid} \in \text{ran}(\text{table}(\text{Uid}))
\text{THEN}
\text{ANY indice}
\text{WHERE indice} \in \text{dom}(\text{table}(\text{Uid})) \land \text{table}(\text{Uid})(\text{indice}) = \text{uid}
\text{THEN}
\text{table} := \text{table} \downarrow \{ \text{Uid} \mapsto (\text{dom}(\text{table}(\text{Uid})) \downarrow \{ \text{indice} \mapsto \text{uid} \}) \downarrow \text{table}(\text{Uid}),
\text{Value} \mapsto (\text{dom}(\text{table}(\text{Value})) \downarrow \{ \text{indice} \mapsto \text{value} \}) \downarrow \text{table}(\text{Value}),
\text{Attribute} \mapsto (\text{dom}(\text{table}(\text{Attribute})) \downarrow \{ \text{indice} \mapsto \text{attr} \}) \downarrow \text{table}(\text{Attribute})\}
\text{END}

\text{update_attribute}(\text{uid}, \text{new_attr}) =
\text{PRE}
\text{uid} \in \text{ran}(\text{table}(\text{Uid})) \land \text{new_attr} \in \mathbb{N}
\text{THEN}
\text{ANY indice}
\text{WHERE indice} \in \text{dom}(\text{table}(\text{Uid})) \land \text{table}(\text{Uid})(\text{indice}) = \text{uid}
\text{THEN}
\text{table} := \text{table} \downarrow \{ \text{Attribute} \mapsto (\text{table}(\text{Attribute}) \downarrow \{ \text{indice} \mapsto \text{new_attr} \})\}
\text{END}

\text{END}

Figure A.1. B model of Database_0
**MODEL** Alarms_U  
**SEE** Types  
**VARIABLES**  
alarms, active_alarms  
**INVARIANT**  
alarms ⊆ AlarmIds ∧  
active_alarms ⊆ alarms  
**INITIALISATION**  
alarms := ∅  
∥ active_alarms := ∅  
**OPERATIONS**  
nb ← number_of_active_alarms =  
BEGIN  
nb := card(active_alarms)  
END;  
active ← get_active_alarms =  
BEGIN  
active := active_alarms  
END;  
reset_alarm (aid) =  
PRE aid ∈ active_alarms  
THEN  
active_alarms := active_alarms – {aid}  
END;  
aid ← new_alarm(type) =  
PRE  
type ∈ AlarmTypes  
THEN  
ANY uid  
WHERE uid ∈ AlarmIds – alarms  
THEN  
aid := uid ∥  
alarms := alarms ∪ {uid} ∥  
active_alarms := active_alarms ∪ {uid}  
END  
END  
END

Figure A.2. B model of Alarms_U
REFINEMENT Alarms_DB_ref1
REFINES Alarms_U
SEES Types

VARIABLES
alarms_ids, alarms_status, alarms_type

INVARIANT
alarms_ids = alarms ∧
alarms_status ∈ alarms_ids → AlarmStatus ∧
alarms_type ∈ alarms_ids → AlarmTypes ∧
alarms_status = active_alarms × {Active} ∪
( alarms_ids − active_alarms ) × {Inactive}

ASSERTIONS
( {Active} × active_alarms ∪ {Inactive} × (alarms − active_alarms) ) [{Active}] = active_alarms

INITIALISATION
alarms_ids := ∅
alarms_type := ∅ × AlarmTypes

OPERATIONS

nb ← number_of_active_alarms =
BEGIN
   nb := card( alarms_status⁻¹[{Active}])
END;

active ← get_active_alarms =
BEGIN
   active := alarms_status⁻¹[{Active}]
END;

reset_alarm (aid) =
BEGIN
   alarms_status := alarms_status ≪ { aid → Inactive }
END;

aid ← new_alarm(type) =
ANY uid
WHERE uid ∈ AlarmIds − alarms_ids
THEN
   aid := uid
   alarms_ids := alarms_ids ∪ {uid}
   alarms_type := alarms_type ≪ { uid → type }
   alarms_status := alarms_status ≪ { uid → Active }
END

Figure A.3. Alarms_DB_ref1: first step of the refinement
REFINEMENT Alarms_DB_ref2
REFINES Alarms_DB_ref1
SEES Types
CONSTANTS
  id_cast
PROPERTIES
  id_cast ∈ AlarmsIds → N
VARIABLES
  nat_ids, alarms_status, alarms_type
INVARIANT
  nat_ids = id_cast[alarms_ids]
ASSERTIONS
  ∀ aid ((aid ∈ alarms_ids) ⇒ (id_cast(aid) ∈ id_cast[dom(alarms_type)]))
INITIALISATION
  nat_ids := ∅
  | alarms_status := ∅ × AlarmStatus
  | alarms_type := ∅ × AlarmTypes
OPERATIONS
  aid ← new_alarm(type) =
  ANY uid_nat
  WHERE
    uid_nat ∈ N
    ∧ uid_nat /∈ nat_ids
  THEN
    aid := id_cast⁻¹(uid_nat)
    | nat_ids := nat_ids ∪ {uid_nat}
    | alarms_type := alarms_type ∖ {id_cast⁻¹(uid_nat) → type}
    | alarms_status := alarms_status ∖ {id_cast⁻¹(uid_nat) → Active}
END
END

Figure A.4. Alarms_DB_ref2: second step of the refinement
REFINEMENT Alarms_DB_ref3
REFINES Alarms_DB_ref2
SEES Types
VARIABLES
  nat_ids, nat_status, nat_type
INVARIANT
  nat_status ∈ nat_ids → AlarmStatus ∧
  nat_type ∈ nat_ids → AlarmTypes ∧
  nat_status⁻¹ = (alarms_status⁻¹; id_cast)
INITIALISATION
  nat_ids := ∅
  nat_status := ∅
  nat_type := ∅
OPERATIONS
  nb ← number_of_active_alarms =
  BEGIN
    nb := card( nat_status⁻¹[ {Active} ])
  END;
  active ← get_active_alarms =
  BEGIN
    active := id_cast⁻¹[ nat_status⁻¹[ {Active} ] ]
  END;
  reset_alarm (aid) =
  BEGIN
    nat_status := nat_status ◁{ id_cast (aid) → Inactive }
  END;
  aid ← new_alarm(type) =
  ANY uid_nat
  WHERE
    uid_nat ∈ N
    ∧ uid_nat /∈ nat_ids
  THEN
    aid := id_cast⁻¹(uid_nat)
    nat_ids := nat_ids ∪ {uid_nat}
    nat_type := nat_type ◁{ uid_nat → type }
    nat_status := nat_status ◁{ uid_nat → Active }
  END
END

Figure A.5. Alarms_DB_ref3: third step of the refinement
REFINEMENT Alarms_DB_ref4
REFINES Alarms_DB_ref3
SEES Types
CONSTANTS
type_cast , status_cast
PROPERTIES
  type_cast ∈ AlarmTypes → 1..card(AlarmTypes) ∧
  status_cast ∈ AlarmStatus → 1..card(AlarmStatus)
CONCRETE_VARIABLES
  uid_gen
VARIABLES
  ids_nn , status_nn , type_nn
INVARIANT
  uid_gen ∈ N ∧
  ids_nn = nat_ids ∧
  status_nn ∈ nat_ids → 1..card(AlarmStatus) ∧
  type_nn ∈ nat_ids → 1..card(AlarmTypes) ∧
  uid_gen > max(nat_ids) ∧
  status_nn = (nat_status : status_cast ) ∧
  type_nn = (nat_type; type_cast )
ASSERTIONS
  status_cast−1[status_cast[{Active}]] = {Active}
INITIALISATION
  uid_gen := 0
  ids_nn := ∅
  status_nn := ∅
  type_nn := ∅
OPERATIONS
  nb ←− number_of_active_alarms =
  BEGIN
    nb := card(status_nn−1[status_cast[{Active}]])
  END;
  active ←− get_active_alarms =
  BEGIN
    active := id_cast−1[ status_nn−1[status_cast[{Active}]] ]
  END;
  reset_alarm (aid) =
  BEGIN
    status_nn := status_nn ⊖ { id_cast (aid) ↦ status_cast(Inactive) }
  END;
  aid ←− new_alarm(type) =
  BEGIN
    aid := id_cast−1(uid_gen)
    ids_nn := ids_nn ⊖ {uid_gen}
    type_nn := type_nn ⊖ {uid_gen ↦ type_cast(type)}
    status_nn := status_nn ⊖ {uid_gen ↦ status_cast(Active)}
    uid_gen := uid_gen + 1
  END
END

Figure A.6. Alarms_DB_ref4: fourst step of the refinement
REFINEMENT Alarms_DB_ref5  
REFINES Alarms_DB_ref4  
SEES Types  
INCLUDES Database_O  

INARIANT  
\[
\text{table}(\text{Uid})[\text{dom}(\text{table}(\text{Uid}))] = \text{ids}_{nn} \land
\text{table}(\text{Uid})^{-1}[\text{table}(\text{Attribute})] = \text{status}_{nn} \land
\text{table}(\text{Uid})^{-1}[\text{table}(\text{Value})] = \text{type}_{nn}
\]

INITIALISATION  
\text{uid}_{gen} := 0  

OPERATIONS  

\text{nb} \leftarrow \text{number_of_active_alarms} =  
\text{BEGIN}  
\text{nb} := \text{card}(\text{table}(\text{Uid})[\text{table}(\text{Attribute})^{-1}[\text{status}_{cast}({\text{Active}})])]  
\text{END};  

\text{active} \leftarrow \text{get_active_alarms} =  
\text{BEGIN}  
\text{active} := \text{id}_{cast}^{-1}\text{table}(\text{Uid})[\text{table}(\text{Attribute})^{-1}[\text{status}_{cast}({\text{Active}})])]  
\text{END};  

\text{reset_alarm}(\text{aid}) =  
\text{BEGIN}  
\text{update_attribute}(\text{id}_{cast}(\text{aid}), \text{status}_{cast}(\text{Inactive}))  
\text{END};  

\text{aid} \leftarrow \text{new_alarm}(\text{type}) =  
\text{BEGIN}  
\text{aid} := \text{id}_{cast}^{-1}(\text{uid}_{gen})  
\text{∥ uid}_{gen} := \text{uid}_{gen} + 1  
\text{∥ add_row( uid}_{gen}, \text{type}_{cast}(\text{type}), \text{status}_{cast}(\text{Active}))  
\text{END}  
\text{END}  

Figure A.7. Alarms_DB_ref5: last step of the refinement